Intermediate Microeconomics

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CHAPTER 1

Preference and Indifference Curves



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THE POLICY QUESTION

IS A TAX CREDIT ON HYBRID CAR PURCHASES THE GOVERNMENT'S BEST CHOICE TO REDUCE FUEL CONSUMPTION AND CARBON EMISSIONS?

The US government, concerned about the dependence on imported foreign oil and the release of carbon into the atmosphere, has enacted policies where consumers can receive substantial tax credits toward the purchase of certain models of all-electric and hybrid cars.

This credit may seem like a good policy choice, but it is a costly one; it takes away resources that could be spent on other government policies, and it is not the only approach to decreasing carbon emissions and dependency on fossil fuels. So how do we decide which policy is best?

Suppose that this tax credit is wildly successful and doubles the average fuel economy of all cars on US roads (this is clearly not realistic but useful for our subsequent discussions). What do you think would

happen to the fuel consumption of all US motorists? Should the government expect fuel consumption and carbon emissions of US cars to decrease by half in response?

The answers to these questions are critical when choosing among the policy alternatives. In other words, is offering a subsidy to consumers the most effective way to meet the policy goals of decreased dependency on foreign oil and carbon emissions? Are there more efficient—that is, less expensive—ways to achieve these goals? The ability to predict with some accuracy the response of consumers to this policy is vital to determining the merits of the policy before millions of federal dollars are spent.

Consumption decisions, such as how much automobile fuel to consume, come fundamentally from our preferences—our likes and dislikes. Human decision-making, driven by our preferences, is at the core of economic theory. Since we can't consume everything our hearts desire, we have to make choices, and those choices are based on our preferences. Choosing based on likes and dislikes does not mean that we are selfish—our preferences may include charitable giving and the happiness of others.

In this chapter, we will study preferences in economics.

LEARNING OBJECTIVES

1.1 Fundamental Assumptions about Individual Preferences

Learning Objective 1.1: List and explain the three fundamental assumptions about preferences.

1.2 Graphing Preferences with Indifference Curves

Learning Objective 1.2: Define and draw an indifference curve.

1.3 Properties of Indifference Curves

<u>Learning Objective 1.3</u>: Relate the properties of indifference curves to assumptions about preference.

1.4 Marginal Rate of Substitution

<u>Learning Objective 1.4</u>: Define marginal rate of substitution.

1.5 Perfect Complements and Perfect Substitutes

Learning Objective 1.5: Use indifference curves to illustrate perfect complements and perfect substitutes.

1.6 Policy Example

Is a Tax Credit on Hybrid Car Purchases the Government's Best Choice?

Learning Objective 1.6: Apply indifference curves to the policy of a hybrid car tax credit.

1.1 FUNDAMENTAL ASSUMPTIONS ABOUT INDIVIDUAL PREFERENCES

Learning Objective 1.1: List and explain the three fundamental assumptions about preferences.

To build a model that can predict choices when variables change, we need to make some assumptions about the preferences that drive consumer choices. Economics makes three assumptions about pref-

erences that are the most basic building blocks of our theory of consumer choice. To introduce these, it is useful to think of collections or bundles of goods. To simplify, let's identify two bundles, \boldsymbol{A} and \boldsymbol{B} . The way we think of preferences always boils down to comparing two bundles. Even if we are choosing among three or more bundles, we can always proceed by comparing pairs and eliminating the lesser bundle until we are left with our choice.

When we call something a **good**, we mean exactly that—something that a consumer likes and enjoys consuming. Something that a consumer might not like we call a *bad*. The fewer bads consumed, the happier a consumer is. To keep things simple, we will focus only on goods, but it is easy to incorporate bads into the same framework by considering their absence—the fewer the bads, the better.

The three fundamental assumptions about preferences are the following:

1. Completeness.

We say preferences are *complete* when a consumer can always say one of the following about two bundles:

1. A is preferred to B,

 \boldsymbol{B} is preferred to \boldsymbol{A} , or

2. A is equally good as B.

2. Transitivity.

We say preferences are *transitive* if they are internally consistent:

1. If A is preferred to B

and B is preferred to C,

- 2. then it must be that A is preferred to C.
- 3. More is better.
 - 1. If BundleA represents more of at least one good and no less of any other good than BundleB.
 - 2. then A is preferred to B.

The most important results of our model of consumer behavior hold when we only assume completeness and transitivity, but life is much easier if we assume more is better as well. If we assume free disposal (we can get rid of extra goods at no cost), the assumption that more is better seems reasonable. It is certainly the case that more is not worse in that situation, and so to keep things simple, we'll maintain the standard assumption that we prefer more of a good than less.

Our model works well when these assumptions are valid, which seems to be most of the time in most situations. However, sometimes these assumptions do not apply. For instance, in order to have complete and transitive preferences, we must know something about the goods in the bundle. Imagine an American who does not speak Hindi entering an Indian restaurant where the menu is entirely in Hindi. Without the aid of translation, the customer cannot act as economic theory would predict.

1.2 GRAPHING PREFERENCES WITH INDIFFERENCE CURVES

Learning Objective 1.2: Define and draw an indifference curve.

Individual preferences, given the basic assumptions, can be represented using something called indifference curves. An **indifference curve** is a graph of all the combinations of bundles that a consumer prefers equally. In other words, the consumer would be just as happy consuming any of them. Representing preferences graphically is a great way to understand both preferences and how the consumer choice model works—so it is worth mastering them early in your study of microeconomics.

Bundles can contain many goods, but to simplify, we will consider only pairs of goods. At first, this may seem impossibly restrictive, but it turns out that we don't really lose generality in so doing. We can always consider one good in the pair to be, collectively, all other consumption goods. What the two-goods restriction does so well is to help us see the trade-offs in consuming more of one good and less of another.

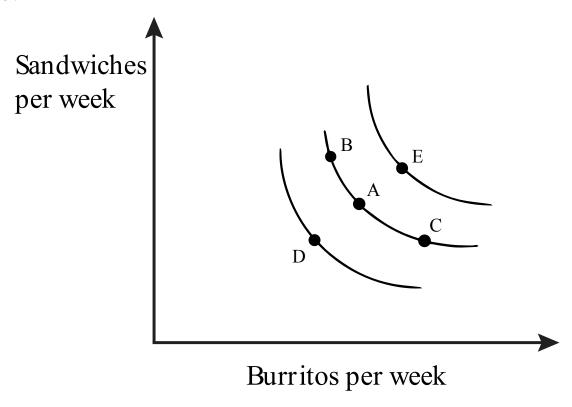


Figure 1.1 Bundles and indifference curves

Figure 1.1 is a graph with two goods on the axes: the weekly consumption of burritos and the weekly consumption of sandwiches for a college student. In the middle of the graph is point A, which represents a bundle of both burritos (read from the horizontal axis) and sandwiches (read from the vertical axis).

Now we can ask what bundles are better, worse, or the same in terms of satisfying this college student. Clearly, bundles that contain fewer of both goods, like BundleD, are worse than A, B, or C because they violate the more-is-better assumption. Equally clear is that bundles that contain more of both goods, like BundleE, are better than A, B, C, and D because they satisfy the more-is-better] assumption.

To create an indifference curve, we want to identify bundles that this college student is indifferent about consuming. If a bundle has more burritos, the student will have to have fewer sandwiches and vice versa. By finding all the bundles that are just as good as A, like B and C, and connecting them with a line, we create an indifference curve, like the one in the middle.

Notice that **figure 1.1** includes several indifference curves. Each curve represents a different level of overall satisfaction that the student can achieve via burrito/sandwich bundles. A curve farther out from the origin represents a higher level of satisfaction than a curve closer to the origin.

Notice also that these curves share a number of characteristics: they *slope downward*, they *do not cross*, and they are all . We explore these properties in more detail in the next section.

1.3 PROPERTIES OF INDIFFERENCE CURVES

Learning Objective 1.3: Relate the properties of indifference curves to assumptions about preference. As introduced in <u>section 1.2</u>, indifference curves have three key properties:

- 1. They are downward sloping.
- 2. They do not cross.
- 3. They are *bowed in* (a non-technical way of saying they are convex to the origin).

For simplicity and clarity, from here on, we will describe preferences that lead to indifference curves with these three properties as standard. This will be our default assumption—that consumers have **standard preferences** unless otherwise noted. As we will see in this chapter, there are other types of preferences that are common as well, and we will continue to study both the standard type and the other types as we progress through the material.

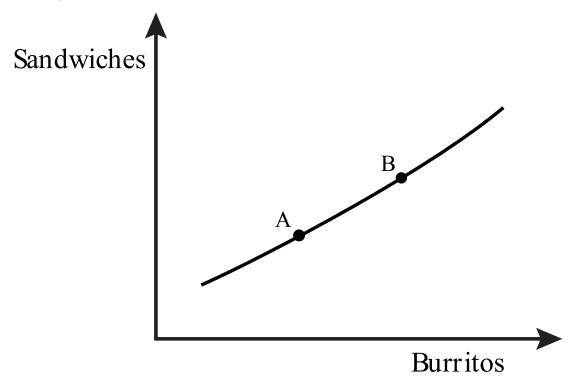


Figure 1.2 Upward-sloping indifference curves violating the more-is-better assumption

To understand the first two properties, it's useful to think about what would happen if they were not true.

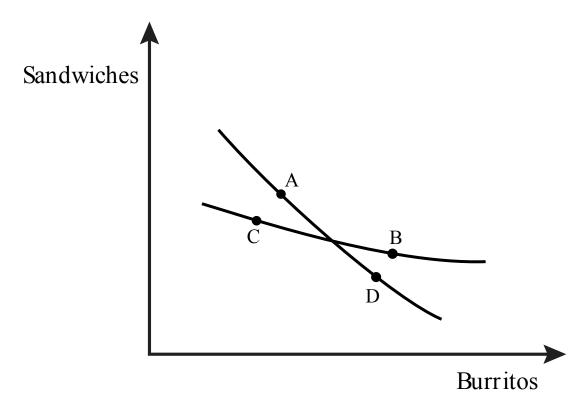


Figure 1.3 Crossing indifference curves violating the transitivity assumption

Think about indifference curves that slope upward, as in **figure 1.2**. In this case, we have two bundles on the same indifference curve, A and B, but B has more of both burritos and sandwiches than does A. So this violates the assumption of more is better. **More is better implies indifference curves are downward sloping.**

Similarly, consider **figure 1.3**. In this figure, there are two indifference curves that cross. Now consider bundle A on one of the indifference curves. It represents more of both goods than bundle C, which lies on the other indifference curve. Because bundle B lies on the same indifference curve as bundle C, the two bundles should be equally preferred, and therefore A should be preferred to B and C. Bundle B also represents more of both goods than bundle D, and therefore B should be preferred to B. However, B is on the same indifference curve as B0, so B2 should be preferred to B2. Since B3 can't be preferred to B4 and B5 preferred to B5 and B6 preferred to B6 and B6 preferred to B6 and B7 preferred to B8 and B8 preferred to B8 and B9 preferred to B8 and B9 preferred to B9 and B9 a

Now we come to the third property: indifference curves bow in. This property comes from a fourth assumption about preferences, which we can add to the assumptions discussed in <u>section 1.1</u>:

4. Consumers like variety.

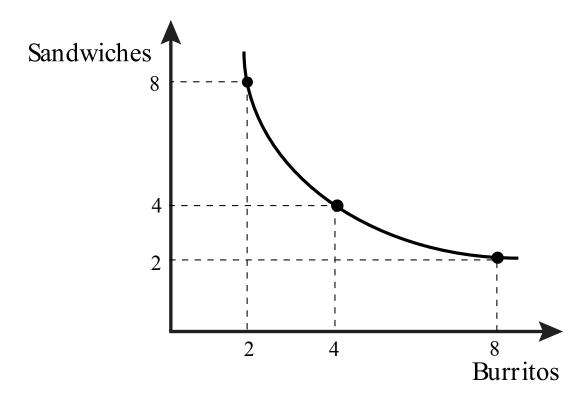


Figure 1.4 Preference for variety resulting in bowed-in indifference curves

The assumption that consumers prefer variety is not necessary but still applies in many situations. For example, most consumers would probably prefer to eat both sandwiches and burritos during a week and not just one or the other (remember, this is for consumers who consider them both goods—who like them). In fact, if you had only sandwiches to eat for a week, you'd probably be willing to give up a lot of sandwiches for a few burritos and vice versa. If you had reasonably equal amounts of both, you'd be willing to trade one for the other, but at closer to one-to-one ratios. Notice that if we graph this, we naturally get bowed-in indifference curves, as shown in **figure 1.4**. **Preference for variety implies that indifference curves are bowed in.**

Remember these three key points about **preferences and indifference curves**:

- 1. *More is better* implies indifference curves are *downward sloping*.
- 2. *Transitivity* and *more is better* imply indifference curves *do not cross*.
- 3. *Preference for variety* implies that indifference curves are *bowed in*.

1.4 MARGINAL RATE OF SUBSTITUTION

Learning Objective 1.4: Define marginal rate of substitution.

From now on, we will assume that consumers like variety and that indifference curves are bowed in. However, it is worth considering examples on either extreme: **perfect substitutes** and **perfect complements**.

When we move along an indifference curve, we can think of a consumer substituting one good for another. Two bundles on the same indifference curve, which represents the same satisfaction from consumption, have one thing in common: they represent more of one good and less of the other. This makes sense given our assumption of "more is better": if more of one good makes you better off, then you must have less of the other good in order to maintain the same level of satisfaction.

In economics, we have a more technical way of expressing this trade-off: the **marginal rate of substitution (MRS)**. The MRS is the number of units of one good a consumer is willing to give up to get one more unit of another good and maintain the same level of satisfaction. This is one of the most important concepts in economics because it is critical to understanding consumer choice.

Mathematically, we express the marginal rate of substitution for two generic goods like this:

$$MRS = rac{\Delta A}{\Delta B}$$

where Δ indicates a change in the quantity of the good.

In the case of our student consuming burritos and sandwiches, the expression would be

$$MRS = rac{\Delta Sandwiches}{\Delta Burritos}.$$

For example, suppose at his current consumption bundle, five burritos and four sandwiches weekly, Luca is willing to give up two burritos to get one more sandwich. Another way of saying the same thing is that Luca is indifferent between consuming five burritos and four sandwiches in a week or three burritos and five sandwiches in a week. The MRS for Luca at that point is

$$MRS = rac{\Delta Burritos}{\Delta Sandwiches} = rac{-2}{1} = -2$$
.

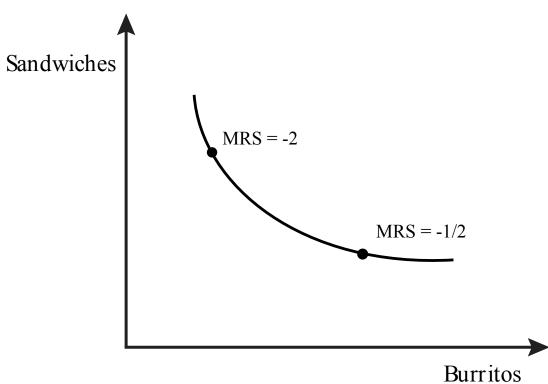


Figure 1.5 Marginal rate of substitution for burritos and sandwiches

Note that the MRS is negative because it represents a trade-off: more sandwiches for fewer burritos. Notice that **figure 1.5** illustrates a change in the good on the vertical axis (sandwiches) over the change in the good on the horizontal axis (burritos). This is the same as saying the rise over the run. From this discussion and graph, it should be clear that the MRS is the same as the slope of the indifference curve at any given point along it.

1.5 PERFECT COMPLEMENTS AND PERFECT SUBSTITUTES

Learning Objective 1.5: Use indifference curves to illustrate perfect complements and perfect substitutes.

We have now studied the assumptions upon which our model of consumer behavior is built:

- 1. Completeness
- 2. Transitivity
- 3. More is better
- 4. Love of variety

It is worth taking a moment to think about two other types of preference relations that are special cases but not uncommon: **perfect complements** and **perfect substitutes**.

Perfect Complements

Perfect complements are goods that consumers want to consume only in fixed proportions.

Consider the example of an iPod and earphones. An iPod is useless without earphones, and earphones are useless without an iPod, but put them together, and voilà, you have a portable stereo, which is worth quite a lot. An extra set of earphones doesn't increase the usefulness of the iPod, and an extra iPod doesn't increase the usefulness of the earphones. So these are things that we consume in a fixed proportion: one iPod goes with one set of earphones. We call such preference relations perfect complements.

Figure 1.6 illustrates the process of drawing indifference curves for perfect complements.

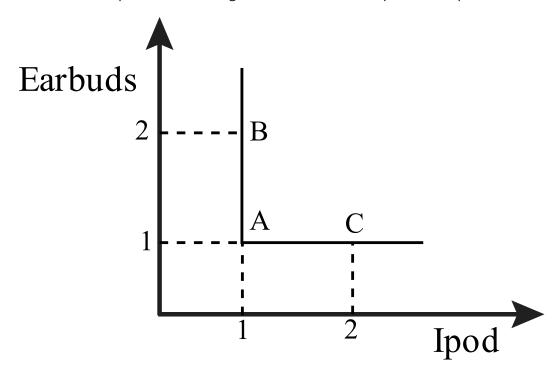


Figure 1.6 Indifference curves for goods that are perfect complements

In **figure 1.6**, when we start with a bundle of one iPod and one set of earbuds (as in bundle A), what are the other bundles that are just as good to the consumer? Two sets of earbuds and one iPod is no better

than one set of earbuds and one iPod, so bundle B lies on the same indifference curve. The same is true for two iPods and one set of earbuds, as in bundle C. From this example, we can see that *indifference* curves for perfect complements have right angles.

Perfect Substitutes

A **perfect substitute** is a good that makes a consumer just as well off as a fixed amount of another good. That is, one unit of one good is just as good as one unit of another good. Both Morton and Diamond Crystal are brands of table salt. For most consumers, a teaspoon of one salt is always just as good as a teaspoon of the other. We call goods like these perfect substitutes.

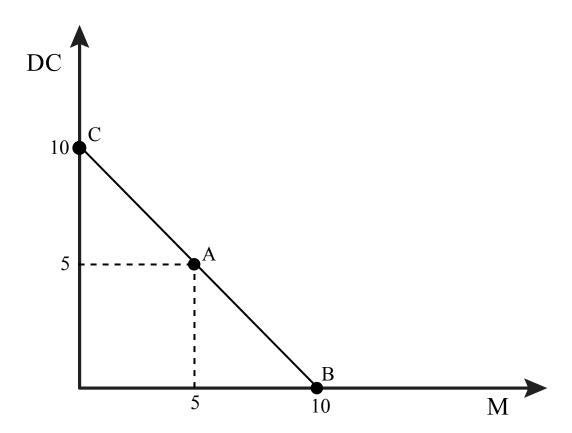


Figure 1.7 Indifference curves for goods that are perfect substitutes

Drawing indifference curves for perfect substitutes is straightforward, as shown in figure **1.7**.

Bundle A in **figure 1.7** contains five teaspoons of each type of salt. This is just as good to the consumer as a bundle with ten teaspoons of Morton salt and zero teaspoons of Diamond Crystal, as in bundle B. It is also just as good as the ten teaspoons of Diamond Crystal and zero teaspoons of Morton in bundle C.

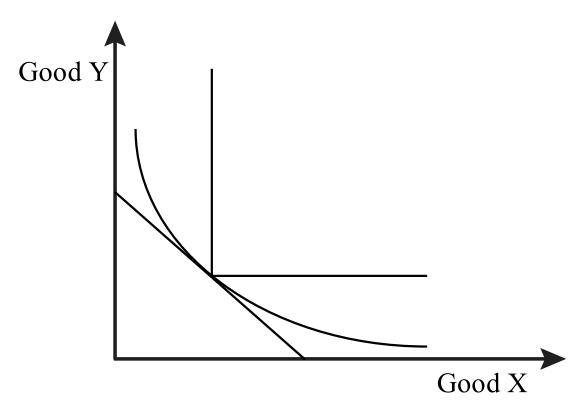


Figure 1.8 The relationship between indifference curves for standard preferences and perfect complements and substitutes

You can think of perfect complements and perfect substitutes as polar extremes of preference relations. **Figure 1.8** shows how a typical indifference curve lies between perfect complements and perfect substitutes. You should understand, when graphically represented, that the *indifference curve for standard preferences lies between perfect complements and perfect substitutes*.

1.6 POLICY EXAMPLE

IS A TAX CREDIT ON HYBRID CAR PURCHASES THE GOVERNMENT'S BEST CHOICE TO REDUCE FUEL CONSUMPTION AND CARBON EMISSIONS?

Learning Objective 1.6: Apply indifference curves to the policy of a hybrid car tax credit.

The issue of consumer preferences is central to the real-world policy question posed at the beginning of this chapter.



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Recall that we are assuming that the tax credit will cause the average fuel economy of US cars to double. So from a consumer behavior perspective, one of the things we want to know in evaluating the policy is whether this improvement in gas mileage will cause an equivalent decrease in the demand for gasoline. In other words, the consumer decision is about the trade-off of purchasing gasoline to travel in a car versus all the other uses of the money spent on gas.

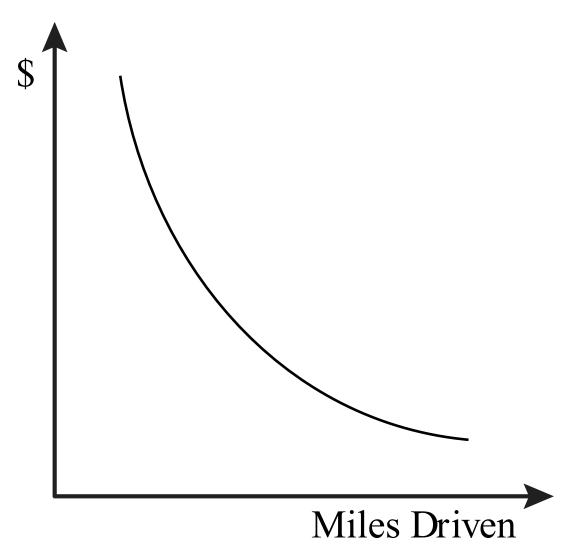


Figure 1.9 Indifference curve for miles driven versus money spent on all other goods

We can apply the principle of preferences and the assumptions we make about them to this particular question by drawing indifference curves, as shown in **figure 1.9**.

We can label one axis of the indifference curve map "miles driven" and the other "money for other consumption." Doing so illustrates how confining ourselves to only two dimensions is really not that confining at all. By considering the other axis as money for all other purchases, we are really looking at the general trade-off between one particular consumption good and everything else that a consumer could possibly consume.

So what would our indifference curve look like? As before, it would be *downward sloping*—surely traveling more by car affords the consumer more freedom of movement and therefore more consumption choices, both of which are goods. The indifference curves would *not cross* for the same reasons discussed in <u>section 1.3</u>. But what about the principle of more is better? The point here is to again think about the principle of free disposal: as long as the ability to drive more miles is not bad (and it is hard to imagine how it could be), then more miles are never worse.

The remaining question is whether the preference for variety is a good assumption in this case. It is helpful to consider the extremes: for those consumers who own cars, never driving any miles is probably not very practical. Likewise, spending one's entire income only on expenses relating to driving one's car

is unappealing. A good assumption, then, is that most people with a car would prefer some combination of miles driven and other consumption to either extreme and we can draw our indifference curves as convex to the origin.

We are not yet in a position to say much about the policy itself, but we have one piece of the model we will use to analyze it. With this indifference curve, we can move on to the other pieces of the model that we will study in chapters 2, 3, and 4.

EXPLORING THE POLICY QUESTION

1. Suppose that a typical consumer is concerned about how their individual driving habits are negatively impacting the environment. How might such a change in attitude change the shape of the consumer's indifference curves?

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

1.1 Fundamental Assumptions about Individual Preferences

Learning Objective 1.1: List and explain the three fundamental assumptions about preferences.

1.2 Graphing Preferences with Indifference Curves

Learning Objective 1.2: Define and draw an indifference curve.

1.3 Properties of Indifference Curves

Learning Objective 1.3: Relate the properties of indifference curves to assumptions about preference.

1.4 Marginal Rate of Substitution

Learning Objective 1.4: Define marginal rate of substitution.

1.5 Perfect Complements and Perfect Substitutes

Learning Objective 1.5: Use indifference curves to illustrate perfect complements and perfect substitutes.

1.6 Policy Example

Is a Tax Credit on Hybrid Car Purchases the Government's Best Choice to Reduce Fuel Consumption and Carbon Emissions?

Learning Objective 1.6: Apply indifference curves to the policy of a hybrid car tax credit.

LEARN: KEY TOPICS

Terms

Completeness

We say preferences are complete when a consumer can always say one of the following about two bundles: A is preferred to B, B is preferred to A, or A is equally good as B.

Transitivity

We say preferences are transitive if they are internally consistent: if A is preferred to B and B is preferred to C, then it must be that A is preferred to C.

More is Better

If bundle A represents more of at least one good and no less of any other good than bundle B, then A is preferred to B.

Indifference Curve

A graph of all the combinations of bundles that a consumer prefers equally. In other words, the consumer would be just as happy consuming any of them.

Marginal Rate of Substitution (MRS)

The MRS is the number of units of one good a consumer is willing to give up to get one more unit of another good and maintain the same level of satisfaction.

Perfect Complements

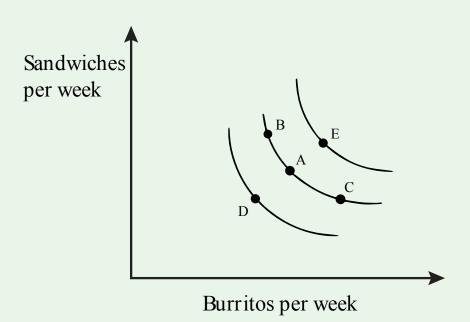
Goods that consumers want to consume only in fixed proportions, i.e., airpods to an iPhone.

Perfect Substitutes

A good that makes a consumer just as well off as a fixed amount of another good, i.e., Morton and Diamond Crystal are brands of table salt. For most consumers, a teaspoon of one salt is always just as good as a teaspoon of the other.

Graphs

Indifference Curve



Bundles and Indifference Curves

Marginal Rate of Substitution

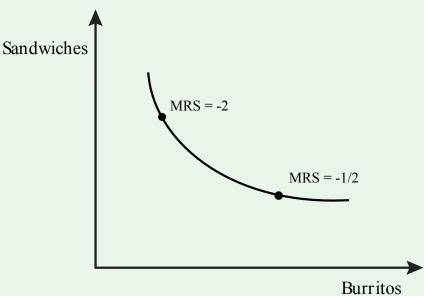


Figure 1.5 Marginal rate of substitution for burritos and sandwiches

Perfect Complements

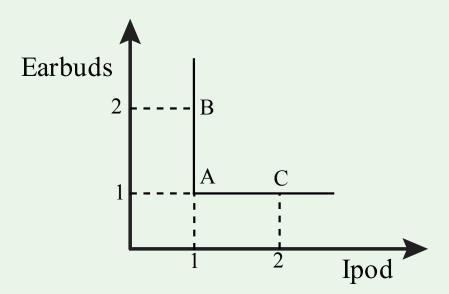


Figure 1.6 Perfect Complements

Perfect Substitutes

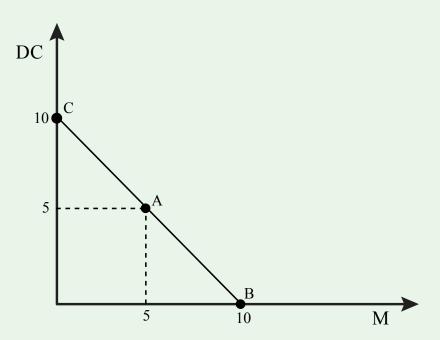


Figure 1.7 Perfect Substitutes

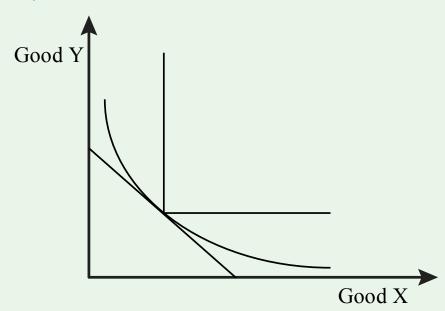


Figure 1.8 The relationship between Standard Preference, Perfect Complements and Perfect Substitutes

Equations

Marginal Rate of Substitution (MRS)

$$MRSbx = rac{\Delta A}{\Delta B}$$

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UTILITY 19

CHAPTER 2

Utility



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THE POLICY QUESTION

IS A TAX CREDIT ON HYBRID CAR PURCHASES THE GOVERNMENT'S BEST CHOICE TO REDUCE FUEL CONSUMPTION AND CARBON EMISSIONS?

US residents and the government are concerned about the dependence on imported foreign oil and the release of carbon into the atmosphere. In 2005, Congress passed a law to provide consumers with tax credits toward the purchase of electric and hybrid cars.

This tax credit may seem like a good policy choice, but it is costly because it directly lowers the amount of revenue the US government collects. Are there more effective approaches to reducing dependency on fossil fuels and carbon emissions? How do we decide which policy is best? To answer this question, policymakers need to predict with some accuracy how consumers will respond to this tax policy before these policymakers spend millions of federal dollars.

We can apply the concept of *utility* to this policy question. In this chapter, we will study utility and utility functions. We will then be able to use an appropriate utility function to derive indifference curves that describe our policy question.

EXPLORING THE POLICY QUESTION

Suppose that the tax credit to subsidize hybrid car purchases is wildly successful and doubles the average fuel economy of all cars on US roads—a result that is clearly not realistic but useful for our subsequent discussions. What do you think would happen to the fuel consumption of all US motorists? Should the government expect fuel consumption and carbon emissions from cars to decrease by half in response? Why or why not?

LEARNING OBJECTIVES

2.1 Utility Functions

<u>Learning Objective 2.1</u>: Describe a utility function.

2.2 Utility Functions and Typical Preferences

Learning Objective 2.2: Identify utility functions based on the typical preferences they represent.

2.3 Relating Utility Functions and Indifference Curve Maps

Learning Objective 2.3: Explain how to derive an indifference curve from a utility function.

2.4 Finding Marginal Utility and Marginal Rate of Substitution

<u>Learning Objective 2.4</u>: Derive marginal utility and MRS for typical utility functions.

2.5 Policy Example

Is a Tax Credit on Hybrid Car Purchases the Government's Best Choice?

Learning Objective 2.5: The Hybrid Tax Credit and customer utility

2.1 UTILITY FUNCTIONS

Learning Objective 2.1: Describe a utility function.

Our preferences allow us to make comparisons between different consumption bundles and choose the preferred bundles. We could, for example, determine the rank ordering of a whole set of bundles based on our preferences. A **utility function** is a mathematical function that ranks bundles of consumption goods by assigning a number to each, where larger numbers indicate preferred bundles. Utility functions have the properties we identified in <u>chapter 1</u> regarding preferences. That is, they are able to order bundles, they are complete and transitive, more is preferred to less, and in relevant cases, mixed bundles are better.

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The number that the utility function assigns to a specific bundle is known as **utility**, the satisfaction a consumer gets from a specific bundle. The utility number for each bundle does not mean anything in absolute terms; there is no uniform scale against which we measure satisfaction. Its only purpose is in relative terms: we can use utility to determine which bundles are preferred to others.

If the utility from bundle A is higher than the utility from bundle B, it is equivalent to saying that a consumer prefers bundle A to bundle B. Utility functions, therefore, rank consumer preferences by assigning a number to each bundle. We can use a utility function to draw the indifference curve maps described in <u>chapter 1</u>. Since all bundles on the same indifference curve provide the same satisfaction and therefore none is *preferred*, each bundle has the same utility. We can therefore draw an indifference curve by determining all the bundles that return the same number from the utility function.

Economists say that utility functions are **ordinal** rather than **cardinal**. Ordinal means that utility functions only rank bundles—they only indicate which one is better, not how much better it is than another bundle. Suppose, for example, that one utility function indicates that $\operatorname{bundle} A$ returns ten **utils** and $\operatorname{bundle} B$ twenty utils. We do not say that $\operatorname{bundle} B$ is twice as good, or ten utils better, only that the consumer prefers bundle B . For example, suppose a friend entered a race and told you she came in third. This information is **ordinal**: You know she was faster than the fourth-place finisher and slower than the second-place finisher. You only know the order in which runners finished. The *individual times* are **cardinal**: if the first-place finisher ran the race in exactly one hour and your friend finished in one hour and six minutes, you know your friend was exactly 10 percent slower than the fastest runner. Because utility functions are ordinal, many different utility functions can represent the same preferences. This is true as long as the ordering is preserved.

Take, for example, the utility function U that describes preferences over bundles of goods A and B: U(A,B). We can apply any **positive monotonic transformation** to this function (which means, essentially, that we do not change the ordering), and the new function we have created will represent the same preferences. For example, we could multiply a positive constant, α , or add a positive or a negative constant, β . So $\alpha U(A,B) + \beta$ represents exactly the same preferences as U(A,B) because it will order the bundles in exactly the same way. This fact is quite useful because sometimes applying a positive monotonic transformation of a utility function makes it easier to solve problems.

2.2 UTILITY FUNCTIONS AND TYPICAL PREFERENCES

Learning Objective 2.2: Identify utility functions based on the typical preferences they represent.

Consider bundles of apples, A, and bananas, B. A utility function that describes Isaac's preferences for bundles of apples and bananas is the function U(A,B). But what are Isaac's particular preferences for bundles of apples and bananas? Suppose that Isaac has fairly standard preferences for apples and bananas that lead to our typical indifference curves: he prefers more to less, and he likes variety. A utility function that represents these preferences might be

$$U(A,B) = AB$$

If apples and bananas are **perfect complements** in Isaac's preferences, the utility function would look something like this:

$$U(A,B) = MIN[A,B]$$

where the MIN function simply assigns the smaller of the two numbers as the function's value.

If apples and bananas are **perfect substitutes**, the utility function is an additive and would look something like this:

$$U(A,B) = A + B$$

Cobb-Douglas utility functions are commonly used in economics for two reasons:

- 1. They represent **standard preferences**, such as **more is better** and **preference for variety**.
- 2. They are very flexible and can be adjusted to fit real-world data very easily.

Cobb-Douglas utility functions have this form:

$$U(A,B) = A^{lpha} B^{eta}$$

Because positive monotonic transformations represent the same preferences, one such transformation can be used to set $\alpha+\beta=1$, which later we will see is a convenient condition that simplifies some math in the consumer choice problem.

Another way to transform the utility function in a useful way is to take the natural log of the function, which creates a new function that looks like this:

$$U(A,B) = \alpha ln(A) + \beta ln(B)$$

To derive this equation, simply apply the rules of natural logs. It is important to keep in mind the level of abstraction here. We typically cannot make specific utility functions that precisely describe individual preferences. Probably none of us could describe our own preferences with a single equation. But as long as consumers in general have preferences that follow our basic assumptions, we can do a pretty good job finding utility functions that match real-world consumption data. We will see evidence of this later in the course.

Table 2.1 Types of preferences and the utility functions that represent them

| Preferences | Utility function | Type of utility function |
|-----------------------------------|---------------------------------|--------------------------|
| Love of variety or "well behaved" | U(A,B)=AB | Cobb-Douglas |
| Love of variety or "well behaved" | $U(A,B)=A^{lpha}B^{eta}$ | Cobb-Douglas |
| Love of variety or "well behaved" | U(A,B) = lpha ln(A) + eta ln(B) | Natural log Cobb-Douglas |
| Perfect complements | U(A,B)=MIN[A,B] | Min function |
| Perfect substitutes | U(A,B)=A+B | Additive |

2.3 RELATING UTILITY FUNCTIONS AND INDIFFERENCE CURVE MAPS

Learning Objective 2.3: Explain how to derive an indifference curve from a utility function.

Indifference curves and utility functions are directly related. In fact, since indifference curves represent preferences graphically and utility functions represent preferences mathematically, it follows that indifference curves can be derived from utility functions.

In **univariate functions**, the dependent variable is plotted on the vertical axis, and the independent variable is plotted on the horizontal axis, like the graph of y=f(x). In contrast, graphs of **bivariate functions** are three-dimensional, like U=U(A,B). **Figure 2.1** shows a graph of $U=A^{\frac{1}{2}}B^{\frac{1}{2}}$. Three-dimensional graphs are useful for understanding how utility increases with the increased consumption of both A and B.

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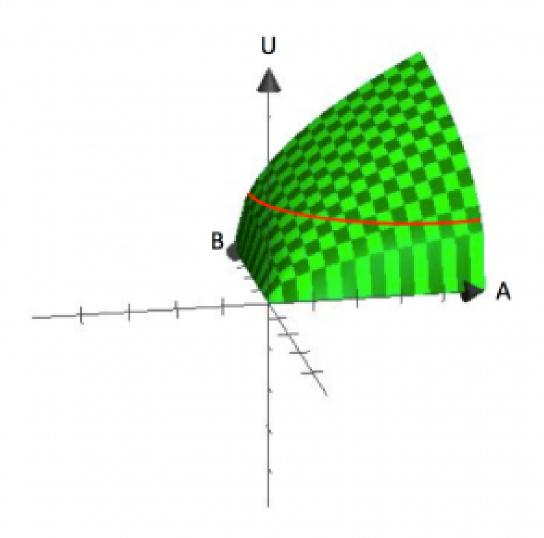


Figure 2.1 [latex]U=A^\frac{1}{2}B^\frac{1}{2}[/latex]

Figure 2.1 clearly shows the assumption that consumers have a preference for variety. Each bundle, which contains a specific amount of A and B, represents a point on the surface. The vertical height of the surface represents the level of utility. By increasing both A and B, a consumer can reach higher points on the surface.

So where do indifference curves come from? Recall that an **indifference curve** is a collection of all bundles that a consumer is indifferent about with respect to which one to consume. Mathematically, this is equivalent to saying all bundles, when put into the utility function, return the same functional value. So if we set a value for utility, $\overline{\mathbb{U}}$, and find all the bundles of A and B that generate that value, we will define an indifference curve. Notice that this is equivalent to finding all the bundles that get the consumer to the same height on the three-dimensional surface in **figure 2.1**.

Indifference curves are a representation of elevation (utility level) on a flat surface. In this way, they are analogous to a **contour line** on a topographical map. By taking the three-dimensional graph back to two-dimensional space—**the A, B space**—we can show the contour lines / indifference curves that represent different elevations or utility levels. From the graph in **figure 2.1**, you can already see how this utility function yields indifference curves that are "bowed-in" or concave to the origin.

So indifference curves follow directly from utility functions and are a useful way to represent utility functions in a two-dimensional graph.

2.4 FINDING MARGINAL UTILITY AND MARGINAL RATE OF SUBSTITUTION

Learning Objective 2.4: Derive marginal utility and MRS for typical utility functions.

Marginal utility [latex](MU)[/latex] is the additional utility a consumer receives from consuming one additional unit of a good. Mathematically, we express this as

$$MU_A = rac{\Delta U}{\Delta A}$$

or the change in utility from a change in the amount of A consumed, where Δ represents a change in the value of the item, so

$$MU_A = rac{\Delta U}{\Delta A} = rac{U(A + \Delta A, B) - U(A, B)}{\Delta A}$$

Note that when we are examining the marginal utility of the consumption of A, we hold B constant. Using calculus, the marginal utility is the same as the partial derivative of the utility function with respect to A:

$$MU_A = rac{\partial U(A,B)}{\partial A}$$

Consider a consumer who sits down to eat a meal of salad and pizza. Suppose that we hold the amount of salad constant—one side salad with a dinner, for example. Now let's increase the slices of pizza; suppose with one slice, utility is ten; with two, it is eighteen; with three, it is twenty-four; and with four, it is twenty-eight. Let's plot these numbers on a graph that has utility on the vertical axis and pizza on the horizontal axis (table 2.2 and figure 2.2).

Table 2.2 Diminishing marginal utility

| Pizza slices | Utility | Marginal utility |
|--------------|---------|------------------|
| 1 | 10 | |
| 2 | 18 | 8 |
| 3 | 24 | 6 |
| 4 | 28 | 4 |

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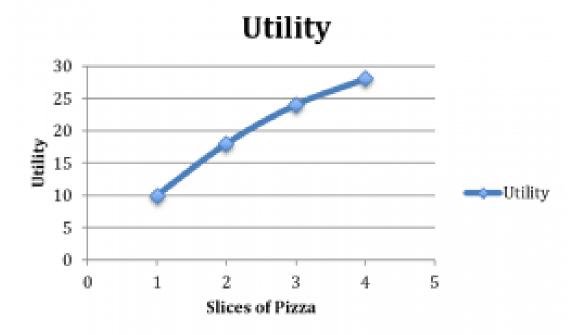


Figure 2.2 Diminishing marginal utility

From the positive slope of the graph, we can see the increase in utility from additional slices of pizza. From the concave shape of the graph, we can see another common phenomenon: the additional utility the consumer receives from each additional slice of pizza decreases with the number of slices consumed.

The fact that the additional utility gets smaller with each additional slice of pizza is called the principle of **diminishing marginal utility**. This principle applies to well-behaved preferences where mixed bundles are preferred.

Marginal rate of substitution (MRS) is the amount of one good a consumer is willing to give up to get one more unit of another good. This is why it is the same thing as the *slope of the indifference curve*—since we keep satisfaction level constant, we stay on the same indifference curve, just moving along it as we trade one good for another. How much of one you are willing to trade for one more of another depends on the marginal utility of each.

Using our previous example, if by consuming one more side salad, your utility goes up by ten, then at a current consumption of four slices of pizza, you could give up two slices of pizza and go from twenty-eight to eighteen utils. Ten more utils from salad and ten fewer utils by giving up two slices of pizza leave overall utility unchanged—so we must still be on the same indifference curve. As you move along the indifference curve, you must be riding the slope—that is, you must be giving up the good on the vertical axis for more of the good on the horizontal axis, which yields a negative rise over a positive run.

We can go directly from marginal utility to MRS by recognizing the connection between the two concepts. In our case, for the utility function U=U(A,B), MRS is represented as

$$MRS = -rac{MU_A}{MU_B}$$

Note that when we substitute, we can simplify the equation:

$$MRS = -rac{MU_A}{MU_B} = -rac{rac{\Delta U}{\Delta A}}{rac{\Delta U}{\Delta B}} = -rac{\Delta B}{\Delta A}$$

Inserting the calculus it equates to

$$MRS = -rac{rac{\partial U(A,B)}{\partial A}}{rac{\partial U(A,B)}{\partial B}}$$

2.5 THE POLICY EXAMPLE

IS A TAX CREDIT ON HYBRID CAR PURCHASES THE GOVERNMENT'S BEST CHOICE TO REDUCE FUEL CONSUMPTION AND CARBON EMISSIONS?

We determined in <u>chapter 1</u> that the relevant consumer decision between more miles driven and other consumption probably conforms to the standard assumptions about consumer choice. Therefore, using the <u>Cobb-Douglas utility function</u> to represent a consumer who likes to drive a car as well as consume other goods and who sees them as a trade-off (money spent on gas is money not spent on other consumer goods) is a good choice. It also has the benefits of both conforming to the assumptions and being flexible:

$$U(MD,C)=MD^aC^eta$$

where MD = miles driven and C= other consumption.

In fact, the function itself can be taken to real-world data, where the parameters can be estimated for this market, the market for miles driven in the consumer's car.

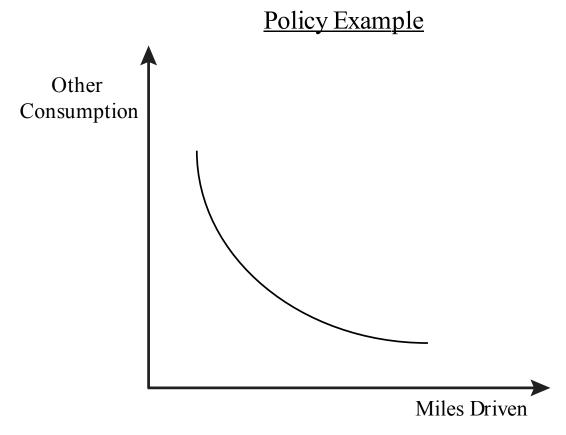


Figure 2.3 Graph of indifference curves for the policy example

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EXPLORING THE POLICY QUESTION

- 1. Would other preference types be more appropriate in this example?
- 2. What would have to be true for perfect complements to be the appropriate preference type to use to analyze this policy?
- 3. What would have to be true for perfect substitutes? Given that we are considering a "typical" consumer who drives, is it appropriate to choose a "typical" utility function?
- 4. Are we just guessing, or do we have some basis in theory to support our choice of "well-behaved" preferences or a Cobb-Douglas utility function?

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

2.1 Utility Functions

<u>Learning Objective 2.1</u>: Describe a utility function.

2.2 Utility Functions and Typical Preferences

Learning Objective 2.2: Identify utility functions based on the typical preferences they represent.

2.3 Relating Utility Functions and Indifference Curve Maps

Learning Objective 2.3: Explain how to derive an indifference curve from a utility function.

2.4 Finding Marginal Utility and Marginal Rate of Substitution

Learning Objective 2.4: Derive marginal utility and MRS for typical utility functions.

2.5 Policy Example

Is a Tax Credit on Hybrid Car Purchases the Government's Best Choice?

Learning Objective 2.5: The Hybrid Tax Credit and customer utility

LEARN: KEY TOPICS

Terms

Utility

The number that a <u>utility function</u> assigns to a specific bundle.

Univariate functions

The dependent variable is plotted on the vertical axis and the independent variable is plotted on the horizontal axis, i.e., the graph of f(x)=mx+b.

Bivariate functions

Functions containing two potentially independent variables. If one variable is influencing another variable, then you will have bivariate data that has an independent and dependent variable.

Useful for understanding how utility increases with the increased consumption of both A and B, i.e., the graph of $U=A^{rac{1}{2}}B^{rac{1}{2}}$.

Ordinal

A function that deals in ranking as opposed to pure quantification; they only indicate which bundle is better, more preferred, etc., but not how much better it is than another bundle. After application of positive monotonic transformation to an ordinal function, meaning the ordering is not changed, the new function will represent the same preferences. If an ordinal function is reported in utils, regardless of the amounts used there is no relationship implied, i.e., bundle A having 10 utils and bundle A having 20 utils does not imply bundle A is two times as preferred as bundle A, only that it is more preferred.

Cardinal

The utility of the product measured with the help of the product's weight, length, temperature, etc.

Util

A unit used to transform the logical utility of a product to empirical. The ordinal utility might say that the consumer prefers the apple to the orange. Cardinal utility might say that the apple provides 80 utils while the orange only provides 40 utils.

Contour line

A way to represent a 3-dimensional topographical map in a two-dimensional space.

Diminishing marginal utility

The additional utility a customer receives from a product diminishes with each additional iteration of the product the customer receives.

Example

Table 2.2 Diminishing marginal utility

| Pizza slices | Utility | Marginal utility |
|--------------|---------|------------------|
| 1 | 10 | |
| 2 | 18 | 8 |
| 3 | 24 | 6 |
| 4 | 28 | 4 |

As a customer consumes more and more slices of pizza, the additional utility having one more slice of pizza provides-satiating excess hunger, producing dopamine from a delicious flavor, etc.-decreases with each additional slice.

Graph

3D utility function and contour line

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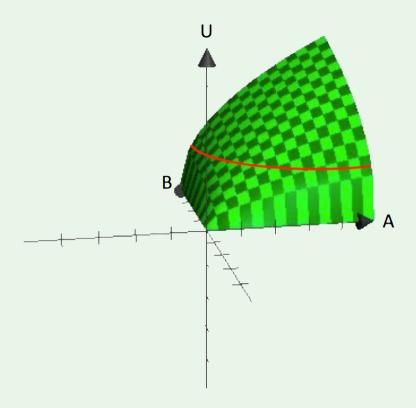


Figure 2.1 A 3D graph showing a graph of [latex]U[/latex] equals [latex]A $^{\frac{1}{2}}$ [/latex] times [latex]B $^{\frac{1}{2}}$ [/latex] to the half power

Equations

Cobb-Douglas utility function

A utility function describing goods which are neither complements nor substitutes.

$$U(A,B)=A^{lpha}B^{eta}$$

Perfect complement utility function

A utility function that describes goods that are perfect complements. See <u>table 2.1</u> for more details.

$$U(A,B) = MIN[A,B]$$

Perfect substitute utility function

A utility function that describes goods that are perfect substitutes. See <u>table 2.1</u> for more details.

$$U(A,B) = A + B$$

Marginal rate of substitution (MRS)

$$MRS = -rac{MU_A}{MU_B}$$

Defined as the amount of one good a consumer is willing to give up to get one more unit of another good.

From MU to MRS

There is a direct connection between marginal utility and the marginal rate of substitution. This connection varies somewhat by utility function. From our basic utility function, $U=U(A,B)\cdot MRS$ is represented as

$$MRS = -rac{MU_A}{MU_B}$$

Substitution results in the following simplification:

$$MRS = -rac{MU_A}{MU_B} = -rac{rac{\Delta U}{\Delta A}}{rac{\Delta U}{\Delta B}} = -rac{\Delta B}{\Delta A}$$

Utilizing calculus:

$$MRS = -rac{rac{\partial U(A,B)}{\partial A}}{rac{\partial U(A,B)}{\partial B}}$$

Marginal utility (MU)

$$MU_a = rac{\Delta U}{\Delta A}$$

The additional utility a consumer receives from consuming one additional unit of a good.

Utility function

Functions that rank bundles of consumption goods by assigning a number to each, where larger numbers indicate preferred bundles.

Table Summarizing Utility Functions

Table 2.1 Types of preferences and the utility functions that represent them

| Preferences | Utility function | Type of utility function |
|-----------------------------------|---------------------------------|--------------------------|
| Love of variety or "well behaved" | U(A,B)=AB | Cobb-Douglas |
| Love of variety or "well behaved" | $U(A,B)=A^{lpha}B^{eta}$ | Cobb-Douglas |
| Love of variety or "well behaved" | U(A,B) = lpha ln(A) + eta ln(B) | Natural log Cobb-Douglas |
| Perfect complements | U(A,B)=MIN[A,B] | Min function |
| Perfect substitutes | U(A,B)=A+B | Additive |

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CHAPTER 3

Budget Constraints

THE POLICY QUESTION

HYBRID CAR PURCHASE TAX CREDIT—IS IT THE GOVERNMENT'S BEST CHOICE TO REDUCE FUEL CONSUMPTION AND CARBON EMISSIONS?

The US government policy of extending tax credits toward the purchase of electric and hybrid cars can have consequences beyond decreasing carbon emissions. For instance, a consumer that purchases a hybrid car could spend less money on gas and have more money to spend on other things. This has implications for both the individual consumer and the larger economy.

Even the richest people—from Bill Gates to Oprah Winfrey—can't afford to own everything in the world. Each of us has a budget that limits the extent of our consumption. Economists call this limit a *budget constraint*. In our policy example, an individual's choice between consuming gasoline and everything else is constrained by their current income. Any additional money spent on gasoline is money that is not available for other goods and services and vice versa. This is why the budget constraint is called a constraint.

The budget constraint is governed by income on the one hand—how much money a consumer has available to spend on consumption—and the prices of the goods the consumer purchases on the other.

EXPLORING THE POLICY QUESTION

1. What are some of the budget implications for a consumer who owns a hybrid car? What purchase decisions might this consumer make given their savings on gas, and how does this, in turn, affect the goals of the tax subsidy policy?

LEARNING OBJECTIVES

3.1 Description of the Budget Constraint

<u>Learning Objective 3.1</u>: Define a budget constraint conceptually, mathematically, and graphically.

3.2 The Slope of the Budget Line

Learning Objective 3.2: Interpret the slope of the budget line.

3.3 Changes in Prices and Income

Learning Objective 3.3: Illustrate how changes in prices and income alter the budget constraint and budget line.

3.4 Coupons, Vouchers, and Taxes

Learning Objective 3.4: Illustrate how coupons, vouchers, and taxes alter the budget constraint and budget line.

3.5 Policy Example

Hybrid Car Purchase Tax Credit—Is It the Government's Best Choice to Reduce Fuel Consumption and Carbon Emissions?

Learning Objective 3.5: The Hybrid Car Tax Credit and Consumers' Budgets

3.1 DESCRIPTION OF THE BUDGET CONSTRAINT

Learning Objective 3.1: Define a budget constraint conceptually, mathematically, and graphically.

The **budget constraint** is the set of all the bundles a consumer can afford given that consumer's income. We assume that the consumer has a budget—an amount of money available to spend on bundles. For now, we do not worry about where this money or income comes from; we just assume a consumer has a budget.

So what can a consumer afford? Answering this depends on the prices of the goods in question. Suppose you go to the campus store to purchase energy bars and vitamin water. If you have \$5 to spend, energy bars cost fifty cents each, and vitamin water costs \$1 a bottle, then you could buy ten bars and no vitamin water, no bars and five bottles of vitamin water, four bars and two vitamin waters, and so on.

This table shows the possible combinations of energy bars and vitamin water the student can buy for exactly \$5:

 Table 3.1 Combinations of energy bars and vitamin water

| Number of Energy bars | Bottles of vitamin water |
|-----------------------|--------------------------|
| 10 | 0 |
| 8 | 1 |
| 6 | 2 |
| 4 | 3 |
| 2 | 4 |
| 0 | 5 |

It is also true that you could spend less than \$5 and have money left over. So we have to consider all possible bundles—including consuming none at all.

Note that we are focusing on bundles of two goods so that we maintain tractability (as explained in <u>chapter 1</u>), but it is simple to think beyond two goods by defining one of the goods as "money spent on everything else."

Mathematically, the total amount the consumer spends on two goods, A and B, is

$$P_AA + P_BB$$
(3.1)

where P_A is the price of good A and P_B is the price of good B. If the money the consumer has to spend on the two goods, their income, is given as I, then the budget constraint is

$$P_AA + P_BB \leq I$$
(3.2)

Note the inequality: this equation states that the consumer cannot spend more than their income but can spend less. We can simplify this assumption by restricting the consumer from spending all of their income on the two goods. This will allow us to focus on the frontier of the budget constraint. As we shall see in chapter 4, this assumption is consistent with the *more-is-better* assumption—if you can consume more (if your income allows it), you should because you will make yourself better off. With this assumption in place, we can write the budget constraint as

$$P_AA + P_BB = I$$
(3.3)

Graphically, we can represent this budget constraint as in **figure 3.1**. We call this the **budget line**: the line that indicates the possible bundles the consumer can buy when spending all their income.

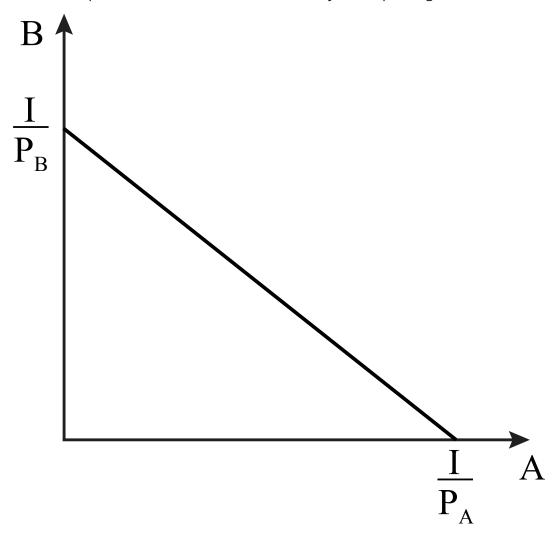


Figure 3.1 The budget line—graph of budget constraint (equation 3.3)

3.2 THE SLOPE OF THE BUDGET LINE

Learning Objective 3.2: Interpret the slope of the budget line.

From the graph of the budget constraint in <u>section 3.1</u>, we can see that the budget line slopes downward and has a constant slope along its entire length. This makes intuitive sense: if you buy more of one good, you are going to have to buy less of the other good. The rate at which you can trade one for the other is determined by the prices of the two goods, and they don't change.

We can see these details in **figure 3.2**.

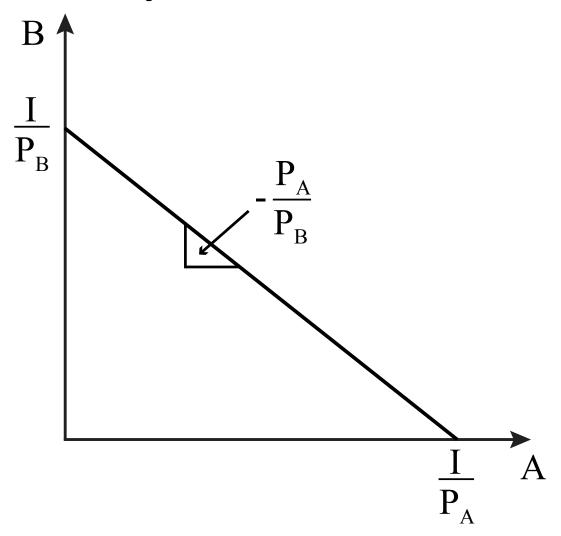


Figure 3.2 Intercepts and slope for the budget line

We can find the slope of the budget line easily by rearranging **equation 3.3** so that we isolate B on one side. Note that in our graph, B is the good on the vertical axis, so we will rearrange our equation to look like a standard function, with B as the dependent variable:

$$B = \frac{I}{P_B} - \frac{P_A}{P_B} A \tag{3.4}$$

Now we have our budget line represented in point-slope form, where the first part, $\dfrac{I}{P_B}$, is the vertical

intercept, and the second part, $-\frac{P_A}{P_B}$, is the slope coefficient on A.

Note that the slope of the budget line is simply the ratio of the prices, also known as the **price ratio**. This is the rate at which you can trade one good for the other in the marketplace. To see this, let's return to the campus store with \$5 to spend on energy bars and vitamin water.

Suppose you originally decided to buy five bottles of vitamin water and placed them in a basket. After some thought, you decided to trade one bottle for two energy bars. Now you have four bottles of vitamin

water and two energy bars in the basket. If you want even more bars, the same trade-off is available: two more bars can be had if you give up one bottle of vitamin water and so on.

The slope of the budget line is also called the **economic rate of substitution [latex](ERS)[/latex]**.

The slope of the budget line also represents the **opportunity cost** of consuming more of good A because it describes how much of good B the consumer has to give up to consume one more unit of good A. The opportunity cost of something is the value of the next best alternative given up in order to get it. For example, if you decide to buy one more bottle of vitamin water, you have to give up two energy bars. Note that opportunity cost is not limited to the consumption of material goods. For example, the opportunity cost of an hour-long nap might be the hour of studying microeconomics that did not happen because of it.

3.3 CHANGES IN PRICES AND INCOME

Learning Objective 3.3: Illustrate how changes in prices and income alter the budget constraint and budget line.

From our mathematical description of the budget line, we can easily see how changes in prices and income affect the budget line and a consumer's choice set—the set of all the bundles available to them at current prices and income. Let's go back to **equation 3.3**:

$$P_AA + P_BB = I$$

We know from the previous figure that the vertical intercept for **equation 3.3** is $\frac{I}{P_B}$ and the horizon-

tal intercept is
$$\dfrac{I}{P_A}$$
 .

Now consider an increase in the price of good A. Notice that this increase does not affect the vertical intercept, only the horizontal intercept. As P_A increases, $\frac{I}{P_A}$ decreases, moving closer to the origin.

This change makes the budget line "steeper" or more negatively sloped, as we can see from the slope coefficient: $-\frac{P_A}{P_B}$. As P_A increases, this ratio increases in absolute value, so the slope becomes more

negative or steeper. What this means intuitively is that the trade-off or opportunity cost has risen. Now the consumer has to give up more of good B to consume one more unit of good A.

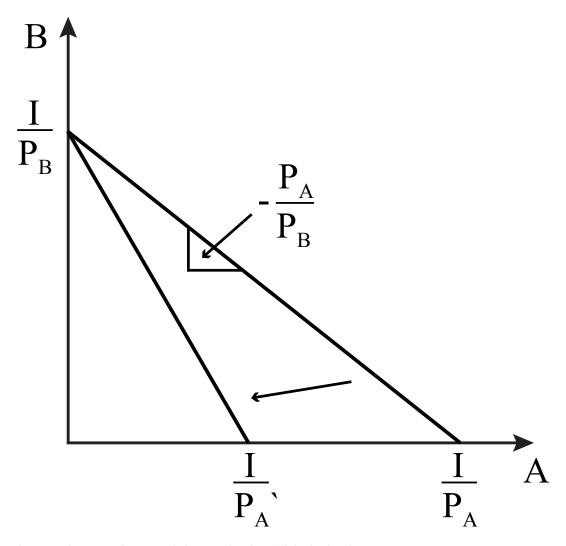


Figure 3.3 Changing the price of one good changes the slope of the budget line.

Next, consider a change in income. Suppose the consumer gets an additional amount of money to spend, so I increases. I affects both intercept terms positively, so as I increases, both $\frac{I}{P_B}$ and $\frac{I}{P_A}$ increase or move away from the origin. But I does not affect the slope: $-\frac{P_A}{P_B}$. Thus the shift in the budget line is a parallel shift outward—the consumer with the additional income can afford more of both (as displayed in **figure 3.4**).

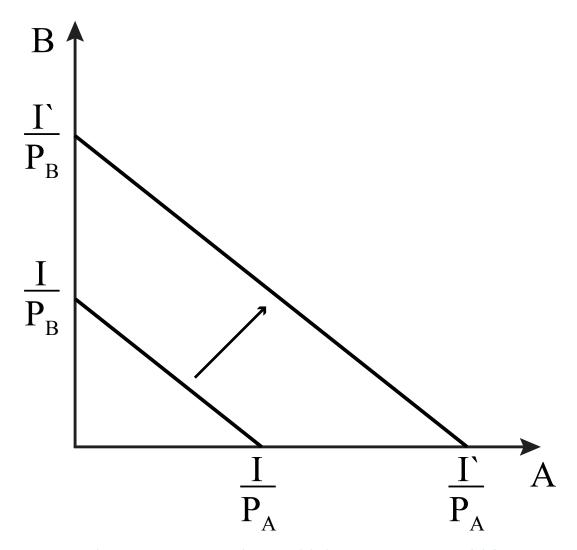


Figure 3.4 A customer with more resources can spend more, and the line experiences an outward shift.

3.4 COUPONS, VOUCHERS, AND TAXES

Learning Objective 3.4: Illustrate how coupons, vouchers, and taxes alter the budget constraint and budget line.

Budget constraints can change due to changes in prices and income, but let's now consider other common features of the real-world market that can affect the budget constraint. We start with coupons or other methods firms use to give discounts to consumers.

Consider a coupon or a sale that gives consumers a discount on the price of one item in our budget constraint problem. A coupon that entitles the bearer to a percentage off in price is essentially a reduction in price and has precisely the same effect. For example, a 20 percent off coupon on a good that normally costs \$10 is the same as reducing the price to \$8.

More complicated is a coupon that gives a percentage off the entire purchase. In this case, the percentage is taken from the price of both items A and B in our budget constraint problem. In this case, the price ratio, or the slope of the budget constraint, does not change.

For example, if the price of A is regularly \$10 and the price of B is regularly \$20, then with 20 percent off the entire purchase, the new prices are \$8 and \$16, respectively. Intuitively, we can see that this is

equivalent to increasing the income and achieves the same result: by expanding the budget set, the consumer can now afford bundles with more of both goods.

Table 3.2 The effect of a 20 percent discount on price

| Product | Regular price (\$) | New price with 20 percent discount on entire purchase (\$) |
|---------|--------------------|--|
| Good A | 10 | 8 |
| Good B | 20 | 16 |

Another common discount is on a maximum number of items. For example, you might see an advertisement for 20 percent off up to three units of good A. This discount lowers the opportunity cost of A in terms of B for the first three units but reverts back to the original opportunity cost thereafter. **Figure 3.5** illustrates this.

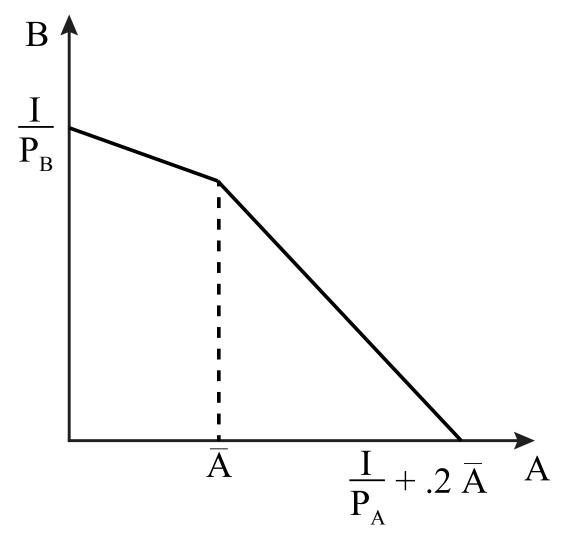


Figure 3.5 Effect of a 20 percent discount on the first Ā units of A

Taxes have the same effects as coupons but in the opposite direction. An **ad valorem tax** is a tax based on the value of a good, such as a percentage sales tax. In terms of the budget constraint, an ad valorem tax on a specific good is equivalent to an increase in price, as shown in **figure 3.6**. A general sales tax on all goods has the effect of a parallel shift of the budget line inward. Note also that income taxes are, in

this case, functionally equivalent to a general sales tax; they cause a parallel shift inward of the budget line.

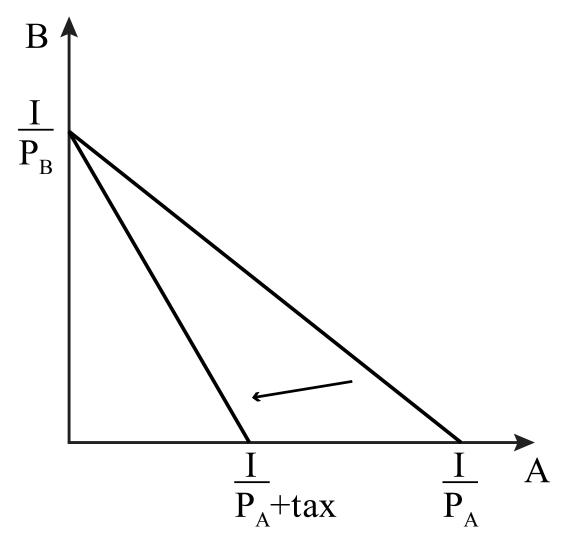


Figure 3.6 An ad valorem tax changes the slope and horizontal intercept of the budget line.

Vouchers that entitle the bearer to a certain quantity of a good (either value or quantity) are slightly more complicated. Let's return to your purchase of vitamin water and energy bars. Suppose you have a voucher for two free energy bars.

You have \$5.

The price of one energy bar is \$0.50.

The price of one bottle of vitamin water is \$1.

How would we now draw your budget line?

One place to start is to consider the simple bundle that contains 2 energy bars and two bottles of vitamin water. Note that giving up one or two bars does not allow the student to consume any more vitamin water. The opportunity cost of these two bars is 0, and so the budget line in this part has a zero slope. After using the voucher, if the student wants more than two bars, the opportunity cost is the same as before—0.5 bottles of vitamin water for an energy bar—and so the budget line from this point on is the same as before. The new budget line with the voucher has a kink.

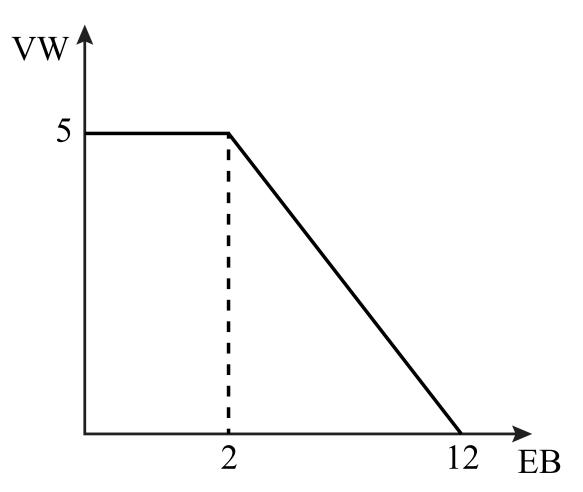


Figure 3.7 The "kink" in the new budget line

3.5 THE POLICY EXAMPLE

HYBRID CAR PURCHASE TAX CREDIT—IS IT THE GOVERNMENT'S BEST CHOICE TO REDUCE FUEL CONSUMPTION AND CARBON EMISSIONS?

Learning Objective 3.5: The Hybrid Car Tax Credit and Consumers' Budgets

For several chapters, we have considered the policy of a hybrid car tax credit. In <u>chapter 1</u>, we thought about the various driving preferences of a typical consumer. In <u>chapter 2</u>, we translated these preferences into a <u>type of utility function</u> and <u>corresponding indifference curve</u>. Now let's think about the appropriate budget line for our policy example.

To start, let's use the same two axes as we used for the indifference curve map as shown in **figure 3.8**. In other words, let's place "miles driven" on the horizontal axis and "\$," which is all the money spent on other consumption, on the vertical axis. For now, we won't specify the precise level of income.

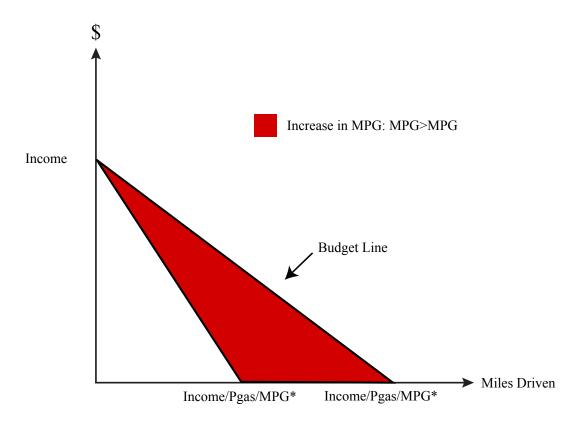


Figure 3.8 A consumer's budget constraint for the hybrid car policy

Now we can ask, "What is the price of 'other consumption'?" Since we are talking about money left over after paying for miles driven, the price for other consumption is simply one. This is because we are talking about money itself, and the price of a dollar is a dollar. So the intercept on this axis is simply the value of I.

But what is the price of a mile driven? This question is more complicated and includes the cost of maintenance and depreciation. However, because we are focused on the effect of increasing the miles per gallon of gas, let's concentrate on only the cost as it relates to the purchase of gasoline. In this case, the cost of driving a mile is the price of gasoline divided by the car's miles per gallon (MPG). Since we are again interested not in an individual but in a group, we can use the average price of a gallon of regular gas divided by the average MPG of cars driven in the United States as a reasonable approximation of the cost of a mile driven in a non-hybrid car. Now we have the "price" of driving a mile; dividing income by this price gives us the intercept on the "miles driven" axis.

Now that we have a budget constraint for our electric and hybrid car subsidy policy example, we can see the effect of the policy on the constraint. Doubling the MPG from twenty to forty dramatically reduces the price of driving a mile. This reduction causes the "miles driven" intercept to move upward and the entire budget constraint to move outward. Note that now the typical consumer can afford to consume bundles with more of both miles driven and everything else—bundles that were unavailable to them prior to the policy.

Equation 3.4 summarizes the budget constraint for miles driven and other goods.

Income = $(P_{MilesDriven})$ (Miles Driven) + Dollars Spent on Other Consumption

EXPLORING THE POLICY QUESTION

1. What can we say about the availability of bundles after the hybrid car tax credit is enacted compared to before? Do the bundles represent more consumption of only miles driven, or do they represent more of other goods as well?

- 2. Another type of car that is high mileage (high MPG) is a diesel car. In the United States, however, the price of diesel gas is typically higher than the price of regular gas. How would only higher MPG shift the budget line in <u>figure 3.8</u>? How would only higher-priced gas shift the budget line in <u>figure 3.8</u>? How would these two factors together alter the budget line from <u>figure 3.8</u>?
- 3. If the government subsidizes the purchase of hybrid cars through a rebate that adds to the income of consumers, what happens to the budget line in figure 3.8?

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

3.1 Description of the Budget Constraint

Learning Objective 3.1: Define a budget constraint conceptually, mathematically, and graphically.

3.2 The Slope of the Budget Line

<u>Learning Objective 3.2</u>: Interpret the slope of the budget line.

3.3 Changes in Prices and Income

Learning Objective 3.3: Illustrate how changes in prices and income alter the budget constraint and budget line.

3.4 Coupons, Vouchers, and Taxes

Learning Objective 3.4: Illustrate how coupons, vouchers, and taxes alter the budget constraint and budget line.

3.5 Policy Example

Hybrid Car Purchase Tax Credit—Is It the Government's Best Choice to Reduce Fuel Consumption and Carbon Emissions?

<u>Learning Objective 3.5</u>: The Hybrid Car Tax Credit and Consumers' Budgets

LEARN: KEY TOPICS

Terms

Ad valorem tax

A tax based on the value of a good, such as a percentage sales tax. In terms of the budget constraint, an ad valorem tax on a specific good is equivalent to an increase in price.

Budget constraint

The limit of which a consumer has capital to purchase goods. The budget constraint is governed by income on the one hand—how much money a consumer has available to spend on consumption—and the prices of the goods the consumer purchases on the other.

Budget line

The line that indicates the possible bundles the consumer can buy when spending all their income.

Economic rate of substitution (ERS)

The slope of the budget line. The slope of the budget line also represents the **opportunity cost** of consuming more of good A because it describes how much of good B the consumer has to give up to consume one more unit of good A.

Opportunity cost

The value of the next best alternative given up in order to get it.

i.e., you have \$3. Vitamin water is \$1 and energy bars are \$.50. You have already bought a bottle of vitamin water. If you decide to buy one more bottle of vitamin water, the **opportunity cost** is that you have to give up two energy bars.

Graphs

Normal budget constraint

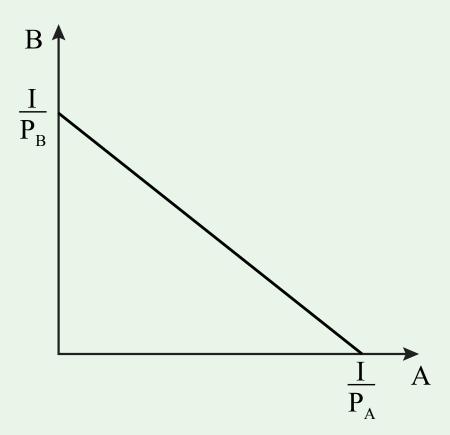
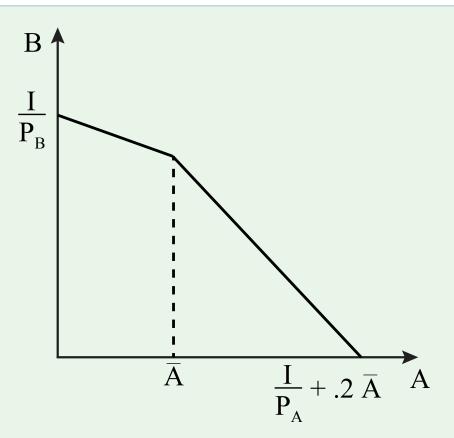


Figure 3.1 The budget line—graph of budget constraint

Budget constraint with coupon



Budget constraint with coupon

Budget constraint with voucher

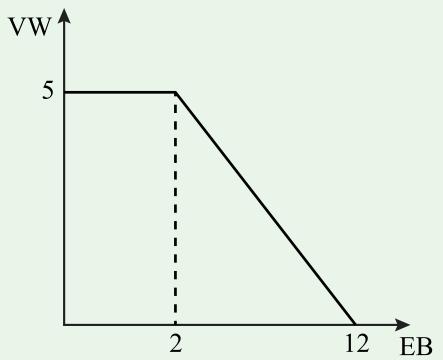


Figure 3.7 The "kink" in the new budget line

Equations

Budget constraint

$$P_A A + P_B B = I$$

Graphically produces a line that indicates the possible bundles the consumer can buy when spending all their income.

$$P_AA + P_BB$$

The total amount a consumer spends on two goods, A and B.

$$P_A A + P_B B \leq I$$

An inequality that states that the consumer cannot spend more than their income but can spend less.

$$B = \frac{I}{P_B} - \frac{P_A}{P_B} A$$

The budget line represented in **point-slope form** form, where the first part, $\frac{I}{P_B}$, is the vertical intercept, and the second part, $-\frac{P_A}{P_B}$, is the

slope coefficient on A. The slope of this equation is the Economic Rate of Substitution [latex](ERS)[/latex].

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CHAPTER 4

Consumer Choice



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THE POLICY QUESTION

HYBRID CAR PURCHASE TAX CREDIT—IS IT THE BEST CHOICE TO REDUCE FUEL CONSUMPTION AND CARBON EMISSIONS?

The US government offered a tax credit toward the purchase of hybrid cars with the goal of reducing the output of carbon emissions produced by cars annually. We are using the tools of microeconomic consumer theory to study this policy and assess its effectiveness in reducing emissions.

We are now very close to being able to predict how consumers will change their driving and gasoline purchases in response to a government tax credit on hybrid cars. As we will see, this is simply a specific example of the general question we first raised in chapter 1 of how to predict consumer behavior when prices or incomes change. For our policy example and in general, we address this question by combining the budget constraint with the concept of preferences and utility maximization. Consumer theory in economics is based on the premise that each person will try to do their best given the money they have and

the prices of the goods and services they like. This is what we mean by utility maximization—choosing the affordable bundle of goods and services that returns the highest utility.

Think about a consumer who goes grocery shopping. There are many ways to fill a shopping basket—ending up with many different possible bundles of goods. This chapter is concerned with how each consumer picks the best affordable good. As we will see shortly, consumers think about the income they have and the relative prices of all the possible goods they could buy and then choose among all the possible bundle combinations that their budget can support.

EXPLORING THE POLICY QUESTION

1. What is your prediction about how consumers' driving and gasoline-purchasing behavior will change when their income increases or decreases? When the price of gasoline increases or decreases? What implications will these behavior changes have for the hybrid car tax credit policy?

LEARNING OBJECTIVES

4.1 The Consumer Choice Problem: Maximizing Utility

<u>Learning Objective 4.1</u>: Define the consumer choice problem.

4.2 Solving the Consumer Choice Problem

Learning Objective 4.2: Solve a consumer choice problem with the typical utility function.

4.3 Corner Solutions and Kinked Indifference Curves

Learning Objective 4.3: Solve a consumer choice problem with utility functions for perfect complements and perfect substitutes.

4.4 Policy Example

Hybrid Car Purchase Tax Credit—Is It the Best Choice to Reduce Fuel Consumption and Carbon Emissions?

Learning Objective 4.4: The Hybrid Car Tax Credit and Consumers' Budgets

4.1 THE CONSUMER CHOICE PROBLEM: MAXIMIZING UTILITY

Learning Objective 4.1: Define the consumer choice problem.

What is the consumer's optimal choice among competing bundles? This question summarizes the **consumer choice problem**. To resolve this problem, we can combine our understanding of the budget constraint and preferences as represented by utility functions. The budget constraint describes all the bundles the consumer could possibly choose. The utility function describes the consumer's preferences and relative level of satisfaction from the consumption of bundles. We put these two pieces together by answering the question, "Among all the bundles the consumer could possibly choose, which one returns the highest level of utility?"

Conceptually, we are overlaying the indifference curve map on the budget constraint and looking for the point or points of intersection, as in **figure 4.1.1.** Recall that there can be more than one indifference curve for bundles of goods A and B. The goal of solving the consumer choice problem is to get on the highest indifference curve—the curve that is the farthest to the upper right—while also satisfying the budget constraint. The highest indifference curve—the one that represents the highest level of utility or satisfaction—is the one that just touches the budget line at a single point. It is not possible to get on a higher indifference curve given the budget constraint, and though it is possible to get on a lower one, doing so necessarily means a lower level of utility or satisfaction.

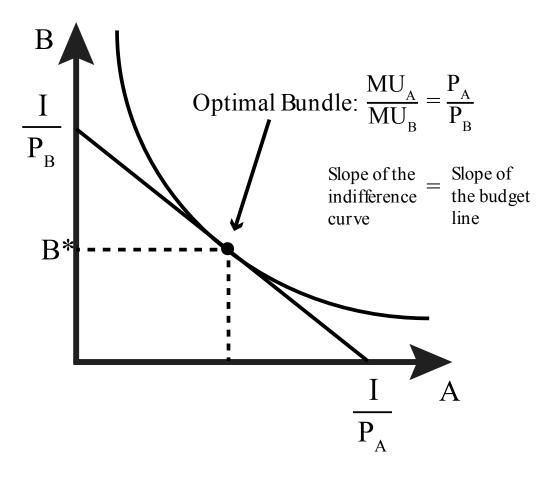


Figure 4.1 Indifference curve on the budget constraint

Figure 4.1 summarizes the solution to the consumer choice problem: The consumer should pick the one bundle that returns the highest level of utility while also satisfying the budget constraint. This graph also shows us the two fundamental conditions that represent the solution to the consumer choice problem:

- 1. The consumer's optimal choice is on the budget line itself, *not* inside the budget constraint. This is why we can focus on the line rather than the whole set of affordable bundles.
- 2. At the optimal choice, the indifference curve just touches the budget line, and so at this one point, they have exactly the same slope.

This second condition has a significant intuitive interpretation. Recall that the slope of the indifference curve is the **marginal rate of substitution** ([latex]MRS[/latex])—the rate at which the consumer is willing to trade off one good for the other and remain just as well off. Recall also that the slope of the budget

line is the **economic rate of substitution ([latex]ERS[/latex])**—the rate at which the consumer is able to trade one good for the other at current prices. What **figure 4.1** shows is that at the optimal choice, these two things *must be equal*. But why?

Consider a point, like point 1 in figure **4.2**, where the indifference curve intersects the budget line. Here, the MRS is greater than the ERS absolute value. The MRS tells us the amount of good B the consumer is willing to give up to get one more unit of good A and remain just as satisfied. In this case, the ERS tells us how much of B a consumer must give up in exchange for one unit of A in the marketplace. Here, the consumer is willing to give up a lot of B to get a little more A and remain just as satisfied, but the ERS indicates that the consumer does not have to give up that much of B to get the same amount of A. So it *must* be the case that if the consumer trades some of B for A in the market, they will be better off. In other words, a consumer who moves down along the budget line will be on a higher indifference curve.

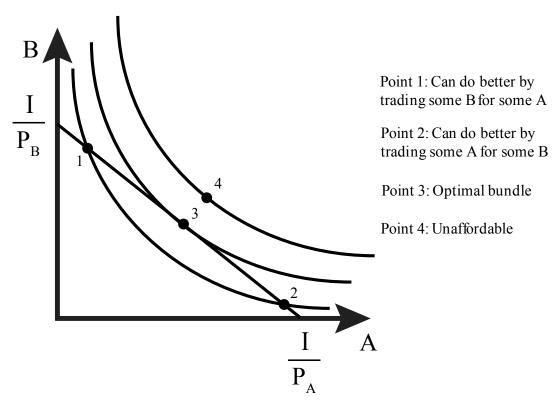


Figure 4.2 Budget line with three indifference curves

So the graph of the budget line and indifference curves illustrates the two conditions that define the consumer's optimal choice:

[latex]P_{A}A+P_{B}B=I[/latex]

and

$$MRS = ERS : \frac{MU_A}{MU_B} = \frac{P_A}{P_B}$$

Note that the negative signs cancel.

With these two conditions, we can solve the consumer choice problem mathematically.

Note that the MRS=ERS condition can be rearranged to $\dfrac{MU_A}{P_A}.$

Economists sometimes call this **the "equal bang for the buck" condition** because the equation indicates that at the optimal choice, the consumer must be getting exactly the same marginal utility per dollar from the consumption of goods A and B. Why? Think of a case where these two goods are not equal. If you're at a pizza parlor eating slices of pizza and bowls of salad, suppose that

$$rac{MU_{Pizza}}{P_{Pizza}} < rac{MU_{Salad}}{P_{Salad}}$$

This equation indicates that the marginal utility per dollar of pizza is less than the marginal utility per dollar of salad at your current level of consumption. You cannot optimize your utility. Why not?

For simplicity, let's assume the price of both a slice of pizza and a small salad is exactly \$1, so

$$MU_{Pizza} < MU_{Salad}$$

Now let's take \$1 away from pizza and spend it instead on salad. You lose the marginal utility of that last slice of pizza, but you gain the marginal utility of one more serving of salad. From the condition above, we know that total utility must have increased, since

$$MU_{Pizza} < MU_{Salad}$$

We also know that the marginal utility for a normal preference diminishes when you consume more of a good and therefore increases when you consume less. Therefore, the marginal utility of pizza will increase, and the marginal utility of salad will decrease, getting you closer to equality. As long as this condition is not met (as long as there is an inequality), a consumer can always make these types of trades to become better off.

4.2 SOLVING THE CONSUMER CHOICE PROBLEM

Learning Objective 4.2: Solve a consumer choice problem with the typical utility function.

Formally, the consumer's optimal choice problem looks like this:

$$max\,U(A,B)$$
 (4.1) subject to $P_AA+P_BB \leq I$

As we discussed in section 4.1, the second line of this problem (the "subject to" part) is the budget constraint. Since we have the more-is-better assumption, the consumer will always spend all of their budget on goods A and B. So we can rewrite the consumer choice problem as

$$max\,U(A,B)$$
 (4.2) $(A,B)+P_BB=I$

Let's use the Cobb-Douglas utility function and solve this problem analytically. Our problem is now

$$\max A^{lpha}B^{eta}$$
 (4.3) subject to $P_AA+P_BB=I$

To solve this problem, we will apply what we know from section 4.1: at the optimal solution, we have two conditions, MRS = ERS, and we are on the budget line.

MRS=ERS in this case requires that we find the marginal utility of bundles A and B. This requires determining the partial derivative of the utility function for good A and then for good B.

$$egin{align} MU_A &= rac{\partial (A^lpha B^eta)}{\partial A} = \partial A^{(a-1)} B^eta \ MU_B &= rac{\partial (A^lpha B^eta)}{\partial B} = eta A^lpha B^{(eta-1)} \ \end{split}$$

The MRS is the ratio of the two marginal utilities:

$$MRS=-rac{MU_A}{MU_B}=-rac{rac{\partial (A^lpha B)}{\partial A}}{rac{\partial (A^lpha B^eta)}{\partial B}}=rac{\partial A^{(a-1)}B^eta}{eta A^aB^{(eta-1)}}=-rac{lpha B}{eta A}$$
(4.4)

The ERS is the ratio of the prices:

$$MRT = -rac{P_A}{P_B}$$
 (4.5)

Putting these two equations together gives us

$$MRS = MRT \Rightarrow -rac{lpha B}{eta A} = -rac{P_A}{P_B} \Rightarrow rac{lpha}{eta} rac{B}{A} = rac{P_A}{P_B}$$
 (4.6)

The second part of the consumer choice problem, the budget constraint, as we are on the budget line or the "subject to" part, is straightforward:

$$P_A A + P_B B = I(4.7)$$

At this point, solving the problem is a matter of simple algebra. We have two equations with two unknowns, good A and good B. We can solve these equations by repeated substitution: solve **equation 4.4** for good A or B, and substitute the result into **Equation 4.5**. If we solve **equation 4.4** for bundle B, we get

$$B = \frac{\beta}{\alpha} \frac{P_A}{P_B} A$$

Substituting into equation 4.5 gives us

$$P_AA + P_B\left(rac{eta}{lpha}rac{P_A}{P_B}A
ight) = I$$
(4.8)

Simplifying this equation gives us

$$\frac{(\alpha+eta)}{lpha}P_AA=I$$

Solving for A, we get

$$A=rac{I}{P_{A}}rac{lpha}{\left(lpha+eta
ight)}$$
(4.9)

Plugging this equation into equation 4.6 gives us

$$A = rac{I}{P_B} rac{eta}{(lpha + eta)}$$

Simplifying this equation gives us the solution for good B:

$$B=rac{I}{P_B}rac{eta}{(lpha+eta)}$$
(4.10)

Remember that the prices, the income, and the parameter values for α and β are all just numbers that are given. Therefore, these solutions for goods A and B are simply a specific amount of

both—one specific bundle of A and B consumption that is the very best choice a consumer has among all the possible choices.

Equations **4.9** and **4.10**) are the demand functions for goods A and B, respectively. **Demand functions** are mathematical functions that describe the relationship between quantity demanded and prices, income, and other things that affect purchase decisions. We can use these demand functions to predict what will happen to the consumption of both goods when prices and incomes change. From the demand functions, it is easy to predict that increases in the price of the good will lead to lower consumption and increases in income will lead to greater consumption. We will return to the examination of these demand functions in the next chapter.

4.3 CORNER SOLUTIONS AND KINKED INDIFFERENCE CURVES

Learning Objective 4.3: Solve a consumer choice problem with utility function for perfect complements and perfect substitutes.

So far, we have considered the optimal consumption bundle for a consumer who has "well-behaved" preferences, meaning that they have indifference curves that are smooth, curved in, and not touching the vertical or horizontal axes. The optimal choice for these well-behaved preferences is characterized by the MRS=ERS. The solution to the consumer choice problem with these preferences is always an **interior solution**: a utility maximizing bundle that has a positive amount of both goods.

But we know that there are other relatively common preference types—such as **perfect complements** and **perfect substitutes**—that have **indifference curves** that are shaped differently. The solution to the consumer choice problem for these preference types cannot be characterized by the MRS=ERS condition.

As we saw in <u>chapter 1</u>, perfect complements have indifference curves that are kinked at ninety-degree angles, and perfect substitutes have indifference curves that are straight lines that begin and end on the axes. For both perfect complements and perfect substitutes, the solution to the consumer choice problem is the one consumption bundle that puts the consumer on the highest indifference curve possible. But in both cases, this does not have the tangency condition of the MRS equaling the ERS.

Since perfect complements have indifference curves that are **kinked**, they have abrupt changes in slope at a single point. At this kink, the MRS is not defined because there is no slope. The solution to the consumer choice problem with perfect complement preferences is interior—you definitely need some of both goods to get any utility—but at the kink, there is no MRS to equate to ERS.

The solutions to consumer choice problems with perfect complement preferences are usually **corner solutions**: a utility maximizing bundle that consists of only one of the two goods—in other words, a consumption bundle that is located at one corner of the budget constraint. Corner solutions are typical when preferences are perfect substitutes but can occur for many other preference types that we will not study. Let's see how to find the utility maximizing bundle for these two preference types, starting with perfect complements.

Perfect Complements

In the case of perfect complements with strictly positive prices, the optimal bundle is always the one at the ninety-degree kink in the indifference curve, as shown in **figure 4.3**. We can use this observation similarly to how we used the fact that MRS = ERS in the previous section. If the optimal bundle is

always at the kink and is always on the budget line, we can once again find two equations with two unknowns to solve.

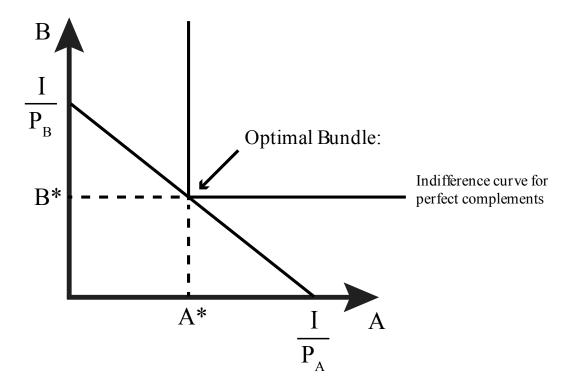


Figure 4.3 Solution to the consumer choice problem for perfect complements

Recall that the utility function for perfect complements looks like this:

$$U(A,B) = min[\alpha A, \beta B]$$

A **parable** is a fixed value given outside the model, one that never changes. A **variable** is a value that can change, such as prices, income, and so on.

Consuming at the **kink** implies that $\alpha A=\beta B$. This condition makes intuitive sense: since the utility function takes on only the value of the smaller of the two choices, spending money on some of good A without the corresponding increase in good B will not raise utility at all but will cost the consumer money. So this choice cannot possibly be optimal. The only optimal decision is to spend money on goods A and B in the precise proportions that they are consumed. With the condition $\alpha A=\beta B$ and the budget constraint $P_AA+P_BB=I$, we can easily solve through repeated substitution. Note

that $A=rac{eta}{lpha}B$ substitutes into the budget constraint as follows:

$$P_A rac{eta}{lpha} B + P_B B = I$$

Solving for $oldsymbol{B}$ gives us

$$B=rac{I}{P_{A}rac{eta}{lpha}+P_{B}}$$
 , or $B=rac{lpha I}{eta P_{A}+lpha P_{B}}$

Solving for
$$A$$
 using $A=rac{eta}{lpha}B$ gives us

$$A=rac{eta}{lpha}[rac{lpha I}{eta P_A+lpha P_B}]=rac{eta I}{eta P_A+lpha P_B}$$

Again, we see that the quantity demanded of each item decreases with an increase in its price and increases with increases in income. But now we also have the interesting result that the quantity demanded of one good decreases as the price of the *other* good increases. This makes intuitive sense because perfect complements are goods that are only consumed together, such as hot dogs and hot dog buns.

Perfect Substitutes

With perfect substitutes, the optimal bundle is generally at either one corner of the budget constraint or the other. If you stop and think about it for a moment, the intuition behind this observation becomes clear. If you like Coke and Pepsi equally well and think of them as perfect substitutes for one another, you will logically buy only the one that has the lower price. If Coke costs \$1 and Pepsi \$1.50, and you like them equally well, why would you ever buy any Pepsi at all? There is one exception to this all-of-one-or-the-other rule. When Coke and Pepsi have the same prices, you can get all of one, all of the other, or any combination of both. In this case, there is not just one optimal bundle. In this chapter, we will concentrate on the case where there is one optimal bundle, and so you, the consumer, have to purchase all of one or the other.

Consider **figure 4.4**, which illustrates a generic budget line (in black) for goods A and B and a series of indifference curves (in **blue**) representing preferences for the perfect substitutes of goods A and B. The slope of the indifference curves (the MRS) is always greater than the slope of the budget line (the ERS). As you can see from **figure 4.5**, this means that consumers always do better when they consume more A and less B—consumers move to a higher indifference curve.

Specifically, consider bundle 1 in the graph. This bundle contains both A and B. If we compare bundle 1 to the bundle in the corner of the budget constraint labeled "optimal bundle," you can see that the optimal bundle is on a higher indifference curve, which means that this bundle is better. In fact, this is true of any other bundle in the budget constraint—all other bundles place consumers on a lower indifference curve.

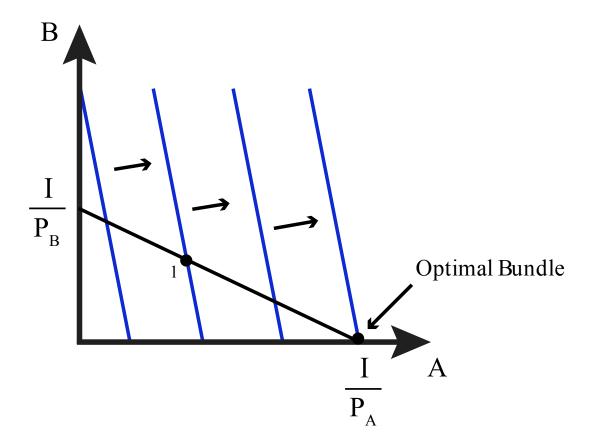


Figure 4.4 Solution to the consumer choice problem for perfect substitutes

Finding this optimal bundle is relatively easy mathematically. Since we know it has to be at a corner, we just need to check the two corners of the budget constraint and see which one yields the higher utility. In general, utility functions that represent perfect complements look like this:

$$U(A,B) = \alpha A + \beta B$$

Note that the additive form of the utility function is the key—you can always get to the same utility by taking away some of one good and adding some of the other (even if there is none of the other good in the bundle). Note also that the MRS is

$$MRS = \frac{\alpha}{\beta}$$

Since α and β are parameters, this means the slope of the indifference curve is a constant, and so the indifference curves for perfect substitutes are straight lines that intersect the axes.

Solving for the optimal consumption bundle for perfect substitutes starts with checking the corners, which means we ask what utility the consumer gets from spending all of their income on just one good. So if

$$P_A A + P_B B = I$$

and the consumer decides to consume only A, then the total amount consumed of A is

$$\frac{I}{P_A}$$

Similarly, the total amount consumed of B if all of the income is spent on B is

$$\frac{I}{P_B}$$

So all that is left to do is to check if

$$U(A,0)=lpharac{I}{P_A}>etarac{I}{P_B}=U(0,B)$$

if the opposite is true, or if they are equal.

If the above is true, then we know immediately that consuming only A is the optimal choice. Similarly, if the opposite is true, we know consuming only B is optimal. Finally, if they happen to be equal, any combination of A and B consumption along the budget line is optimal. **Figure 4.5** illustrates these three possibilities.

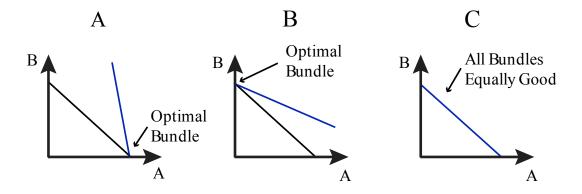


Figure 4.5 Solutions to the consumer choice problem for perfect substitutes. Solutions (a) and (b) show the corner solutions.

4.4 POLICY EXAMPLE

HYBRID CAR PURCHASE TAX CREDIT—IS IT THE BEST CHOICE TO REDUCE FUEL CONSUMPTION AND CARBON EMISSIONS?

Learning Objective 4.4: The Hybrid Car Tax Credit and Consumer Choice

Suppose you are a policymaker considering proposals to reduce the consumption of fossil fuels and carbon emissions. With the tools from chapters 1 through 4, you can now conduct an economic analysis to analyze the likely outcome of a tax credit for electric and hybrid cars. Begin by considering the consumer choice problem prior to the introduction of the tax credit.

First, combine the indifference curve mapping from <u>chapters 1</u> and 2 with the budget constraint from <u>chapter 3</u>, as shown in **figure 4.6**. Remember, these are simply graphical representations of the mathematical equations **4.4** and **4.5**.

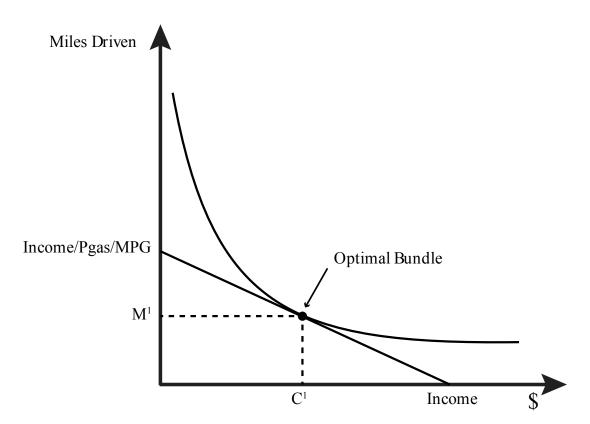


Figure 4.6 Optimal miles driven without car tax credit

We are looking for the point on the budget line that puts the consumer on the highest indifference curve possible. This is of course the tangency point between the indifference curve and the budget line. This tangency is characterized by the equality of the marginal rate of substitution between miles driven and other goods consumed and the price ratio of the same two goods, the economic rate of substitution. **Figure 4.6** shows that given our assumption of convex indifference curves, there is a unique point that defines the number of miles driven and the amount of money for other goods consumed that make up the optimal bundle for this "typical" consumer.

Mathematically, we can solve for the tangent point by remembering that it is characterized by two things:

- 1. The equality of the marginal rate of substitution to the price ratio
- 2. The budget constraint holding with equality

The first equation ensures that the bundle is at a point of tangency between the indifference curve and lines with the same slope as the budget line. But remember that the price ratio describes the slope, not the specific budget line, which is why we need the second equation to make sure we are on the specific line that describes the consumer's budget.

Specifically, if the utility function that represents the "typical" consumer's preferences over miles driven (M) and all other consumption (C) is

$$U(M,C)=M^{lpha}C^{eta}$$

then we can solve for the MRS:

$$MRS = rac{MU_M}{MU_C} = rac{rac{lpha U}{lpha M}}{rac{lpha U}{lpha C}} = rac{lpha}{eta}rac{C}{M}$$

As noted above, this is one condition that characterized the optimal consumption bundle. The other is the budget line:

 $Income = (Price_{MilesDriven}) (Miles \ Driven) + Dollars \ for \ Other \ Consumption$ We can solve this system of equations by the process of repeated substitution to come up with the description of the precise optimal bundle for this consumer.

Now let's consider what happens after policymakers pass the tax credit into law. From <u>chapter 3</u>, we know that the effect of the tax credit on the budget constraint is to make the cost of miles consumers drive less expensive, which represents a drop in the price of miles driven. This will cause the budget line to expand along the vertical axis, but it will not change the horizontal intercept. The consumer must now choose a new optimal bundle, and we must compare the new bundle to the old one. Let's first examine this graphically in **figure 4.7**.

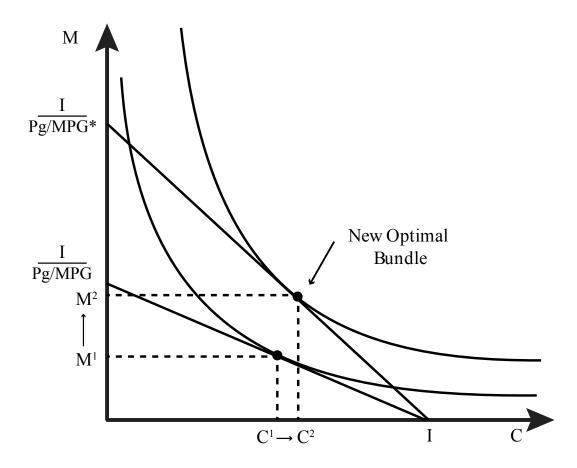


Figure 4.7 Optimal miles consumers drive with car tax credit

In this graph, it is clear that the new bundle represents more of both goods. The consumer will choose to consume more of other goods with the extra buying power that the more fuel-efficient car affords as well as to consume more miles driven due to the lower cost of the activity. So the policy turns out to have an unintended consequence: in an effort to decrease fuel consumption, the policy actually lowers the marginal cost of driving, inducing consumers to drive more.

By making some fairly basic assumptions about typical consumer preferences and modeling the consumer choice problem, economic theory suggests that we should expect an increase in miles driven as a result. This application illustrates the power of models. By simplifying reality into a model framework, we can discover something about the world and human behavior that was not obvious.

But this is just a theory, so it is suggestive rather than definitive. It is important to note that the assumptions we made may not be completely accurate, and so our prediction may be inaccurate. For example, depending on the precise indifference curve mapping, we could actually see decreased miles driven after the hybrid car tax credit.

We now need to test the theory by evaluating real-world data. So what does the data suggest? Studies have shown that

- 1. An increase in MPG increases how much consumers drive and
- 2. This effect is in the range of 10 to 30 percent, meaning that a 10 percent increase in MPG would increase how many miles consumers drive by between 1 and 3 percent.

In the case of fuel consumption, economists generally prefer that policymakers increase the gas tax–the subsidy approach–and other indirect approaches, like the <u>corporate fuel economy standard known as CAFE</u>.

The tax on fuel raises the cost of consumption and, as we have now seen, decreases fuel consumption. A <u>number of studies</u> have shown that an increase in the gas tax is a more cost-effective way to decrease gasoline usage.

With our analysis of the policy based on both theory and evidence, we are now in a position to answer the original question posed at the beginning of section 1.1.

Suppose that a hybrid car tax credit was wildly successful and succeeded in doubling the average fuel economy of all cars on US roads. What do you think would happen to the fuel consumption of all US motorists? Should the government expect the fuel consumption and carbon emissions of cars driven in the United States to decrease by half in response?

The answer is clearly no. Even the most conservative estimates suggest that a 100 percent increase in average fuel efficiency will result in an increase of miles driven by 10 percent, meaning that the decrease in fuel consumption and carbon emissions will fall but by less than half.

EXPLORING THE POLICY QUESTION

- 1. Suppose the hybrid car tax credit was accompanied by a tax increase on gasoline. How would the analysis of the policy change? Could you make a prediction about the change in carbon emissions now?
- 2. How would the analysis change if consumers' preferences change and they begin to lower their gas consumption by carpooling, walking, and biking more instead of driving? How could you show this in figure 4.7?
- 3. The phenomenon of increased energy efficiency leading to increased consumption is known among economists as the rebound effect, and it is common in other practical contexts besides vehicles and driving. What other examples of rebound effect would you expect to see in the real world?

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

4.1 The Consumer Choice Problem: Maximizing Utility

<u>Learning Objective 4.1</u>: Define the consumer choice problem.

4.2 Solving the Consumer Choice Problem

Learning Objective 4.2: Solve a consumer choice problem with the typical utility function.

4.3 Corner Solutions and Kinked Indifference Curves

Learning Objective 4.3: Solve a consumer choice problem with utility functions for perfect complements and perfect substitutes.

4.4 Policy Example

Hybrid Car Purchase Tax Credit—Is It the Best Choice to Reduce Fuel Consumption and Carbon Emissions?

Learning Objective 4.4: The Hybrid Car Tax Credit and Consumers' Budgets

LEARN: KEY TOPICS

Terms

Consumer choice problem

What is the consumer's optimal choice among competing bundles? Among all the bundles the consumer could possibly choose, which one returns the highest level of utility?

Corner solutions

A utility maximizing bundle that consists of only one of the two goods—in other words, a consumption bundle that is located at one corner of the budget constraint. Corner solutions are typical when preferences are perfect substitutes.

Demand functions

Mathematical functions that describe the relationship between quantity demanded and prices, income, and other things that affect purchase decisions.

Interior solutions

A utility maximizing bundle that has a positive amount of both goods.

Kinked curves

Curves that have abrupt changes in slope at a single point.

Graphs

Solution to the general consumer choice problem

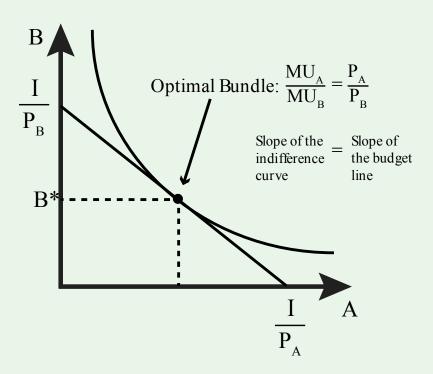


Figure 4.1 Indifference curve on the budget constraint

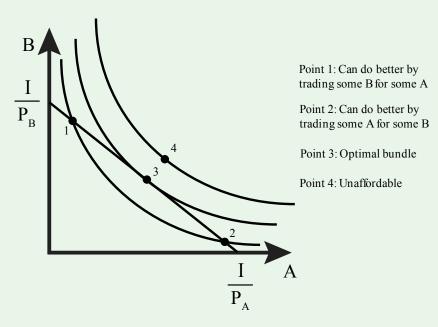


Figure 4.2 Budget line with three indifference curves

Solution to the consumer choice problem for perfect complements

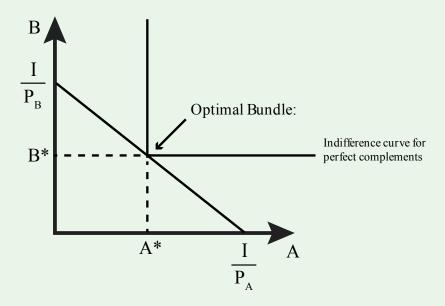


Figure 4.3 Solution to the customer choice problem for perfect complements

Solution to the consumer choice problem for perfect substitutes

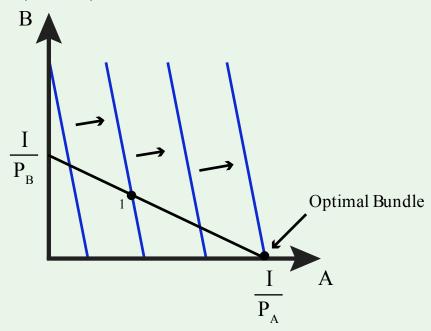


Figure 4.4 Solution to the consumer choice problem for perfect substitutes

Equation

Demand functions

The Demand Function for Good A

$$A = rac{I}{P_A} rac{lpha}{(lpha + eta)}$$

The Demand Function for Good B

$$B = \frac{I}{P_B} \frac{\beta}{(\alpha + \beta)}$$

The Consumer's Optimal Choice Problem

$$max\,U(A,B) \ (A,B) \ ext{subject to } P_A\,A + P_BB \leq I$$

The second line of the consumer's optimal choice problem (the "subject to" part) is the budget constraint. Using the more-is-better assumption, the equation is rewritten to indicate the consumer will always spend all of their budget on goods A and B, as below:

$$max\,U(A,B) \ (A,B) \ ext{subject to } P_AA+P_BB=I$$

Applying the Cobb-Douglas utility function

$$\max A^{lpha}B^{eta} \ (A,B)$$
 subject to $P_AA+P_BB=I$

To solve this requires taking the partial derivative. This equation looks as follows:

$$MU_A = rac{\partial (A^lpha B^eta)}{\partial A} = \partial A^{(a-1)} B^eta \ MU_B = rac{\partial (A^lpha B^eta)}{\partial B} = eta A^lpha B^{(eta-1)}$$

The MRS is the ratio of the two marginal utilities:

$$MRS = -rac{MU_A}{MU_B} = -rac{rac{\partial (A^lpha B)}{\partial A}}{rac{\partial (A^lpha B^eta)}{\partial B}} = rac{\partial A^{(a-1)}B^eta}{eta A^a B^{(eta-1)}} = -rac{lpha B}{eta A}$$

The ERS is the ratio of the prices:

$$MRT = -rac{P_A}{P_B}$$

When combined, they take the following form:

$$MRS = MRT \Rightarrow -rac{lpha B}{eta A} = -rac{P_A}{P_B} \Rightarrow rac{lpha}{eta} rac{B}{A} = rac{P_A}{P_B}$$

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The second part of consumer choice problem, the budget constraint, reads like this:

$$P_A A + P_B B = I$$

Solving the Cobb-Douglas Equation

Solving the problem involves repeated substitution. The MRS ratio initially solved for Bundle B is as follows:

$$B = rac{eta}{lpha} rac{P_A}{P_B} A$$

The next step is substituting the above result into the ERS ratio equation, providing the formula below:

$$P_A A + P_B \left(rac{eta}{lpha}rac{P_A}{P_B}A
ight) = I$$

Simplified:

$$rac{(lpha+eta)}{lpha}P_AA=I$$

Solved for A:

$$A = rac{I}{P_A} rac{lpha}{(lpha + eta)}$$

The result of the above equation substituted into the combined MRS/ERS equation is the demand function for good A:

$$A = rac{I}{P_B} rac{eta}{(lpha + eta)}$$

Solving again for B provides the demand function for good B:

$$B = \frac{I}{P_B} \frac{\beta}{(\alpha + \beta)}$$

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CHAPTER 5

Individual Demand and Market Demand

THE POLICY QUESTION

SHOULD YOUR CITY CHARGE MORE FOR DOWNTOWN PARKING SPACES?

Major cities have a significant number of parking spaces on public streets. In congested places, such as downtown areas, street parking is usually priced and limited in duration. Cities meter downtown parking for many reasons, including to raise revenue, ensure the frequent turnover of customers for local merchants, and ensure the availability of parking spots for those looking for parking. But how much should a city charge for parking in order to raise revenue or ensure available spots? The answer depends on understanding the *demand* for parking.

Demand is a natural topic after the consumer choice problem of maximizing utility among competing bundles of goods, which we studied in <u>chapter 4</u>. We saw in <u>chapter 4</u> that the solution to the consumer choice problem gives us, among other things, the individual demand functions. These functions tell us how much the individual consumer will demand of each good in order to maximize utility for *any* set of prices and income. And by taking into account all the individual demands, we can come up with an overall market demand for a good.



"Does DC's Pay by Phone Parking really work? A parking ticket dodging test" from Wayan Vota on Flickr is licensed under CC BY-NC-SA

EXPLORING THE POLICY QUESTION

- 1. What factors affect the demand for parking?
- 2. How sensitive is the demand for parking to price changes?

The main reason a city might want to set parking rates higher is to increase parking revenues or ensure enough available parking for those who drive downtown to conduct business—or both. For our policy

question, we'll concentrate on the second objective: to ensure that customers who come downtown to shop will be able to find a place to park.

In order to think about the policy question, we need to know the answers to two related questions: "What factors affect the demand for parking?" and "How sensitive is the demand for parking to price changes?" Answering these questions will provide insight into the demand for parking in general and allow us to answer the central policy question of whether the price for parking in the downtown area should be higher.

LEARNING OBJECTIVES

5.1 The Meaning of Markets

<u>Learning Objective 5.1</u>: Define the concept of a market.

5.2 The Demand Curve

<u>Learning Objective 5.2</u>: Describe a demand curve.

5.3 Summing Individual Demands to Derive Market Demand

Learning Objective 5.3: Derive market demand by aggregating individual demand curves.

5.4 Movement along versus Shifts of the Demand Curve

<u>Learning Objective 5.4</u>: Explain movements along versus shifts of the demand curve.

5.5 Price and Income Elasticity of Demand

Learning Objective 5.5: Calculate and interpret the price and income elasticity of a demand curve.

5.6 Income and Substitution Effects

Learning Objective 5.6: Identify income and substitution effects that result from a change in prices.

5.7 Policy Question

Should Your City Charge More for Downtown Parking Spaces?

Learning Objective 5.7: Use elasticity to determine how much city officials should charge for parking.

5.1 THE MEANING OF MARKETS

Learning Objective 5.1: Define the concept of a market.

Broadly defined, a **market** is a place where people go in order to buy, sell, or exchange goods and services. Markets can be physical or virtual, large or small, for one good or for many. In order to understand and derive demand curves, we need to specify the particular market we are studying.

A market is always for an **individual good** at a specific price. We can define a **collective good**, like sandwiches, only if we can describe a single price—as opposed to distinct prices for cheese sandwiches, club sandwiches, and sub sandwiches, for example. There are many types of sandwiches, and therefore no one price exists. However, for a restaurant owner, the specific market for cheese sandwiches does not matter as much as how the market behaves for sandwiches in general. Just remember that when we are analyzing markets, we are talking about a specific good with a specific price.

A market for a good is also defined by a place and a time. For example, we could study the market for iPhones in the United States in 2014, in California in May 2014, or even in Cupertino on May 5, 2014. In order to talk reasonably about a quantity demanded, we have to know who is demanding the quantity and when.

Sometimes the boundaries of a market are not entirely clear. Think about the market for telephone calls. Does this include wired home telephone service through dedicated wires (yes), telephone over coaxial cable (almost certainly), mobile phones (probably), voice over internet protocol (maybe), texting (probably not)? We will return to this issue in future chapters when we discuss market concentration, so for now, just understand that market boundaries can sometimes be hard to define.

A market must have

- a good specific enough to have a single price,
- · a defined time or time period, and
- a defined place.

5.2 THE DEMAND CURVE

Learning Objective 5.2: Describe a demand curve.

As we saw in <u>chapter 4</u>, when we solve the consumer choice problem—that is, when we determine the optimal consumption bundle based on the current prices of the goods and the income of the consumer—we end up with a demand function.

A **demand curve** is a graphical representation of the demand function that tells us for every price of a good how much of the good is demanded. As we saw from deriving the demand function in <u>chapter</u> 4, other factors help determine the demand for a good—namely, the price of the other good and the buyer's income. Holding the price of the other good and buyer's income constant and changing prices, the demand function describes the optimal consumption quantity for every price—that is, what quantity the individual will demand at every price.

Figure 5.1 illustrates how the demand curve for coffee is derived from the consumer choice problem. In the upper panel, we see that as the price of coffee increases, the consumer chooses to consume less and less coffee. In the lower panel, we can plot the pairs of price and quantity of coffee consumed at that price to draw the demand curve.

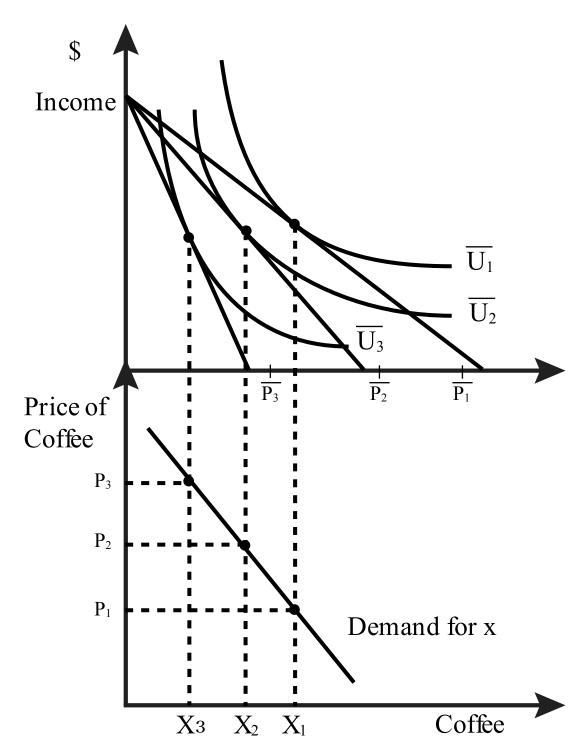


Figure 5.1 Deriving individual demand curves from consumer consumption choices

In the top graph of **5.1**, the price of coffee increases from P_1 to P_2 and then to P_3 . Since this is an increase of the price of the good, this consumer chooses to consume less as the price increases. The bottom graph plots the combinations of prices of coffee and quantities consumed (demanded) of coffee: P_1 and X_1 , P_2 and X_2 and P_3 and X_3 .

Note that by keeping the price and income of other goods constant, we are simply changing the slope of the budget line and anchoring it at the vertical intercept.

As an example, let's consider Marco, who eats burritos and pizza slices. **Figure 5.1** describes his weekly consumption. The top panel shows his consumption bundles given the prices of burritos and pizza and his income. The bottom panel shows his demand curve.

In the top panel, we see that Marco has a weekly income of \$15 to spend on burritos and pizza slices. Originally, when the prices are \$1.50 each, he consumes five burritos and five slices of pizza. When the price of pizza falls to \$1, Marco adjusts his consumption to six burritos and six slices of pizza. When the price of pizza slices falls for a second time to \$0.50, Marco adjusts his consumption to seven burritos and nine slices of pizza.

For each price, there is a unique solution to the consumer choice problem. By mapping the price and resulting optimal consumption pairs, we can describe this individual's demand curve for pizza slices, as shown in the bottom panel. At a price of \$1.50 per slice, Marco demands five. At a price of \$1, Marco demands six, and at a price of \$0.50, Marco demands nine. We can plot these points on a graph that has price on the vertical axis and quantity of pizza slices on the horizontal axis.

By connecting these price-quantity points with a line, we graphically approximate the demand curve. These points are the same as the price and quantity pairs you would get directly from the demand function when you hold the price of the other good and income constant. The difference is that the demand function is continuous and therefore has a continuous graph that we can draw precisely. For our purposes now, the approximate demand curve is sufficient.

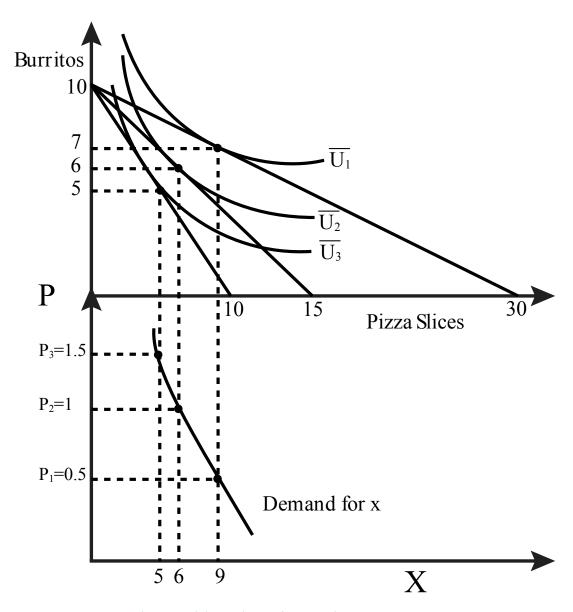


Figure 5.2 Marco's consumption choices and demand curve for pizza slices

Note that as the price of a good declines, the consumer consumes more and more of the good because, holding the other price and income constant, the consumer's income goes further. In our example, this means that Marco consumes more of both burritos and pizza slices. His demand curve exhibits the **law of demand**: as price decreases, quantity demanded increases, holding other factors such as income and the price of other goods constant. It is worth noting that this "law" has limits—it does not hold for certain types of goods, as we will discuss in <u>chapter 6</u>.

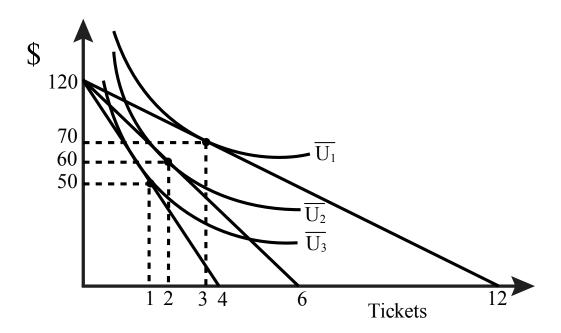


Figure 5.3 Law of Demand

5.3 SUMMING INDIVIDUAL DEMANDS TO DERIVE MARKET DEMAND

Learning Objective 5.3: Derive market demand by aggregating individual demand curves.

The demand curve we described for Marco's weekly consumption of pizza slices is an individual demand curve. It tells us precisely how many slices of pizza Marco will demand for each price. But if you sell pizza slices in Marco's neighborhood, it does not tell you what the total demand for a week will be. In order to derive the market demand curve, we need to know the demand curve for every person in the neighborhood.

As noted in <u>section 5.1</u>, the market we are describing is the weekly demand for pizza slices in Marco's neighborhood. We are implicitly assuming that all pizza slices are identical and that Marco and other demanders of pizza will buy it in the neighborhood.

Suppose that there are only three people who eat pizza slices in the neighborhood and one pizza vendor and that each customer has a demand curve for pizza slices identical to Marco's. What is the correct way to think about the total (or market) demand for pizza? Consider what the pizza shop owner will experience:

- When she sets the price at \$1.50, she sees three customers who each demand five slices of pizza or a total demand of 5+5+5=15 slices of pizza.
- When she lowers the price to \$1, she sees a total demand of 6+6+6=18 slices of pizza.
- When she lowers the price to \$0.50, she sees a total demand of 9+9+9=27 slices of pizza.

These are the three points on the total demand curve in figure **5.4**:

1.
$$Q = 15$$
 at $P = 1.50

2.
$$Q=18$$
 at $P=\$1$

3.
$$Q = 27$$
 at $P = \$0.50$

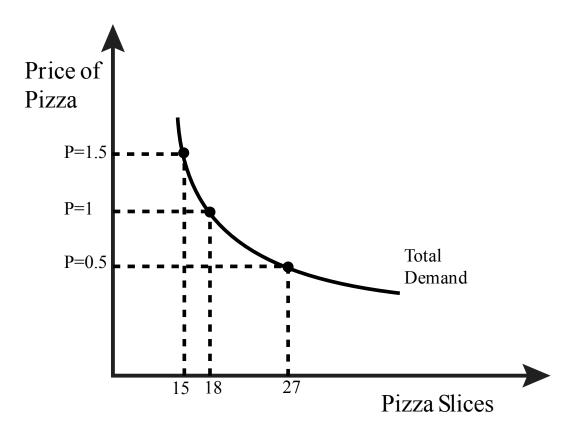


Figure 5.4 Total demand curve for pizza slices

By connecting the three points with a line, we can approximate the actual demand curve. The key takeaway from this simple example is that we are summing up quantities at every price. Keep this in mind as we move on to demand functions.

What about making a total demand curve by aggregating demand functions? Let's consider three simple individual demand functions for pizza for customer A, customer B, and customer C:

- 1. $Pizza_A = 150 p$
- 2. $Pizza_B = 100 p$
- 3. $Pizza_C=100-2p$

We want to sum them up to arrive at the total demand. Let's start by graphing them, as shown in figure **5.5**.

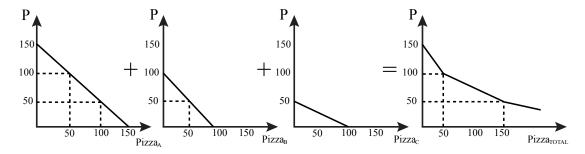


Figure 5.5 Summing three demand functions

We want total demand, which is the sum of all the quantities at every price, or $Pizza_{\mathrm{TOTAL}} = Pizza_A + Pizza_B + Pizza_C$. To get this, we can simply add up the left and right sides of the equations above. If we did so, we would get

$$Pizza_{\mathrm{TOTAL}} = 350 - 4p$$

Is this total demand function correct?

Consider a price of \$25. From the individual demands, we know that $q_A=125$, $q_B=75$, and $q_C=50$, so the total demand is 250. If we put p=\$25 directly into our total demand function, we get

$$Pizza_{\rm TOTAL} = 350 - 4(25) = 250.$$

Another way of thinking about total demand is to sum the three demands in the individual graphs horizontally, which reveals a problem with our total demand function. Notice that at a price of \$75,

$$Pizza_A = 75$$
, $Pizza_B = 25$, and $PizzaC = 0$,

so the total demand is one hundred. Note that demands cannot have a negative number.

If we put p=\$75 into the aggregate function, we get

$$Pizza_{\text{TOTAL}} = 350 - 4(75) = 50.$$

In this case, we have not accounted for the fact that q_C has stopped at zero. So we have not quite accurately described the total demand.

Note that the graph of each individual demand function has a different vertical intercept. So we have to account for the case where a demand goes to zero. For customer C, this is at p=\$50; for customer B, this is at p=\$100; and for customer C, this is at p=\$150. It's important to note that for prices above \$50, there are only two consumers who still demand, consumers B and A. And for prices above \$100, only consumer A demands. We can express the demand curve by the function

$$egin{array}{lll} 350 - 4p, ext{ for } p & \leq 50 \ 250 - 2p, ext{ for } 50 &$$

This demand function is a bit complicated but makes sense if you focus on the prices when demand goes to zero for each consumer.

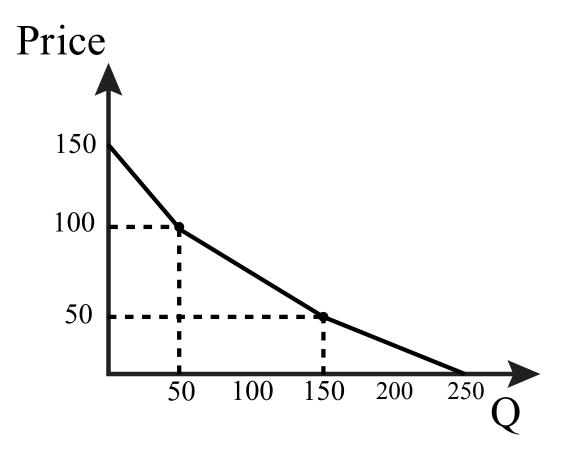


Figure 5.6 Total demand curve for three individual demand functions

Graphing the total demand curve in **figure 5.6** reveals a kinked demand curve but one that is downward sloping. When we examine a market with only a few potential customers, it is reasonable to expect kinks at the prices where potential customers turn into real customers. But it is easy to see that as we add more and more demand curves together, the individual kinks will become smaller and more frequent. After we have added enough demand together, we get a smooth and downward-sloping market demand curve.

5.4 MOVEMENT ALONG VERSUS SHIFTS OF THE DEMAND CURVE

<u>Learning Objective 5.4</u>: Explain movements along versus shifts of the demand curve.

The market demand curve describes the relationship between the price a good is offered at and the resulting quantity demanded. As the price of a good moves higher and lower, consumers demand different quantities of the good, and the demand function and resulting graph change in response.

But we know that variables other than price can affect the demand for a particular good—for example,

- the income of consumers and
- the price of complements and substitutes

A host of other factors might influence the consumer's demand for a good as well, including advertising, the popularity of the good, and news stories about its health benefits or risks.

How do these potential impacts conform to our observation that the demand curve is simply a description of the quantity demanded for any given price? This is where the concept of *ceteris paribus* comes in: this Latin phrase means, roughly, all other things remain the same. Here, *ceteris paribus* means that any demand curve that we graph is for a specific set of circumstances—we are considering only the price of the good and holding all the other factors that affect demand constant.

Once we have a particular demand curve, we can observe what happens when a factor is allowed to change.

- Changes in price cause movements along the demand curve.
- Changes in factors other than the price of the good itself cause *shifts* in the demand curve.

Movement Along the Demand Curve

Figure 5.7 illustrates the market demand for jeans. We assume jeans are generic and leave unspecified the time and place of this market; these simplifications will make the analysis easier to follow. For a given and fixed set of factors—such as income, prices of other goods, and advertising—this demand curve describes the relationship between the price of jeans and the quantity of jeans demanded. We can see, for instance, that when the price of jeans increases from \$40 to \$50, the quantity demanded will decrease from 100,000 to 90,000. The change in price causes a movement along the demand curve.

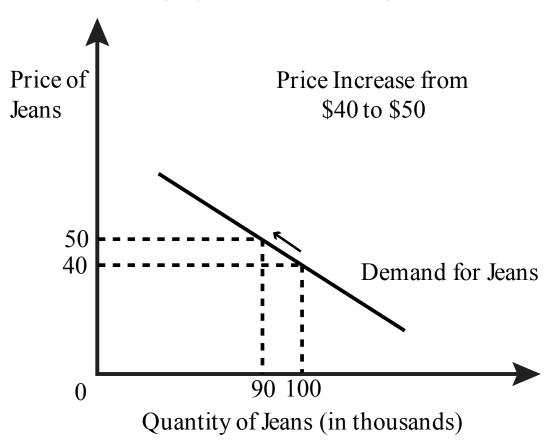


Figure 5.7 A price increase or decrease causes movement along the demand curve.

Shifting the Demand Curve

So what happens when factors other than price change? Let's start by thinking about incomes.

What would happen to demand if incomes increase, perhaps because the government sends everyone a tax rebate? Is it reasonable to consider jeans a **normal good**, or a good for which demand increases when incomes rise? How does this tax rebate affect our graph? When we say demand increases, we mean that for every price, we expect a greater quantity demanded after the income increase than before it. This means that at a given price, the quantity demanded increases, or shifts to the right, farther along the x-axis in our graph. In **figure 5.8**, it is a parallel shift—the slopes of the original and revised demand curve remain the same—which might well happen. But in general, we can only say that demand will shift rightward; the slope or shape of the graph could change after an income increase.

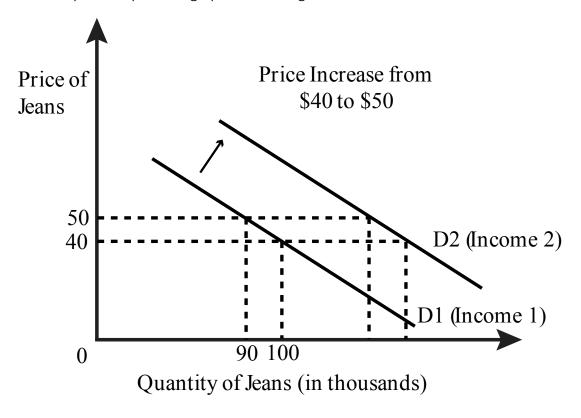


Figure 5.8 An increase in income shifts the demand curve to the right.

What about factors other than price, like the price of substitutes or an increase in advertising for jeans? Let's try them both.

Suppose the price of khaki pants—a substitute for jeans—falls. Is it reasonable to expect that consumers looking for new pants might decide to buy khaki pants rather than jeans? We should expect a decrease in the quantity demanded of jeans at any given price. This decrease causes the demand curve to shift to the left. **Figure 5.9** shows the leftward shift of the demand curve due to a fall in the price of a substitute—khaki pants.

Suppose a jeans company hires a top model or celebrity to advertise its jeans. An increase in advertising for jeans should make potential consumers think more positively about jeans and increase their demand, which causes the demand curve to shift to the right. **Figure 5.9** shows the rightward shift of the demand curve due to the new or increased advertising.

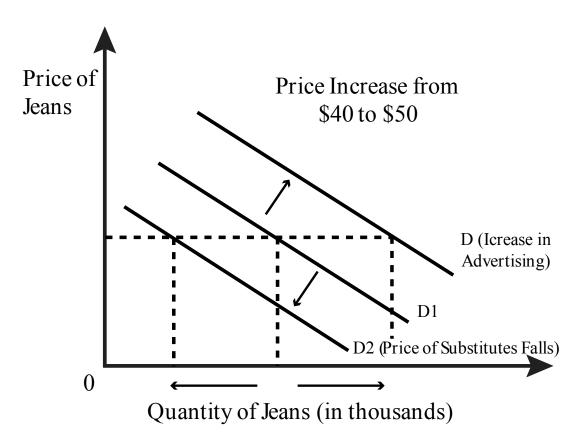


Figure 5.9 Changes in other factors shift the demand curve right or left.

For each change we have made in factors that affect demand, other than the price of the good, the demand curve shifted to the left or right. Here is a good rule to remember: changes in the price of the good result in movements along the demand curve, while changes in any other factor that affects demand result in shifts in the demand curve.

5.5 PRICE AND INCOME ELASTICITY OF DEMAND

Learning Objective 5.5: Calculate and interpret the price and income elasticity of a demand curve.

Businesses, governments, and economists are interested in how sensitive demand is to changes in prices and income. For example, a city government might want to estimate the effect of a change in parking rates on its budget revenue. Because economists often like to compare markets across products, time, and units of measure, we prefer to have a measure of demand sensitivity that is unit-free. This means it doesn't matter if we are talking about gallons of milk, liters of cola, pounds of flour, kilos of sugar, or pairs of socks. Similarly, we don't want to worry about talking in 2014 dollars, 1950 dollars, or 1975 pounds.

The way we measure demand sensitivity in a unit-free way is to measure **price elasticity of demand**, which is the percentage change in the quantity demanded of a product resulting from a 1 percent change in price.

The price elasticity of demand is defined mathematically as

Sticity of demand is defined mathematically as
$$E = rac{ ext{Percentage change in quantity demanded}}{ ext{Percentage change in price}} = rac{\Delta Q/Q}{\Delta P/P'}$$

where

- Δ (delta) indicates a change in a variable,
- ΔQ refers to a change in a quantity demanded, and
- ΔP refers to a change in price.

Note that $\Delta Q/Q$ is the definition of a percentage change.

Let's look at a numerical example. Suppose the demand for lemonade from a lemonade stand on a busy street corner increases from 100 cups a day to 110 cups a day when the price decreases from \$2 to \$1.90. The change in quantity, ΔQ , is an increase of 10 cups, or +10. The change in price, ΔP , is a decrease of \$0.10 cups, or -0.10. So we have

$$\frac{\Delta Q/Q}{\Delta P/P} = \frac{10/100}{-0.10/2} = \frac{0.1}{-0.05} = -2.$$

Note that the elasticity we calculated is negative. Price elasticity of demand is usually negative, reflecting the law of demand: As price decreases, quantity demanded increases. Note also that the elasticity we calculated does not indicate what units the quantities are measured in or what currency or time the prices were measured in. None of that matters because we are only dealing with percentage changes.

How do we interpret the -2 value of elasticity? It tells us how much quantity demanded changes when the price increases by 1 percent. But wait, didn't prices change by 5 percent? Yes, but the elasticity says that for every 1 percent increase in price, we should see a -2 percent change in quantity demanded (multiply by the elasticity).

Table 5.1 Classifying values of price elasticity of demand Value of price elasticity of **Description of** Interpretation demand Perfectly inelastic Quantity demanded does not change at all with price. From 0 to -1 Inelastic Quantity demanded is relatively unresponsive to price changes. Unit elastic Percentage change in quantity demanded is equal to percentage change in price. From -1 to -Elastic Quantity demanded is relatively responsive to price changes. Quantity demanded goes to zero with any increase in price and goes to infinity with any Perfectly elastic

Figure 5.10 shows demand curves that are more and less elastic as well as demand curves that are perfectly inelastic and perfectly elastic. Notice that the slope of the elastic demand curve is less steep than that of the inelastic demand curve, as it takes a small change in P (price) to induce a large change in Q (quantity) relative to the inelastic demand. However, note that the elasticity is constantly changing along the demand curves, so to compare elasticity across demand curves, you have to compare them at the same price (see figure 5.11).

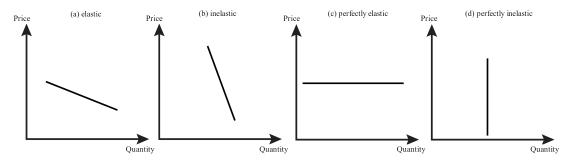


Figure 5.10 Demand Curves

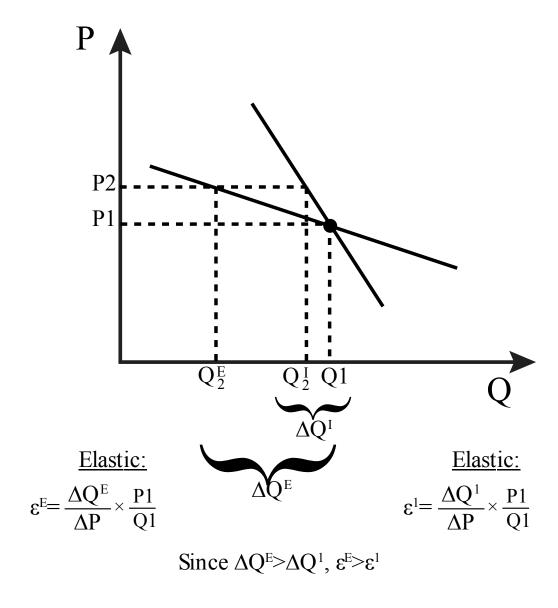


Figure 5.11 Comparing elasticity across two demand curves

We can use elasticity to measure other demand sensitivities, such as sensitivity to a change in the price of another good or to a change in income.

The **cross-price elasticity of demand** is the percentage change in the quantity demanded of a product resulting from a 1 percent change in the price of another good. It is defined mathematically as

$$E_{x,y} = rac{ ext{Percentage change in quantity demanded of good x}}{ ext{Percentage change in price of good y}} = rac{\Delta Q_x/Q_x}{\Delta P_y/P_y}$$

The cross-price elasticity of demand describes the sensitivity of demand for one good to a change in the price of *another* good. From this formula, we can quickly determine if two goods are complements or substitutes. A positive value of cross-price elasticity of demand means that an increase in the price of one good will increase the demand for the other. This indicates the two goods are substitutes: Consumers will substitute more of the other good as the price of the first good increases. Examples of **substitutes** are Coke and Pepsi, Apple computers and PCs, and private cars and public transportation. Similarly, if the cross-price elasticity of demand is negative, the goods are **complements**: since they are consumed together, raising the price of one raises the price of the combination, so consumers cut back on both. Examples of complements are tortilla chips and salsa, iPods and headphones, and tennis rackets and tennis balls.

Economists are often interested in seeing how a change in income affects demand—for instance, how a government tax rebate will affect the demand for used economics textbooks. The **income elasticity of demand** is the percentage change in the quantity demanded for a product from a 1 percent change in income.

Income elasticity of demand is defined mathematically as

$$E_I = rac{\% ext{ change in quantity demanded}}{\% ext{ change in income}} = rac{\Delta Q/Q}{\Delta I/I}$$

Suppose that your income increases from \$1,000 a month to \$1,200 a month and your demand for songs on iTunes changes from ten a month to twelve a month as a result. Let's find the income elasticity of demand.

$$rac{\Delta Q/Q}{\Delta I/I} = rac{2/10}{200/1,000} = rac{0.2}{0.2} = 1$$

Note that this value of one indicates that the income elasticity of your demand for iTunes is unit elastic. That is, the quantity response is proportional to the change in income.

A positive value of income elasticity of demand indicates a **normal good**, or a good for which the quantity demanded increases as income rises. We call goods for which the quantity demanded falls as income rises **inferior goods**. Inferior goods have a negative value of income elasticity of demand. **Figure 5.12** shows an example of an inferior good: as income rises, the quantity of ramen consumed falls.

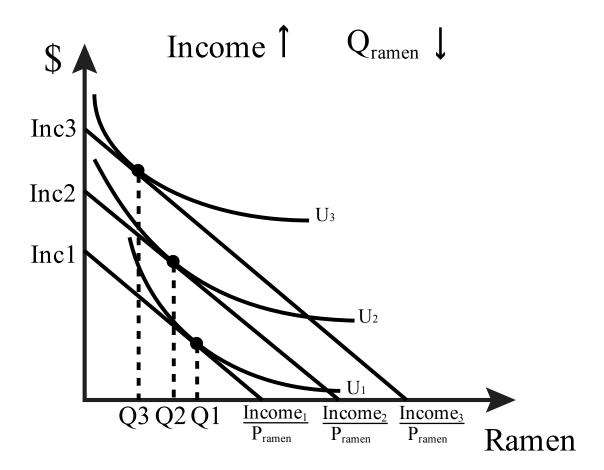


Figure 5.12 Demand for an inferior good



"Ramen Noodle Soup Oriental Flavor" from Bradley Gordon on Flickr is licensed under CC BY

Example—if the demand function is

$$Q_D = 100 - \frac{1}{2}P$$

the price elasticity of demand is

$$E = \frac{dQ}{dI} \frac{I}{Q}$$

From the laws of differentiation, we know

$$\frac{dQ}{dP}$$
 is $-\frac{1}{2}$

Therefore,

$$rac{dQ}{dP}rac{P}{Q}$$
 is $-rac{1}{2}rac{P}{Q}$

By substituting $100-rac{1}{2}P$ for Q, we

get an expression entirely in ${\it P}$:

$$E = -\frac{1}{2} \frac{P}{100 - \frac{1}{2}P}.$$

Calculus

Elasticity formulas—note that we can re-write the formulas for price and income elasticity of demand as

$$E=rac{\Delta Q}{\Delta P}rac{P}{Q}, E_{x,y}=rac{\Delta Q_x}{\Delta P_y}rac{P_y}{Q_x}$$
 and $E_I=rac{\Delta Q}{\Delta I}rac{I}{Q}.$

Since the derivative gives the instantaneous rate of change, $\dfrac{\Delta Q}{\Delta P}$ can be

expressed as the derivative $\dfrac{dQ}{dP}$.

Therefore, the elasticity formulas can be written as

$$E=rac{dQ}{dP}rac{P}{Q}$$
 , $E_{x,y}=rac{dQx}{dPy}rac{P_y}{Qx}$, and $E_I=rac{dQ}{dI}rac{I}{Q}$.

Now if we want to know where the demand curve is unit elastic, we can set the elasticity to one and solve (note that we can drop the negative sign from the $\frac{1}{2}$, since we are interested in the absolute value):

$$1 = \frac{1}{2} \frac{P}{100 - \frac{1}{2}P}$$

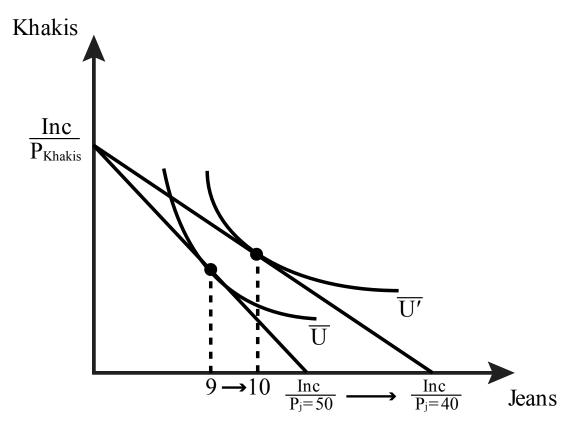
Solving this for **P** yields

$$200 - P = P$$
 or $P = 100$.

5.6 INCOME AND SUBSTITUTION EFFECTS

Learning Objective 5.6: Identify income and substitution effects that result from a change in prices.

Recall that the <u>consumer choice problem</u> is what gives us the individual demand curve. In **figure 5.13**, changes in the price of jeans lead to different consumption choices of both jeans and khakis. We can see precisely how the fall in the price of jeans from \$50 to \$40 leads to the increase in demand for jeans. In the market, this increase was from ninety thousand pairs of jeans to one hundred thousand pairs of jeans, but now we are back to an individual consumer who goes from purchasing nine jeans to purchasing ten jeans, let's say in a year (yes, they buy a lot of jeans!).



5.13 Change in consumption of jeans due to price change

Notice in the graph that after the price of jeans falls (again, assuming everything else held constant), the consumer increases not only their consumption of jeans but also their consumption of khakis. This result occurs because the real value of consumer income has increased; under the new prices, the consumer can afford more of both goods. We call this an **income effect**: an increase in real income means the consumer purchases more of normal goods. Formally, the income effect is the change in consumption of a good resulting from a change in a consumer's income, holding prices constant.

But something else has happened as well: the *relative prices* of the two goods have changed. Jeans are now *relatively* cheaper than they used to be compared to khakis. This change is a **substitution effect**—the change in relative prices means that consumers naturally consume more of the now relatively cheaper good compared to the now relatively more expensive good. Formally, the substitution effect is the change in consumption of a good resulting from a change in its price, holding the consumer's utility level constant.

A question economists often ask is how much of the resulting change in consumption of jeans—what we call the **total effect** of the price change—is due to the income effect, and how much is due to the substitution effect? They care about this because understanding how much of a change is due to each allows us to better predict the effect of changes in demand from changes in income and prices in the future. The easiest way to think about an answer is with a thought experiment: What if we could adjust the consumer's nominal income after the change in price so that in the end, they are no better or worse off? How would this income adjustment look on the consumer choice graph?

Let's start with the condition that the consumer is no better or worse off after the change in price than before it. This means that by definition, the consumer must still be consuming on the *same indifference curve*. So after the change in price, we adjust the nominal income so that the new budget line just touches the old indifference curve. Remember that changes in nominal income lead to shifts in the budget line but do not change the slope. If we shift the new budget line back to where it just touches the indifference curve, we can find the bundle that the consumer would choose under these hypothetical circumstances. By comparing the original consumption bundle to the hypothetical one, we can isolate the substitution effect. The change in jeans consumption in this case has nothing to do with income (in the sense that the consumer is just as well off) and everything to do with the change in the price of jeans.

As long as the indifference curve conforms to the "well-behaved" conditions discussed in chapter 1, the substitution effect will always act in the same way. When relative prices change, consumers will substitute away from the good that has become relatively more expensive and toward the good that has become relatively less expensive.

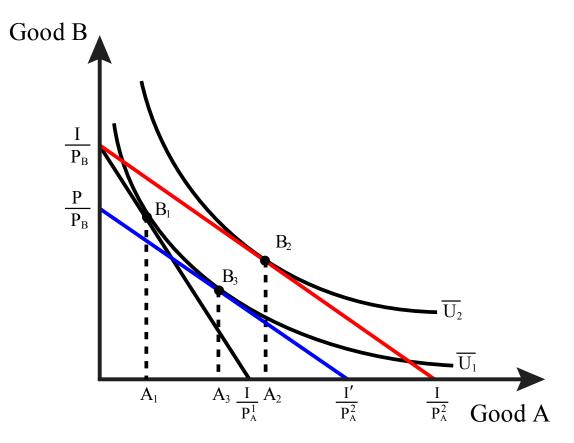


Figure 5.14 Decomposing consumption change into income and substitution effects

The income effect, however, may be either positive or negative depending on whether the good is normal or inferior. Recall that for an inferior good, an increase in income leads to a decrease in consumption. The total effect can still be positive, even in the case of an inferior good, if the substitution effect is larger than the income effect. Only in the case of an inferior good whose income effect is larger than the substitution effect do we get a **Giffen good**: a good for which a decrease in price leads to a *decrease* in consumption (or an increase in price leads to an *increase* in consumption; **figure 5.15**).

Consider the case of a family that likes to eat salmon (expensive) and potatoes (relatively cheap) every meal. On a fixed budget, they might start out with very small pieces of salmon and large portions of potatoes to meet their daily caloric needs. Now, what if their income stays the same but the price of potatoes decreases? Their fixed income can now buy more of both goods, but they don't need more calories. They would prefer instead to have larger portions of salmon and smaller portions of potatoes. So as their real income goes up due to the drop in the price of potatoes, they consume more salmon and *fewer* potatoes. For this family, potatoes are a Giffen good.

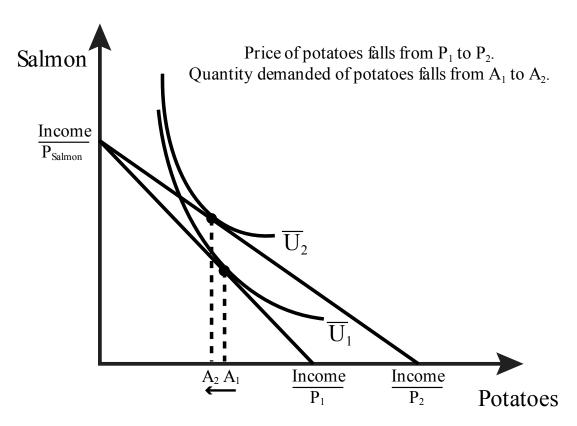


Figure 5.15 Potatoes as a Giffen good

5.7 THE POLICY EXAMPLE

SHOULD YOUR CITY CHARGE MORE FOR DOWNTOWN PARKING SPACES?

Learning Objective 5.7: Use elasticity to determine how much city officials should charge for parking.



"Parking Meter Parking Pay Coins San Diego Park Fee" on maxpixel.net is licensed under CCO

The city of San Francisco would like to encourage shoppers and clients of local businesses and other day-trippers to visit the downtown area. City officials know that one main factor in people's decision to come downtown is the availability of parking. The city controls the surface parking spots, the curb parking, and charges for parking through the use of meters, so officials know they can use the price of parking to change the number of shoppers and clients who visit through the law of demand.

- Price the parking too low, and day-trippers will increase their quantity demanded of parking spaces. Potential shoppers and clients will become discouraged by their inability to find parking.
- Price the parking *too high*, and day-trippers will decrease their quantity demanded of parking spaces. When too few day-trippers come downtown, the local merchants will complain about the lack of customers (even though the parking is plentiful!).

Understanding the nature of the demand for parking enables the city to get the pricing just right.

By knowing the price elasticity of demand for parking in the downtown area, San Francisco officials can predict how much the quantity demanded will fall if they raise rates and, conversely, how much it will rise as rates decrease. Understanding the demand function allows city planners to anticipate changes in demand from other factors, including incomes, weather, and days of the week. In the days of mechanical coin-operated meters, cities were forced to pick one price. With modern electronic technology, cities can become much more flexible with pricing. Take, for example, San Francisco's dynamic pricing scheme. In San Francisco, smart meters can adjust parking rates from as low as \$0.25 an hour to \$6 an hour. In times of high demand (e.g., sporting events), the rates will rise for local parking, and in times of low demand, rates will fall. This is the mission statement from SF Park, the local bureau in charge of setting rates.

<u>SF Park charges the lowest possible hourly rate</u> to achieve the right level of parking availability. In areas and at times where it is difficult to find a parking space, rates will increase incrementally until *at least one*

space is available on each block most of the time. In areas where open parking spaces are plentiful, rates will decrease until some of the empty spaces fill.

Let's take a simple hypothetical example. Suppose the city of San Francisco has exactly one thousand one-hour parking spaces available over one hundred city blocks. City planners have estimated the hourly demand for parking (Q_D) as 3,000 – 600P, where P is the hourly price of parking. Suppose that city planners have determined that to reduce congestion and pollution from drivers searching for available parking, the optimal hourly demand for parking is nine hundred per hour (averaging one free space per block). What should they charge per hour of parking? The answer is \$3.50. We find this price by setting Q_D at nine hundred and solving for P.

Since the precise demand curve is difficult to ascertain, a more realistic example is one where the city has a pretty good idea of the price elasticity of demand for hourly parking. Suppose the city estimates that the elasticity at current prices is close to one. Currently, the city charges \$2 an hour, and the demand for spots is one thousand hours. The city's goal is to decrease this demand to nine hundred hours. Since a one-hundred-spot reduction in demand represents a 10 percent decrease and the elasticity is one, the city knows that a 10 percent increase in price should accomplish the goal. The city should therefore increase parking rates to \$2.20 an hour.

EXPLORING THE POLICY QUESTION

The demand for hourly parking in Cleveland, Ohio, is given by the demand function

$$Q_D = 3,600 - 400P$$
.

Suppose Cleveland has 1,600 hourly spots available. What should Cleveland charge for hourly parking if the goal is to keep 10 percent of the spots open at any given time in order to encourage shoppers, clients, and day-trippers to come to the downtown core?

show answer 10 percent of 1,600 is 160

So Cleveland city planners want hourly demand to be $Q_D=1,440$ (or 1,600 – 160). Therefore:

$$1,440=3,600-400P$$
, and $400P=2,160$, or $P=2,160/400$, or $P=\$5.40$ an hour

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

5.1 The Meaning of Markets

<u>Learning Objective 5.1</u>: Define the concept of a market.

5.2 The Demand Curve

Learning Objective 5.2: Describe a demand curve.

5.3 Summing Individual Demands to Derive Market Demand

<u>Learning Objective 5.3</u>: Derive market demand by aggregating individual demand curves.

5.4 Movement along versus Shifts of the Demand Curve

<u>Learning Objective 5.4</u>: Explain movements along versus shifts of the demand curve.

5.5 Price and Income Elasticity of Demand

Learning Objective 5.5: Calculate and interpret the price and income elasticity of a demand curve.

5.6 Income and Substitution Effects

Learning Objective 5.6: Identify income and substitution effects that result from a change in prices.

5.7 Policy Example

Should Your City Charge More for Downtown Parking Spaces?

Learning Objective 5.7: Use elasticity to determine how much city officials should charge for parking.

LEARN: KEY TOPICS

Terms

Ceteris paribus

Roughly translated from Latin as "all other things remain the same." In English, used to mean that any demand curve that we graph is for a specific set of circumstances—we are considering only the price of the good and holding all the other factors that affect demand constant.

Cross-price elasticity of demand

The percentage change in the quantity demanded of a product resulting from a 1 percent change in the price of another good.

Giffen good

A good for which a decrease in price leads to a decrease in consumption (or an increase in price leads to an increase in consumption; figure 5.15).

Income effect

The change in consumption of a good resulting from a change in a consumer's income, holding prices constant.

Income elasticity of demand

The percentage change in the quantity demanded for a product from a 1 percent change in income.

Inferior good

A good for which the quantity demanded decreases as income rises.

Law of demand

As price decreases, quantity demanded increases, holding other factors such as income and the price of other goods constant. The law has limits, as discussed in chapter 6.

Market

A place where people go in order to buy, sell, or exchange goods and services. Markets can be physical or virtual, large or small, for one good or for many.

Defining a Market for a Demand Curve

A market must have

- 1. a good specific enough to have a single price,
- 2. a defined time or time period, and
- 3. a defined place.

Place and Time, elaborated

A market for a good is also defined by a place and a time, i.e., we could study the market for iPhones in the United States in 2014, in California in May 2014, or even in Cupertino on May 5, 2014.

Normal good

A good for which the quantity demanded increases as income rises

Price elasticity of demand

The percentage change in the quantity demanded of a product resulting from a 1 percent change in price.

Substitution effect

The change in consumption of a good resulting from a change in its price, holding the consumer's utility level constant.

Total effect

The total resulting change in consumption due to both the income effect and the substitution effect.

Graphs

Demand function

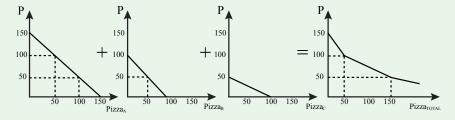


Figure 5.2 Building a graph for a demand function

Movement along the demand curve

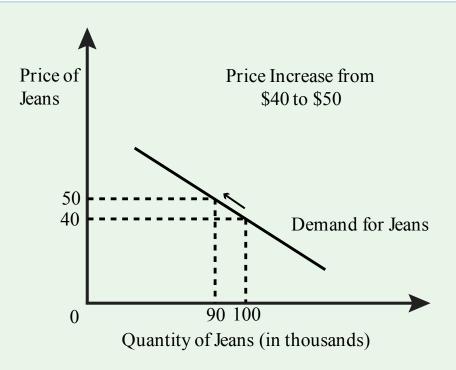


Figure 5.7 A price increase or decrease causes movement along the demand curve.

Shifting the demand curve

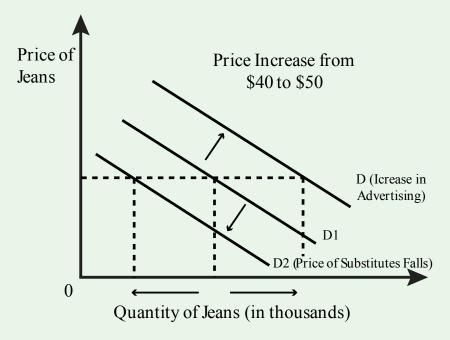


Figure 5.9 Changes in other factors shift the demand curve right or left.

Inferior good

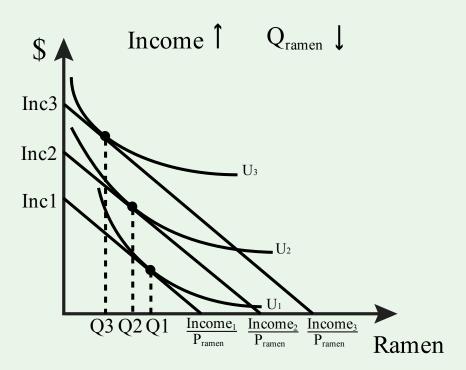


Figure 5.10 Demand for an inferior good

Giffen good

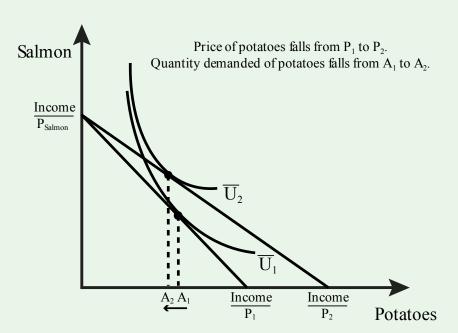
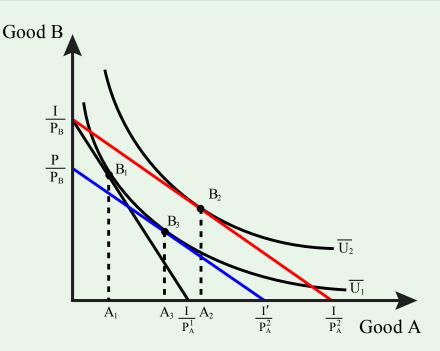


Figure 5.15 Potatoes as a Giffen good

Income and substitution effects



5.14 Decomposing consumption change into income and substitution factors

Equations

Income elasticity of demand

$$E_I = rac{\% ext{ change in quantity demanded}}{\% ext{ change in income}} = rac{\Delta Q/Q}{\Delta I/I}$$

Price elasticity of demand

Cross-Price Elasticity

$$E_{x,y} = \frac{\text{Percentage change in quantity demanded of good x}}{\text{Percentage change in price of good y}} = \frac{\Delta Q_x/Q_x}{\Delta P_y/P_y}$$

Price Elasticity of Demand

$$E = \frac{\text{Percentage change in quantity demanded}}{\text{Percentage change in price}} = \frac{\Delta Q/Q}{\Delta P/P'}$$

- $\cdot \quad \Delta \ (ext{delta}) \ ext{ indicates a change in a variable}$
- \cdot ΔQ refers to a change in a quantity demanded
- ΔP refers to a change in price

Table classifying values of price elasticity of demand

| Value of price elasticity of demand, $arepsilon$ | Description of demand | Interpretation |
|--|-----------------------|--|
| 0 | Perfectly inelastic | Quantity demanded does not change at all with price. |
| From 0 to −1 | Inelastic | Quantity demanded is relatively unresponsive to price changes. |
| -1 | Unit elastic | Percentage change in quantity demanded is equal to percentage change in price. |
| From -1 to - | Elastic | Quantity demanded is relatively responsive to price changes. |
| - | Perfectly elastic | Quantity demanded goes to zero with any increase in price and goes to infinity with any decrease in price. |

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CHAPTER 6

Firms and Their Production Decisions

THE POLICY QUESTION

IS INTRODUCING TECHNOLOGY IN THE CLASSROOM THE BEST WAY TO IMPROVE EDUCATION?

In <u>chapter 5</u>, we covered individual and market demand. We now turn to the supply side of the market—where the goods and services that are offered for sale in markets come from. A *good* is a physical product like a candy bar or a car, while a *service* is a task, like an accountant doing your taxes or a hair-dresser cutting your hair. In economics, we say that all goods and services come from firms. **Firm** is a term that describes any entity that produces a good or service for sale in a market. Thus, a firm can be a mammoth conglomerate like General Electric that makes everything from kitchen appliances to advanced medical equipment to jet engines. Or a firm can be an eleven-year-old child selling lemonade on the street corner.

Our goal in this section is to understand where supply curves come from and what influences their shape and movement. We can then make reasonable predictions about how changes in production affect the price and sales of goods and services.

When we understand and are able to describe supply curves, we can match them up to the demand curves and talk about markets and market outcomes in section 6.3.

EXPLORING THE POLICY QUESTION

Reform efforts are common in the history of public education in the United States. The Bush administration's No Child Left Behind Act and the Obama administration's Race to the Top initiative are examples of broad efforts to reform education. Yet despite these and many other efforts in recent decades, the United States still does relatively poorly in rankings of educational outcomes.

This suggests that policy makers need to better understand how knowledge is acquired and transmitted in a group setting. The following are important questions that need to be answered in order to make an effective policy:

- How important is the training of teachers, and what types of training are most effective?
- How important is caring for the health and well-being of students, and what are the best ways of doing so?
- How important are good textbooks, and what makes a textbook good?
- Does the quality of school infrastructure matter?
- Is it important to have computers integrated into learning in the twenty-first century?

These are all part of what an economist would describe as the education production function: the set of inputs (teachers, students, supplies, and infrastructure) that are combined by education systems to produce an output, educated children. This chapter explains production functions in economics and will give us some guidance in thinking about the education production function that we might use to guide and shape education policy.

LEARNING OBJECTIVES

6.1 Inputs

Learning Objective 6.1: Identify the four basic categories of inputs in production and give examples of each.

6.2 Production Functions, Inputs, and Short and Long Runs

Learning Objective 6.2: Explain the concept of production functions, the difference between fixed and variable inputs, and the difference between the economic short run and long run.

6.3 Production Functions and Characteristics in the Short Run

Learning Objective 6.3: Explain the concepts of the marginal product of labor, the total product of labor, the average product of labor, and the law of diminishing marginal returns.

6.4 Production Functions in the Long Run

Learning Objective 6.4: Describe and illustrate isoquants generally and for Cobb-Douglas, perfect complements (fixed proportions), and perfect substitutes.

6.5 Returns to Scale

Learning Objective 6.5: Define the three categories of returns to scale and describe how to identify them.

6.6 Technological Change and Productivity Growth

Learning Objective 6.6: Discuss technological change and productivity increases and how they affect production functions.

6.7 The Policy Question

Is Introducing Technology in the Classroom the Best Way to Improve Education?

Learning Objective 6.7: Use a production function to model the process of learning in education.

6.1 INPUTS

Learning Objective 6.1: Identify the four basic categories of inputs in production, and give examples of each

Previously, we distilled the essence of consumers to a utility function that describes their preferences and is used to choose a consumption bundle among many possible alternatives. In this chapter, we are

going to do something very similar with producers, boiling down their real-world complexity to the very essence of their function.

Another term for a producer is firm. The most basic definition of a firm is an entity that combines a set of inputs to produce a good or service for sale in a market. There are four basic categories of inputs that describe most of the potential inputs used in any production process:

1. Labor (L)

This category of input encompasses physical labor as well as intellectual labor. It includes less skilled or manual labor, managerial labor, and skilled labor (engineers, scientists, lawyers, etc.)—the *human* element that goes into the production of a good or service.

2. Capital (K)

This input category describes all the machines that are used in production, such as conveyor belts, robots, and computers. It also describes the buildings, such as factories, stores, and offices, and other non-human elements of production, such as delivery trucks.

3. **Land** (*N*)

Some goods, most notably agricultural goods, need land to produce. Fields that grow crops and forests that grow trees for lumber and pulp for paper are examples of the land input in production.

4. Materials (M)

This input category describes all the raw materials (trees, ore, wheat, oil, etc.) or intermediate products (lumber, rolled aluminum, flour, plastic, etc.) used in the production of the final good. Note that one firm's final good, like aluminum, is often another firm's input.

Not all firms use all the inputs. For example, a child who runs a lemonade stand uses labor (the time cutting, squeezing, mixing, and selling), capital (the knife to cut, the juicer to juice, and the pitcher to hold the lemonade), and materials (lemons, water, and sugar). This young entrepreneur does not use land, though the producer of the lemons does.

The providers of services use inputs as well. An accountant, for example, might use labor, a computer (capital), office supplies (materials), and so on.

6.2 PRODUCTION FUNCTIONS, INPUTS, AND SHORT AND LONG RUNS

Learning Objective 6.2: Explain the concept of production functions, the difference between fixed and variable inputs, and the difference between the economic short run and long run.

The way inputs are combined to produce an output is called the firm's technology or production process. We describe the production process with a **production function**: a mathematical expression of the maximum output that results from a specific amount of each input.

Let's start with the very simple example of our lemonade stand. Suppose for each cup of lemonade the child can sell, it takes exactly one lemon, two cups of water, one tablespoon of sugar, and ten minutes

of labor, including the making and the selling of the beverage. A production function that describes this process would look something like this:

Cups of Lemonade =
$$f(lemons, sugar, water, labor time)$$

where f stands for some functional form. For the moment, we are not describing the actual function but that these inputs are what go into the production of lemonade. A more generic description of a production function would look like this:

$$Output, Q = f(L, K, M, N)$$

Similar to the way we simplified the consumer choice problem, we will generally use two input production functions to keep the problem simple and tractable. By convention, we typically use labor (L) and capital (K) as the two inputs, and so the generic production function is

$$Q = f(L, K)$$
.

When we put in actual amounts for labor and capital, this function tells us the maximum output that can be achieved with the two amounts. Producing less than that output is possible, but we will soon find that firms that are trying to maximize profits or minimize costs would never produce less than the full amount of something that they can sell for a positive price. Said another way, if a firm has a specific output in mind, it has no interest in using more than the minimum amounts of inputs.

Producing a good or service for the market requires firms to make choices about the type and number of inputs to use. As we will see, this choice depends critically on the contribution the input makes to the final output relative to its cost. But a firm can only make choices about inputs that are variable: inputs whose quantities can be adjusted by the firm. In shorter time periods, some inputs are not variable but fixed: the firm cannot adjust these quantities.

Consider a firm that produces tablet computers for use in classrooms using an assembly line. A conveyor belt (capital) carries the computers in various stages of construction past stations where the next part is added by a worker (labor). The firm might decide that it wants to expand production and add a second conveyor belt, but it takes time to expand the factory, build the belt, and get it operational. In this case, capital (the conveyor belt) is a **fixed input**—an input than cannot be adjusted by the firm in a given time period. If the firm wants to increase production for the time being, it will have to adjust labor, a variable input—an input that can be adjusted by the firm in a given time period.

Given enough time, this firm could add the second conveyor belt and increase production on its new level of capital. This concept is how we define short run and long run in economics: the **short run** is a period of time in which some inputs are fixed, and the **long run** is a period of time long enough that all inputs can be adjusted. It is important to note that these are not defined by any objective period of time (day, month, year, etc.) but are specific to the particular firm and its particular inputs.

Suppose our tablet computer manufacturer needs three months to install a second assembly line—that is, its short run is less than three months, and its long run is three months or more. For our lemonade salesperson, it might take an hour-long trip to the store to buy a new juicer or pitcher. In this case, the short run is less than an hour, and the long run is an hour or more.

6.3 PRODUCTION FUNCTIONS AND CHARACTERISTICS IN THE SHORT RUN

Learning Objective 6.3: Explain the concepts of the marginal product of labor, the total product of labor, the average product of labor, and the law of diminishing marginal returns.

The short run, as was just described, is a period short enough that at least one input is fixed. We will follow the convention that the capital (K) input is fixed in the short run and labor is variable. This assumption is not always true, but labor hours often can be adjusted quickly—for example, by having workers

put in a little overtime—and capital inputs generally take some time to adjust. To describe the short run using our production function, we write it like this:

$$Q = f(L, \overline{K})$$

where Q is the quantity of the output, L is the quantity of the labor (generally measured in labor hours), and K is the quantity of capital (generally measured in capital hours). The bar over the capital variable indicates that it is fixed: \overline{K} .

Let's go back to our computer manufacturer. In the short run, the firm cannot add capital in the form of a new assembly line. But it can add workers. It could, for example, add a second shift to production, using the same assembly line through the night. Or if already running twenty-four hours, the firm could add more workers to the same assembly line and squeeze more production out of it.

The relationship between the amount of the variable input used and the amount of output produced (given a level of the fixed input) is the *total product*, or in this case the **total product of labor** (Q), as labor is the variable input. **Table 6.1** summarizes this information for our tablet computer manufacturer along with some additional information, which we will discuss.

Table 6.1 Input, Output, Marginal Product, and Average Product

| Capital, <mark>Formula does not parse</mark> | Labor, L (number of workers on the tablet assembly line) | Output, total product of labor, Q (number of tablets assembled) | Marginal product of labor, MP_{L} (number of additional tablets assembled with the addition of one worker to the line) | Average product of labor, AP_L (average number of tablets assembled per worker) | |
|---|--|--|--|---|--|
| 1 | 0 | 0 | _ | _ | |
| 1 | 1 | 6 | 6 | 6 | |
| 1 | 2 | 20 | 14 | 10 | |
| 1 | 3 | 44 | 24 | 14.7 | |
| 1 | 4 | 60 | 15 | 15 | |
| 1 | 5 | 70 | 10 | 14 | |
| 1 | 6 | 78 | 8 | 13 | |
| 1 | 7 | 84 | 6 | 12 | |
| 1 | 8 | 88 | 4 | 11 | |
| 1 | 9 | 86 | -2 | 9.6 | |
| 1 | 10 | 80 | -6 | 8 | |

As the number of workers (labor) increases incrementally by one in **table 6.1**, the output also increases. Note that at first, increases in production are pretty big. This is due to the efficiencies from increased specialization made possible by more workers. After a while, the increases in output from increased labor get smaller and smaller as the assembly line gets crowded and the additional workers have difficulty being as productive. The maximum number of workers is reached at ten due to the firm being unable to fit more workers on the assembly line.

The extra contribution to output of each worker is critically important to the firm's decision about how many workers to employ. The extra output achieved from the addition of a single unit of labor is the **marginal product of labor** (MP_L). In our case, the extra unit is an additional worker, but in general, we might measure units as worker hours. MP_L is a key measure listed in the fifth column of **table 6.1**. Formally, it is

$$MP_L = rac{\Delta Q}{\Delta L}$$

Table 6.1 shows that this marginal product increases at first as we add more workers, peaks at five workers, but then starts to decline and even goes negative as we reach ten workers.

Calculus

$$MP_L = rac{\partial Q}{\partial L}$$

Note that we use the partial derivative here even though it is a univariate function in the short run, because in general, it is a bivariate function.

Also important to keep track of is the average product of labor (AP_L) , or how much output per worker is being produced at each level of employment:

$$AP_L = rac{Q}{L}$$

In **table 6.1**, we see that the average product of labor increases at first, peaks at five workers, but then starts to decline.

These measures of labor productivity can also be represented as curves. We will draw them as smooth continuous curves because we can hire fractional workers in the sense that we could hire one full-time employee and another who works 60 percent of the time, and so on.

In **figure 6.1**, we represent the total product of labor curve in the upper panel and the marginal and average product of labor curves in the lower panel.

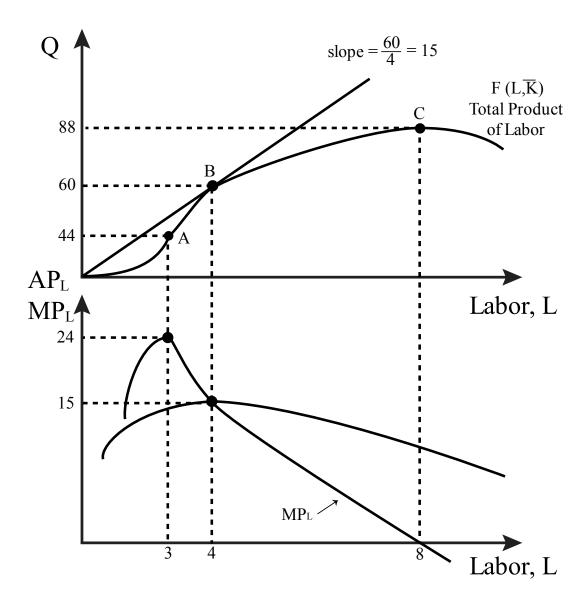


Figure 6.1 Short-run total product curve and average and marginal product curves

The shape of the total product of labor curve confirms that, at first, adding workers allows more specialization and more output per worker. This can be seen in the initial part of the curve where the slope is getting steeper. Then given the fact that the capital is fixed, adding more workers continues to increase output but at a decreasing rate. We see this past point A on the graph, where the slope is still positive but decreasing. Finally, more workers actually cause output to fall.

From the total product of labor graph, we can actually measure the average and marginal product of labor. The average product of labor is the same as the slope of the ray from the origin that intersects the total product curve (note that the slope's rise/run is output/labor). This reaches its highest slope right at point B, where the ray is just touching the total product curve. The marginal product of labor curve is the change in output over the change in labor, which is the same as the slope of the total product curve itself. Notice that the maximum slope is right at point A so that the average and the marginal are *exactly the same* at point B and that the slope turns negative at point C—the point of maximum output. These observations can help us draw the average and marginal product curves in the lower panel. We know marginal product reaches a maximum at A, crosses the average product curve at B, and turns negative

at C. We also know that when the marginal product is above the average, the average is increasing, and when the marginal product is below the average, the average is decreasing. Thus the two sets of curves relate directly to each other.

There is one more important characteristic of production to note before we move on: **the law of diminishing marginal returns**. This "law" states that if a firm increases one input while holding all others constant, the marginal product of the input will start to get smaller, just like in our example at three labor units. It is important to remember that we are talking about the *marginal* returns here—that the additional output will be *positive* but smaller and smaller. We can also talk about diminishing returns—what happens to total output as labor is increased, which in our case does eventually diminish (at nine labor units), but this is not a general rule.

6.4 PRODUCTION FUNCTIONS IN THE LONG RUN

Learning Objective 6.4: Describe and illustrate isoquants generally and for Cobb-Douglas, perfect complements (fixed proportions), and perfect substitutes.

In the long run, all production inputs are variable. Because of this, firms have more flexibility in how they choose to produce, expand, and contract their output in the long run than in the short run. But this situation also complicates firms' decision-making. They have to weigh the marginal contribution to output an extra unit of each input would provide and the cost of that extra unit. We will now focus on this decision process.

Since we have simplified our firm to one that uses only two inputs, capital (K) and labor (L), we have a choice problem that shares many similarities with the consumers' problem we studied in section 6.1. It should come as no surprise then that the way we solve the problem is similar as well. Let's start with the production function.

$$Q = f(L, K)$$

Note that there is no bar above the K, meaning that both labor and capital are now variable. This makes the function mathematically similar to the **utility function** from <u>chapter 2</u>. The graph of these two variable functions is three-dimensional.

| | Labor (L) | | | | | |
|-------------|-----------|-----|-----|-----|-----|--|
| Capital (K) | 1 | 2 | 3 | 4 | 5 | |
| 1 | 100 | 180 | 250 | 300 | 340 | |
| 2 | 180 | 300 | 380 | 440 | 500 | |
| 3 | 250 | 380 | 500 | 560 | 600 | |
| 4 | 300 | 440 | 560 | 650 | 680 | |
| 5 | 340 | 500 | 600 | 680 | 740 | |

Table 6.2 Output from the use of two variable inputs, capital (K) and labor (L)

From **table 6.2**, we can see the diminishing marginal productivity of one variable input. Holding one input constant—for example, holding capital at three—we can see that the increase in the total output falls as we increase labor. The extra output from going from one unit of labor to two is 130 (380 - 250), from two to three is 120, from three to four is 60, and from four to five is 40.

Like indifference curves for utility functions, we can visualize this output function in two dimensions by drawing contour lines: lines that connect all combinations of labor and capital that lead to an identical output. To draw one, we can start by arbitrarily choosing an output level and then finding all the combinations of labor and capital the firm could possibly use to produce this quantity:

$$\overline{Q} = f(L, K)$$

Drawing this on a graph with capital on the vertical axis and labor on the horizontal axis produces an **isoquant**: a curve that shows all the possible combinations of inputs that produce the same output. *Iso* means "the same" and *quant* means "quantity." So an isoquant is a curve that for every point on it, the output quantity is the same.

Figure 6.2 shows three isoquants for **table 6.2**, corresponding to the outputs 180, 300, and 500. In the figure, the combinations of inputs that yield the same output are connected by a smooth curve. We draw them as smooth curves to illustrate that firms can use any fraction of a unit of input they desire.

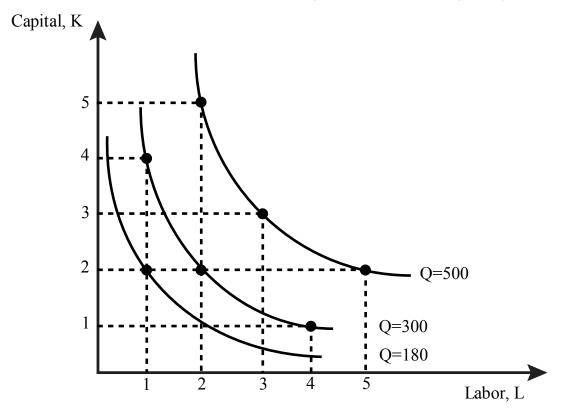


Figure 6.2 Selected isoquants from table 6.2

You can, of course, do this for any output level you choose so the entire space is filled with potential isoquants; **figure 6.2** simply sketches three. Note that we do not have a specific functional form for the production function, so we are drawing hypothetical isoquants. We will derive an isoquant from a specific production function momentarily.

Properties of Isoquants

Just like indifference curves, isoquants have properties that we can characterize.

- 1. Isoquants that represent greater output are farther from the origin.
 - Quite simply, if you add more of both inputs, you get more output. Stated the other way, if you want more output, you have to increase the inputs.
- 2. Isoquants do not cross each other.

To understand this, try a thought experiment. If two isoquants crossed, it would mean that at the crossing point, the same inputs would yield two different and distinct output levels. Under the assumption that firms make efficient decisions, they would never produce a lower output.

3. Isoquants are downward sloping.

This is the same as saying there are trade-offs with inputs: you can replace some capital with labor and produce the same amount of output and vice versa. Really this requirement is only a prohibition on upward-sloping isoquants, which would imply that you could cut back on both inputs and produce the same output.

4. Isoquants do not bow out.

This is a similar property to the one for indifference curves, which are bowed in. Note that we do not say that isoquants can only be bowed in because perfect complements and substitutes play a big role in production functions. But isoquants that curve in represent the idea that it is often more efficient to have a mix of labor and capital working together than too much of one or the other (this is quite similar to the desire-for-variety motive in consumption).

Three Types of Production Functions and Their Related Isoquants

As with preferences, there are three basic types of production functions. Though they are essentially the same as the three indifference curves that represent the three basic types of preferences, it is good to keep in mind that the context is very different. Depending on the production process, inputs into the production process could be easily substitutable, might need to be used in fixed proportions, or might be mixed together but have flexibility in terms of proportions.

Perfect Substitute Production Functions

Some production processes can substitute one input for another in a fixed ratio. For example, our lemonade-selling child might have an electric juicer that will transform whole lemons into lemonade without any human input. This child might also be able to make lemonade entirely by hand.

Suppose the juicer can always make one gallon of lemonade in half an hour and the child can always make one gallon in one hour. Thus the production function for the quantity of lemonade (Q) given labor (L) and capital (K) looks like this:

$$Q = L + 2K$$

To see this, think in terms of an isoquant: producing exactly one gallon of lemonade (Q=1) requires either one hour of labor (L) or $\frac{1}{2}$ hour of capital, the juicer (K). You can also mix inputs—for example, you could use $\frac{1}{2}$ hour of labor and $\frac{1}{4}$ hour of capital. To produce two gallons (Q=2), you could use

two hours of labor or one hour of capital. You could also mix and use one hour of labor and $\frac{1}{2}$ hour of capital or any linear combination of the two inputs.

Isoquants for a perfect substitute production function are therefore straight lines. Figure 6.3 presents three isoquants for a production function, Q=L+K.

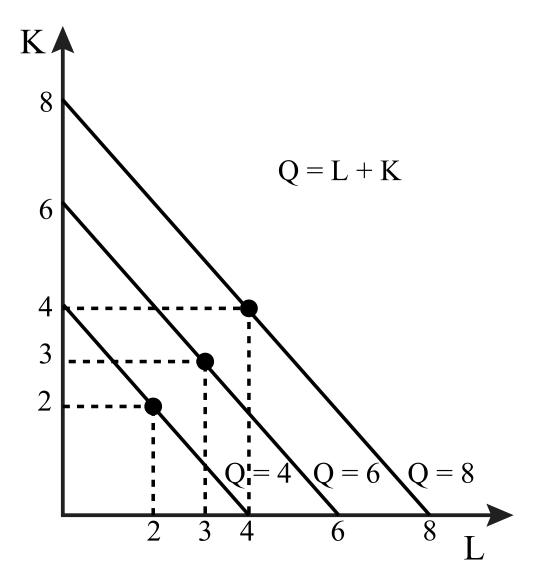


Figure 6.3 Isoquants for a production function with inputs that are perfect substitutes

Perfect substitute production functions generally have the form

$$Q = aL + \beta K$$
,

where α and β are positive constants. A more general form of this production function that incorporates a measure of overall productivity is this:

$$Q = A(aL + \beta K)$$
,

where A is also a positive constant. Careful observers will notice that the A is unnecessary because it can be incorporated into α and β , but expressing the production function this way provides an easy

method of adjusting for (and empirically estimating) productivity. We will examine A and productivity in more detail in section 6.6.

Perfect Complement (Fixed-Proportions) Production Functions

If inputs have to be used in fixed proportions, then we have a fixed-proportions production function where the inputs are perfect complements, also known as a *fixed-proportions production function*. Imagine a metal-stamping business where the business takes metal sheets from its clients and stamps them into shapes, such as auto body parts. Suppose the stamping machines require exactly one operator. Without a full-time operator, the machine will not work. Without a machine, a worker cannot stamp the metal sheet. Thus the inputs are perfect complements—they have to be applied in fixed proportions to get any extra output. Suppose also that one machine and one worker can produce one hundred stamped panels in a day.

A production function that describes the daily output of the metal-stamping business looks like this:

$$Q=100^*min[L,K]$$
,

where the min function simply takes the smaller of the two values of the arguments L and K. For example, if the business has ten workers (L) and eight machines (K), the value of the function, Q, would be eight times one hundred, or eight hundred. Similarly, if the business has twelve machines but only seven workers, the daily output would be seven hundred.

We can draw the isoquants for this firm starting with equal inputs. At point A, there are five machines and five workers, and the daily output is five hundred. Now suppose we move to point B, where there are still five machines and seven workers. Does this yield any more output? No. So this point is on the same indifference curve. This is similar to point C, where there are seven machines and five workers.

Perfect complement production functions have the general functional form of

$$Q=A^*min[lpha L,eta K]$$
 ,

where A, α , and β are positive constants. As in the case of perfect substitutes, the A is unnecessary because it can be incorporated into α and β , but we will keep it for simplicity and clarity.

Figure 6.4 presents three isoquants for the production function Q=min[L,K].

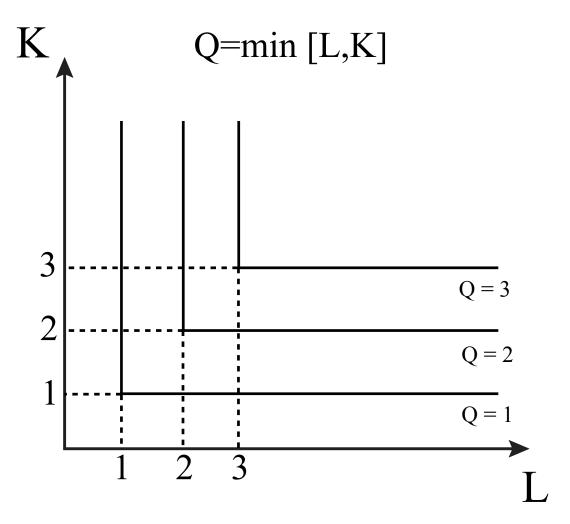


Figure 6.4 Isoquants for a production function with inputs that are perfect complements

Cobb-Douglas Production Functions

Perfect substitute and fixed-proportion production functions are special cases of a more general production function that describes inputs as imperfect substitutes for each other. In other words, we can get rid of some machines (capital) in exchange for more workers (labor) but at a ratio that changes depending on the current mix of workers and machines. The Cobb-Douglas function that we used to describe consumer choice with the **preference for variety assumption** is used for just such a production process.

An example of a Cobb-Douglas production function is

$$Q = AL^{\alpha}K^{\beta}$$

where A, α , and β are positive constants. Notice that A represents overall productivity (as A increases, the same number of inputs yields more output), and the α and β parameters represent the contribution to the output of each input. In other words, the higher the level of α , the more one unit of capital will produce in extra output, and likewise for β , labor. The essential aspect of this production function is always having the ability to substitute one input for the other and maintain the same level of output.

From this production function, we can study the substitutability of inputs into production. In order to do this, we need to define the marginal rate of technical substitution, which is similar to the marginal rate of substitution from consumer theory. The **marginal rate of technical substitution (MRTS)** describes how much you must increase one input if you decrease the other input by one unit in order to produce the same output. The MRTS is simply the ratio of the marginal product of labor to the marginal product of capital:

$$MRTS = -rac{MP_L}{MP_K}$$

To see where this ratio comes from, remember that the marginal product of an input tells us how much extra output will result from a one-unit increase in the input. Earlier we defined the marginal product of labor as

$$MP_L = \Delta Q/\Delta L$$

Similarly for capital, we have

$$MP_K = \Delta Q/\Delta K$$

Note that we can rearrange the marginal product of labor and express it as

$$\Delta Q = M P_L^* \Delta L$$

So if the MP_L is four and the firm increases labor by one unit, then the extra output is four.

Similarly, if the MP_K is two and the firm decreases capital by one unit, then the decline in output is two, or

$$\Delta Q = MP_K^* \Delta K.$$

Notice that in order to stay on the same isoquant, the net change in output has to be zero, or

$$(MP_L^*\Delta L) + (MP_K^*\Delta K) = 0.$$

Rearranging the steps, we get the following:

$$-(MP_L^*\Delta L) = (MP_K^*\Delta K)$$

which we can simplify to give us:

$$-rac{MP_L}{MP_K} = rac{\Delta K}{\Delta L} = MRTS$$

Note that the MRTS describes the slope of the isoquant—how many units of capital you would need to add (rise) if the labor decreases by one unit (run) to maintain the same output (stay on the isoquant).

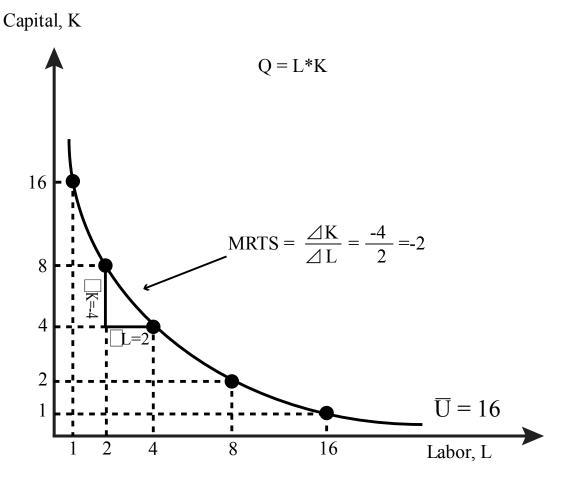


Figure 6.5 Isoquant with marginal rate of technical substitution (MRTS)

Now let's return to the Cobb-Douglas utility function, $Q=AL^{\alpha}K^{\beta}$, and derive the MRTS. Since the parameters α and β are positive constants that describe the contribution of each input to the final output, they are related to the marginal products. It turns out that the marginal product of labor is just α times the average product of labor:

$$MP_L = aAP_L = aQ/L$$

And the marginal product of capital is just β times the marginal product of capital:

Since
$$MRTS=-rac{MP_L}{MP_K}$$
 and $MP_L=rac{\partial Q}{\partial L}$ and $MP_K=rac{\partial Q}{\partial K}$, then $MRTS=-rac{\partial Q}{rac{\partial L}{\partial K}}$, or $MRTS=-rac{\partial K}{\partial L}$

$$MP_K = aAP_K = aQ/K$$

Thus for the MRTS, we have

$$-rac{MP_L}{MP_K} = -rac{aQ/L}{eta Q/K} = -rac{lpha}{eta}rac{K}{L}.$$

Notice the absence of A in this ratio. Since we are talking about marginal returns to inputs and A only affects total return, it does not appear in this calculation.

Calculus

With
$$MP_L=rac{\partial Q}{\partial L}$$
 and $Q=AK^{lpha}B^{eta}$, $MPL=(lpha K^{lpha-1})L^{eta}$. Similarly, $MP_K=AK^{lpha}(eta L^{eta-1})$. Thus, $MRTS=-rac{rac{\partial Q}{\partial L}}{rac{\partial Q}{\partial K}}=-rac{AK^{lpha}(eta L^{eta-1})}{A(lpha K^{lpha-1})}rac{L^{eta-1}}{L^{eta}}=-rac{lpha}{eta}rac{K}{L}$

Let's look at an example of a specific production function. Suppose a firm's production function is estimated to be

$$Q = 3.7L^{.45}K^3$$

In this case, A=3.7, α = .45, and β = .3. Thus the MRTS for this production function is

$$MRTS = -rac{MP_L}{MP_K} = -rac{lpha}{eta}rac{K}{L} = -rac{.45}{.3}rac{K}{L} = -1.5rac{K}{L}.$$

So the slope of this firm's isoquant depends on the specific mix of capital (K) and labor (L) but is -1.5(K/L). Note that when K is relatively large and L is relatively small (as in point [1, 16] in **figure 6.5**), the slope is negative and steep. Alternatively, when K is relatively small and L is relatively large, the slope is negative and shallow. The slope is also always changing along the isoquant, and thus we have the "bowed-in" shape (concave to the origin) typical to the Cobb-Douglas production function.

6.5 RETURNS TO SCALE

Learning Objective 6.5: Define the three categories of returns to scale, and describe how to identify them.

Up to now, our focus on marginal returns has centered on the change of one input, holding the other input constant. In this section, we consider what happens to output when we increase or decrease *both* inputs. Increasing or decreasing both inputs can be described as scaling the firm up or down, and we want to know how it affects output. In particular, we would like to know about proportional changes to output. For example, if the firm doubles both inputs, does output double as well? Does it increase more or less than double the previous amount? The answer to these questions determines the **returns to scale** of the firm: the rate at which the output increases when all inputs are increased proportionally.

Constant Returns to Scale (CRS)

If a firm's output changes in exact proportion to changes in the inputs, we say the firm exhibits constant returns to scale (CRS). Let's consider this situation using the doubling example.

Suppose a firm has a production function of

$$Q = f(L, K)$$
.

Now the firm doubles its inputs. We can show this by multiplying the current inputs by two:

If this yields exactly double the output, we can write this expression as

$$f(2L,2K) = 2f(L,K) = 2Q.$$

This expression says that if both inputs double, output doubles. It is an example of a CRS production function. The CRS condition can be expressed more generally as

$$f(\Phi L, \Phi K) = \Phi f(L, K) = \Phi Q$$

where Φ is a strictly positive constant, like two in our example. In the case of scaling down, Φ would be a fraction, such as $\frac{1}{2}$.

Increasing Returns to Scale (IRS)

Increasing returns to scale (IRS) production functions are those for which the output increases or decreases by a *greater* percentage than the percentage increase or decrease in inputs. In the case of doubling inputs, the IRS expression would look like this:

$$f(2L,2K)>2f(L,K)=2Q$$

Look carefully at what this says. The first term on the left is the output that results from the doubling of the two inputs. We compare this to the doubling of the output, represented by the two expressions on the right of the inequality sign. This expression says that you get more output from doubling the inputs than you get from doubling the output—or that if you double the inputs, you get more than double the output. In general terms,

$$f(\Phi L, \Phi K) > \Phi f(L, K) = \Phi Q$$

again where Φ is a strictly positive constant.

Decreasing Returns to Scale (DRS)

Finally, **decreasing returns to scale (DRS)** production functions are those for which the output increases or decreases by a *smaller* percentage than the increase or decrease in inputs. In the case of doubling the inputs, the DRS expression would look like this:

$$f(2L,2K) < 2f(L,K) = 2Q$$

This expression says that you get less output from doubling the inputs than you get from doubling the output—or that if you double the inputs, you get less than double the output. In general terms,

$$f(\Phi L, \Phi K) < \Phi f(L, K) = \Phi Q$$

again where Φ is a strictly positive constant.

Varying Returns to Scale

Some production processes have varying returns to scale. The most common is where there are increasing returns to scale for small output levels, constant returns for medium output levels, and decreasing for very large output levels.

Returns to Scale and Production Functions

Let's think about the three types of production functions we have studied—perfect substitutes, perfect complements, and Cobb-Douglas—and their returns to scale. The question we want to answer can be expressed as, If the amounts of inputs are doubled, by how much does the output increase? The answer will tell us if the production function exhibits constant, increasing, or decreasing returns to scale.

Perfect Substitutes

Recall the expression for perfect substitutes:

$$Q = \alpha L + \beta K$$

Here we double both inputs, so we replace L and K with 2L and 2K:

$$\alpha 2L + \beta 2K = 2Q$$

By simple algebra, we can factor out the common two and come up with

$$2(\alpha L + \beta K) = 2Q.$$

By the above equation, we know that the term in the parentheses is equal to Q. So we know that by doubling both L and K, we exactly double Q, or we have constant returns to scale. This means that production functions for perfect substitutes are CRS.

Perfect Complements

The perfect complement function is

$$Q = A^*min[\alpha L, \beta K].$$

Again, we want to begin by replacing L and K with 2L and 2K and note that since we are doubling both inputs, the minimum of the two numbers must also be doubled so we can pull the two out in front of the min:

$$Amin[\alpha 2L, \beta 2K] = A2min[\alpha L, \beta K]$$

Since the order of multiplication does not matter, we know

$$A2min[\alpha L, eta K] = 2A^*[\alpha L, eta K]$$
,

which is the same as doubling output:

$$2A^*min[lpha L,eta K]=2Q$$

The first step is not immediately obvious, but think about the way the min function works: it just picks the smaller of the two numbers in the square brackets. Doubling them both does not change which one is smaller, and in the end, the value is just double the smaller one, so it is the same as doubling *after* we choose the min of the two numbers. From there, since order doesn't matter in multiplication, we can move the two out in front of the A, and now we have two multiplied by the original production functions (in parentheses), which is the same as Q. Again, we know that by doubling both L and K, we *exactly* double Q, or we have constant returns to scale. Thus production functions for perfect complements are also CRS.

Cobb-Douglas

Recall the Cobb-Douglas function:

$$Q = AL^{\alpha}K^{\beta}$$

We will start the same way, replacing L and K with 2L and 2K:

$$A(2L)^{lpha}(2K)^{eta}$$

You have to be careful here because the exponents α and β are on L and K, respectively, and when we replace L with 2L, for example, the α is now the exponent for 2L. By the rules of exponents, we can separate the 2s and the L and K:

$$A2^{lpha}L^{lpha}2^{eta}K^{eta}$$

Next, we can rearrange terms at will, as the order of operations does not matter in multiplication:

$$2^{\alpha}2^{\beta}AL^{\alpha}K^{\beta}$$

We can also, by the rules of exponents, express $2^{\alpha}2^{\beta}$ as $2^{\alpha+\beta}$:

$$(2^{lpha+eta}(AL^{lpha}K^{ar{eta}})= 2^{lpha+eta}Q^{-1}$$

Now we have an expression with Q and can evaluate the returns to scale. We do so by considering the three possibilities for the exponent $\alpha+\beta$:

1.
$$\alpha + \beta = 1$$
.

Any number to the power of one is itself, so $2^1 \equiv 2$. So in this case, we have *exactly* double the output, and the production function is CRS.

2.
$$\alpha + \beta < 1$$
.

In this case, we have some number less than two multiplied by Q, and so we will have something *less than* double the output. That is, the production function exhibits decreasing returns to scale (DRS).

3.
$$\alpha + \beta > 1$$
.

In this case, ${\cal Q}$ is multiplied by a number larger than two, so the output is *more* than double. That is, the production function exhibits increasing returns to scale (IRS).

So for Cobb-Douglas production functions, the returns to scale depend on the sum of the exponents: if they equal one, they are CRS; if they are less than one, they are DRS; and if they are more than one, they are IRS.

Returns to Scale and Isoquants

We can see returns to scale in isoquants by examining how much they increase with input increases for a particular production function. For example, in **figure 6.6(a)**, when we double inputs from ten to twenty, we double output from one hundred to two hundred. Since output increases at the same rate as inputs, we know it is CRS.

The isoquants in **figure 6.6(b)** illustrate increasing returns to scale. When we double inputs from 10 to 20, we increase output by more than double the original quantity, from 100 to 235.

The isoquants in **figure 6.6(c)** illustrate decreasing returns to scale. When we double inputs from 10 to 20, we increase output by less than double the original quantity, from 100 to 160.

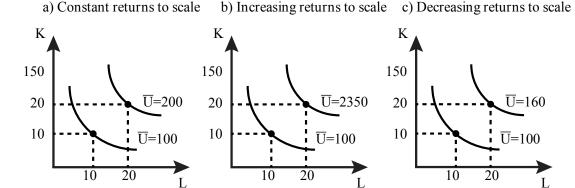


Figure 6.6 Isoquants and returns to scale

6.6 TECHNOLOGICAL CHANGE AND PRODUCTIVITY GROWTH

Learning Objective 6.6: Discuss technological change and productivity increases and how they affect production functions.

A firm's production function need not be static over time. Many firms adopt new technologies or new ways of organizing and doing things in order to become more productive. **Technological change** refers to new production technology or knowledge that changes firms' production functions so that more output is produced by the same amount of inputs. Technological change is also known as *total factor productivity growth*.

We can express changes in overall productivity with production functions. So far we have assumed that firms are *efficient*, meaning that they do not waste inputs—they use the minimum of inputs necessary to produce a particular output level. You can see this by the way we assume that certain inputs yield specific amounts of output. There is no waste in this scenario. *Productivity*, on the other hand, refers to how much overall output a firm gets from a set amount of inputs. The more a firm produces with the same inputs, the more productive it is.

As was noted in section 6.4, the constant A is a measure of overall productivity in the types of production functions we have been studying. All else equal, increasing A increases the output that a firm produces from a set amount of inputs.

Graphically adjusting A in any of our three production function types relabels our isoquants. As **figure 6.7** shows, when A is increased from one to three in the case of a simple Cobb-Douglas production function, all the outputs associated with the individual isoquants increase by three as well.

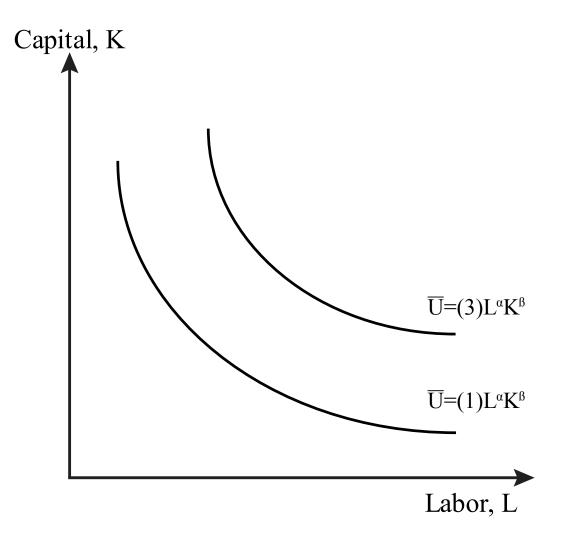


Figure 6.7 Isoquant Cobb-Douglas with outputs increasing

We measure productivity increases by comparing output before and after the productivity change. In the case above, our production function

$$Q=(1)L^{lpha}K^{eta}$$

changed to

$$Q=(3)L^{lpha}K^{eta}$$
 .

The output of the firm thus increased by $\Delta Q/Q$, or $[(3)L^{\alpha}K^{\beta}-(1)L^{\alpha}K^{\beta}]/(1)L^{\alpha}K^{\beta}$, or two. In percentage terms, output increased by 200 percent.

6.7 THE POLICY EXAMPLE

IS INTRODUCING TECHNOLOGY IN THE CLASSROOM THE BEST WAY TO IMPROVE EDUCATION?

Learning Objective 6.7: Use a production function to model the process of learning in education.

Let's return now to the policy question introduced earlier. One way to think of education is similar to a firm: you take a mix of inputs—students, teachers, books, buildings, pedagogy, and technology—and mix them together and get an output. The output in this case is the education itself—how much the students

learn. If learning is the output and we can identify the inputs, then it is possible to think of education as a type of production that is governed by a production function.

Modeling education as a production function is mechanical and has limitations for sure. The true test of this endeavor is whether we can gain any insight into how student learning is accomplished. We would have to start by coming up with a plausible production function. By far the most flexible—and perhaps the most relevant to education—is the Cobb-Douglas production function, where inputs are imperfectly substitutable.

For example, you don't get any learning without a teacher, but you might be able to substitute some technology-based instruction for some live teaching. This is the essence of the Cobb-Douglas production function. We can express an education production function, apply it to real-world data, and estimate its parameters to find out, for example, how important good teachers are and how substitutable they could be using technology. Doing so will give policy makers a better idea of the most effective ways to spend scarce resources if the ultimate goal of education funding is learning.

For example, suppose we posit that learning is a function of teacher quality, the technology used in the classroom, the quality of the class materials, and the size of the class (number of students per teacher). So we imagine that the learning production function looks something like this:

$$learning = Teacher^{lpha} Technology^{eta} Materials^{\gamma} Class\, Size^{\delta}$$

With the appropriate data, the parameters alpha, beta, gamma, and delta can be measured, giving policy makers an idea about where the highest return on investment is found. In fact, economists have been doing this for quite some time. See <u>Measuring Investment in Education</u>.

EXPLORING THE POLICY QUESTION

- 1. What do you think are the relevant inputs into the learning production function?
- 2. Which type of production function best represents the grade school learning environment?
- 3. If you believe that teachers are easily replaced by online videos, where one hour of online video is exactly equivalent to one hour of live teaching, what type of production function would you use to describe this?
- 4. If there were a magic "learning pill" that students could take and that would, regardless of the current level and mix of inputs, double their learning, how would you express this in a production function?

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

6.1 Inputs

Learning Objective 6.1: Identify the four basic categories of inputs in production and give examples of each.

6.2 Production Functions, Inputs, and Short and Long Runs

<u>Learning Objective 6.2</u>: Explain the concept of production functions, the difference between fixed and variable inputs, and the difference between the economic short run and long run.

6.3 Production Functions and Characteristics in the Short Run

<u>Learning Objective 6.3</u>: Explain the concepts of the marginal product of labor, the total product of labor, the average product of labor, and the law of diminishing marginal returns.

6.4 Production Functions in the Long Run

<u>Learning Objective 6.4</u>: Describe and illustrate isoquants generally and for Cobb-Douglas, perfect complements (fixed proportions), and perfect substitutes.

6.5 Returns to Scale

Learning Objective 6.5: Define the three categories of returns to scale and describe how to identify them.

6.6 Technological Change and Productivity Growth

Learning Objective 6.6: Discuss technological change and productivity increases and how they affect production functions.

6.7 The Policy Question

Is Introducing Technology in the Classroom the Best Way to Improve Education?

Learning Objective 6.7: Use a production function to model the process of learning in education.

LEARN: KEY TOPICS

Terms

Labor (T_i)

Input that encompasses physical labor as well as intellectual labor. Includes less skilled or manual labor, managerial labor, and skilled labor (engineers, scientists, lawyers, etc.) i.e., the human element that goes into the production of a good or service.

Capital (K)

Input category which describes all the machines that are used in production: conveyor belts, robots, and computers. It also describes the buildings, such as factories, stores, offices, and other non-human elements of production, such as delivery trucks.

Land (N)

Input category that encompasses land used for production, i.e., fields that grow crops and forests that grow trees for lumber and pulp for paper.

Materials (M)

All the raw materials (trees, ore, wheat, oil, etc.) or intermediate products (lumber, rolled aluminum, flour, plastic, etc.) used in the production of the final good.

Production function

A mathematical expression of the maximum output that results from a specific amount of each input.

Variable input

An input that can be adjusted by the firm in a given time period.

Fixed input

An input that cannot be adjusted by the firm in a given time period.

Short rur

A period of time in which some inputs are fixed; not defined by any objective period of time (day, month, year, etc.) but are specific to the particular firm and its particular inputs.

Long run

A period of time long enough that all inputs can be adjusted; not defined by any objective period of time (day, month, year, etc.) but are specific to the particular firm and its particular inputs.

Total product of labor (Q)

The relationship between the amount of the variable input used and the amount of output produced (given a level of the fixed input).

Average product of labor (AP_L)

How much output per worker is being produced at each level of employment.

Marginal product of labor (MP_L)

The extra output achieved from the addition of a single unit of labor.

Law of diminishing marginal returns

If a firm increases one input while holding all others constant, the marginal product of the input will start to get smaller. It will still remain positive, just smaller and smaller.

Isoquant

From iso meaning "same" and quant meaning quantity. A curve that shows all the possible combinations of inputs that produce the same output.

Cobb-Douglas production functions

An example:

$$Q=AL^{lpha}K^{eta}$$

A production function that describes a ratio that changes depending on the current mix of workers (labor) and capital (machines, etc). A variant of the **Cobb-Douglas function** that describes consumer choice with the preference for variety assumption.

Perfect substitute production functions

A production function used when two means of production can substitute for one another in a fixed ratio. Generally have the form:

$$Q = aL + \beta K$$

where α and β are positive constants

Perfect complement (fixed-proportions) production functions

A fixed-proportions production function where the inputs are perfect complements:

$$Q = A^*min[\alpha L, \beta K]$$

where A, lpha, and eta are positive constants

Marginal rate of technical substitution (MRTS)

A ration of the marginal product of labor (MP_L) and the marginal product of capital (MP_K)

$$MRTS = -rac{MP_L}{MP_K}$$

Returns to scale

The rate at which the output increases when all inputs are increased proportionally.

Constant returns to scale (CRS)

Exhibited when a firm's output changes in exact proportion to changes in the inputs

$$f(\Phi L, \Phi K) = \Phi f(L, K) = \Phi Q$$

where Φ is a strictly positive constant. Φ becomes fractional in the case of scaling down.

Increasing returns to scale (IRS)

When the *output* increases or decreases by a *greater* percentage than the percentage increase or decrease in *inputs*

$$f(\Phi L, \Phi K) > \Phi f(L, K) = \Phi Q$$

where $\boldsymbol{\Phi}$ is a strictly positive constant.

Decreasing returns to scale (DRS)

When the outputs increases or decreases by a smaller percentage than the percentage increase or decrease in inputs.

$$f(\Phi L, \Phi K) < \Phi f(L, K) = \Phi Q$$

where $\boldsymbol{\Phi}$ is a strictly positive constant.

Graphs

Short-run total product curve and average and marginal product curves

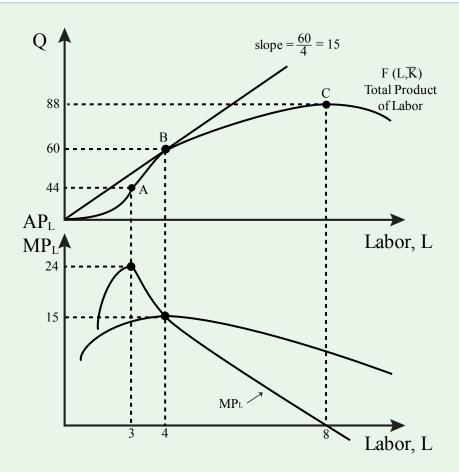


Figure 6.1 Short-run total product curve and average and marginal product curves

Examples of isoquants

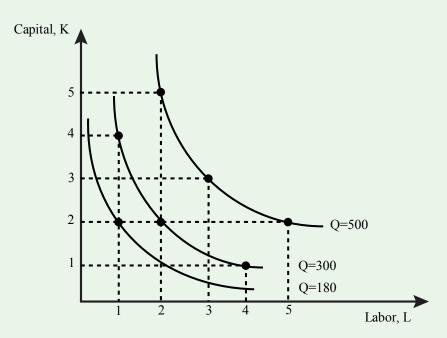


Figure 6.2 Selected isoquants from table 6.2; examples of isoquants

Isoquants for a production function with inputs that are perfect complements

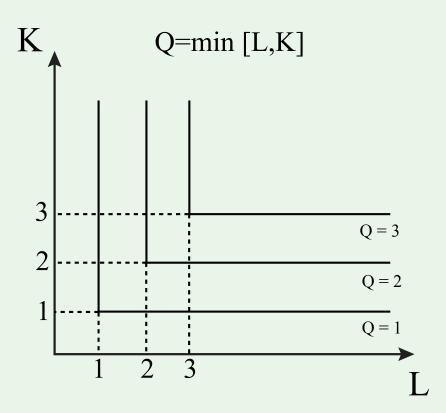


Figure 6.4 Isoquants for a production function with inputs that are perfect complements

Isoquants for a production function with inputs that are perfect substitutes

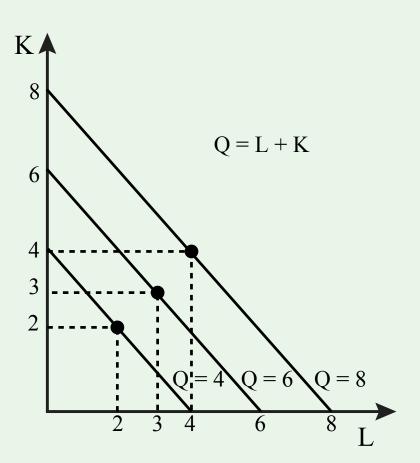


Figure 6.3 Isoquants for a production function with inputs that are perfect substitutes

Isoquant with MRTS

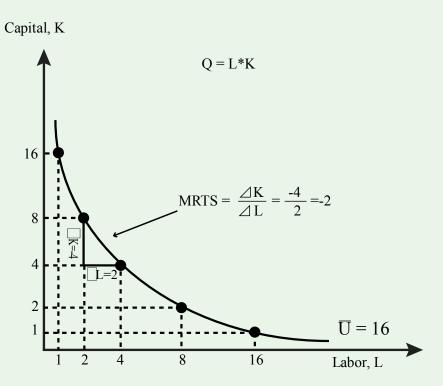


Figure 6.5 Isoquant with marginal rate of technical substitution (MRTS)

Isoquants and returns to scale

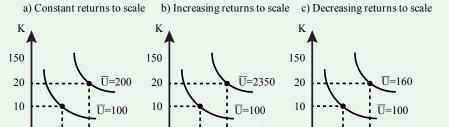


Figure 6.6 Isoquants and returns to scale: a) constant returns (crs), b) increasing returns (irs), c) decreasing returns (drs)

Isoquant Cobb-Douglas with outputs increasing

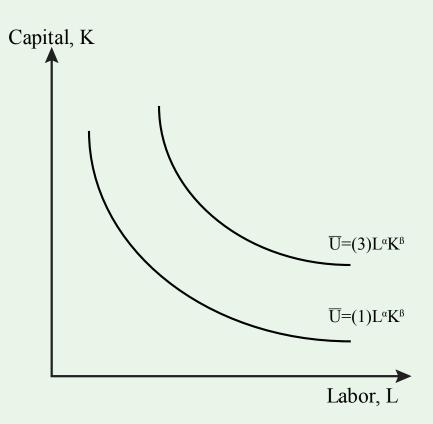


Figure 6.7 Isoquant Cobb-Douglas with outputs increasing

Equations

Average product of labor (AP_L)

$$AP_L = rac{Q}{L}$$

Marginal product of labor (MP_L)

$$MP_L = rac{\Delta Q}{\Delta L}$$

See also:

$$MP_L = rac{\partial Q}{\partial L}$$

The partial derivative is used when working with MP_L , regardless if it is univariate in presentation. In general, it is a bivariate function.

Marginal rate of technical substitution (MRTS)

$$MRTS = -rac{MP_L}{MP_K}$$

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CHAPTER 7

Minimizing Costs

THE POLICY QUESTION

WILL AN INCREASE IN THE MINIMUM WAGE DECREASE EMPLOYMENT?

Recently, a much-discussed policy topic in the United States is the idea of increasing minimum wages as a response to poverty and growing income inequality. There are many questions of debate about minimum wages as an effective policy tool to tackle these problems, but one common criticism of minimum wages is that they increase unemployment. In this chapter, we will study how firms decide how much of each input to employ in their production of a good or service. This knowledge will allow us to address the question of whether firms are likely to reduce the amount of labor they employ if the minimum wage is increased.

In order to provide goods and services to the marketplace, firms use inputs. These inputs are costly, so firms must be smart about how they use labor, capital, and other inputs to achieve a certain level of output. The goal of any profit maximizing firm is to produce any level of output at the minimum cost. Doing anything else cannot be a profit maximizing strategy. This chapter studies the cost minimization problem for firms: how to most efficiently use inputs to produce output.

EXPLORING THE POLICY QUESTION

Read the <u>Labor Day Turns Attention Back to Minimum-Wage Debate</u> article and answer the following questions:

- What potential benefits to raising the minimum wage are identified in the article?
- · What potential disadvantages to raising the minimum wage are identified?

LEARNING OBJECTIVES

7.1 The Economic Concept of Cost

Learning Objective 7.1: Explain fixed and variable costs, opportunity cost, sunk cost, and depreciation.

7.2 Short-Run Cost Minimization

Learning Objective 7.2: Describe the solution to the cost minimization problem in the short run.

7.3 Long-Run Cost Minimization

Learning Objective 7.3: Describe the solution to the cost minimization problem in the long run.

7.4 When Input Costs and Output Change

Learning Objective 7.4: Analyze the effect of changes in prices or output on total cost.

7.5 Policy Example

Will an Increase in the Minimum Wage Decrease Employment?

Learning Objective 7.5: Apply the concept of cost minimization to a minimum-wage policy.

7.1 THE ECONOMIC CONCEPT OF COST

Learning Objective 7.1: Explain fixed and variable costs, opportunity cost, sunk cost, and depreciation.

From the isoquants described in <u>chapter 6</u>, we know that firms have many choices of input combinations to produce the same amount of output. Each point on an isoquant represents a different combination of inputs that produces the same amount of output.

Of course, inputs are not free: the firm must pay workers for their labor, buy raw materials, and buy or rent machines, all of which are costly. So the key question for firms is, Which point on an isoquant is the best choice? The answer is the point that represents the lowest cost. The topics of this chapter will help us locate that point.

This chapter studies production costs—that is, how costs are related to output. In order to draw a cost curve that shows a single cost for each output amount, we have to understand how firms make the decision about which set of possible inputs to use to be as efficient as possible. To be as efficient as possible means that the firm wants to produce output at the lowest possible cost.

For now, we assume that firms want to produce as efficiently as possible—in other words, minimize costs. Later, in <u>chapter 9</u>, "Profit Maximization and Supply," we will see that producing at the lowest cost is what profit maximizing firms must do (otherwise, they cannot possibly be maximizing profit!).

A good way to think about the cost side of the firm is to consider a manager who is in charge of running a factory for a large company. She is responsible for producing a specific amount of output at the lowest possible cost. She must choose the mix of inputs the factory will use to achieve the production target. Her task, in other words, is to run her factory as efficiently as possible. She does not want to use any extra inputs, and she does not want to pick a mix of inputs that costs more than another mix of inputs that produces the same amount of output.

To make efficient or cost-minimizing decisions, it is important to understand some basic cost concepts, starting with fixed and variable costs as well as opportunity costs, sunk costs, and depreciation.

Fixed and Variable Costs

A **fixed cost** is a cost that does not change as output changes. For example, a firm might need to pay for the lights to be on in order for the workers to see what they are doing and for production to happen. But the lights are simply on or off, and the cost of powering them does not change when output changes.

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A **variable cost** is a cost that changes as output changes. For example, a firm that wishes to produce more output might need to employ more labor hours by either hiring more workers or having existing workers work more hours. The cost of this labor is therefore a variable cost, as it changes as the output level changes.

Opportunity Costs

As we learned in <u>chapter 3</u>, the **opportunity cost** of something is the value of the next best alternative given up in order to get it.

Suppose a firm has access to an input that it can use in production without paying a price for it. A simple example is a family farm. The farm uses land, water, seeds, fertilizer, labor, and farm machinery to produce a crop—let's say corn—which it then sells in the marketplace. If the farm owns the land it uses to produce the corn, do we then say that the land component is not part of the firm's costs? The answer, of course, is no. When the farm uses the land to produce corn, it forgoes any other use of the land; that is, it gives up the opportunity to use the resource for another purpose. In many cases, the opportunity cost is the market value of the input.

For example, suppose an alternative use for the land is to rent it to another farmer. The forgone rent from the decision to use the land to produce its own corn is the farm's opportunity cost and should be factored into the production decision. If the opportunity cost, which in this case is the rental fee, is higher than the profit the farm will earn from producing corn, the most efficient economic decision is to rent out the land instead.

Now consider the more complex example of a farm manager who is told to produce a certain amount of corn. Suppose that the manager figures out that she can produce exactly that amount using a low-fer-tilizer variety of corn and all the available land. She also knows that another way to produce the same amount of corn is with a higher-yielding variety that requires a lot more fertilizer but uses only 75 percent of the land. The additional fertilizer for this higher-yielding corn will cost an extra \$50,000. Which option should the farm manager choose?

Without considering the opportunity cost, she would use the low-fertilizer variety of corn and all of the land because it costs \$50,000 less than the alternative method. But what if, under the alternative method, she could rent out for \$60,000 the 25 percent of the land that would not be planted? In that case, the cost-minimizing decision is actually to use the higher-yielding corn variety and rent out the unused land.

Another classic example is that of a small business owner who runs, say, a coffee shop. The inputs into the coffee shop are the labor, the coffee, the electricity, the machines, and so on. But suppose the owner also works a lot in the shop. He does not pay himself a salary but simply pays himself from the shop's excess revenues, or revenues in excess of the cost of the other inputs. The cost of his labor for the shop is not \$0 but the amount he could earn working elsewhere instead. If, for example, he could work in the local bank for \$4,000 a month, then the opportunity cost of his working at the coffee shop is \$4,000, and if the excess revenues are less than \$4,000, he should close the shop and work at the bank instead, assuming he likes both jobs equally well.

Sunk Costs

Some costs are recoverable, and some are not. An example of a recoverable cost is the money a farmer spends on a new tractor knowing that she can turn around and re-sell it for the same amount she paid.

A **sunk cost** is an expenditure that is not recoverable. An example of a sunk cost is the cost of the paint a business owner uses to paint the leased storefront of his coffee shop. Once the paint is on the wall, it has no resale value. Many inputs reflect both recoverable and sunk costs. A business that buys a car for an employee's use for \$30,000 and can resell it for \$20,000 should consider \$10,000 of its expenditure a sunk cost and \$20,000 a recoverable cost.

Why do sunk costs matter in choosing inputs? Because after incurring sunk costs, a manager should not consider them in making subsequent decisions. Sunk costs have no bearing on such decisions. To see this, suppose you buy a \$500 non-refundable and non-transferrable airline ticket to go to Florida during spring break. However, as spring break approaches, you are invited by friends to spend the break at a mountain cabin they have rented to which they will give you a ride in their car at no cost to you. You prefer to spend the break with your friends in the cabin, but you have already spent the \$500 on the ticket, and you feel compelled to get your money's worth by using it to go to Florida. Doing so would be the wrong decision. At the time of your decision, the \$500 spent on the ticket is non-recoverable and therefore a sunk cost. Whether you go to Florida or not, you cannot get the \$500 back, so you should do what makes you most happy, which is going to the cabin.

Depreciation

Depreciation is the loss of value of a durable good or asset over time. A **durable good** is a good that has a long usable life. Durable goods are things like vehicles, factory machines, or appliances that generally last many years. The difference between the beginning value of a durable good and its value sometime later is called depreciation. Most durable goods depreciate: machines wear out; newer, more advanced ones are produced, thus reducing the value of current ones; and so on.

Suppose you are a manager who runs a pencil-making factory that uses a large machine. How does the machine's depreciation factor into the cost of using it?

The appropriate way to think about these costs is through the lens of opportunity cost. If your factory didn't use the machine, you could rent it to another firm or sell it. Let's consider the selling of the machine. Suppose it costs \$100,000 to purchase the machine new, and it depreciates at a rate of \$1,000 per month, meaning that each month, its resale value drops by \$1,000. Note that the purchase cost of the machine is not sunk because it is recoverable—but each month, the recoverable amount diminishes with the rate of depreciation. So, for example, exactly one year after purchase, the machine is worth \$88,000. At this point in time, the \$12,000 depreciation has become a sunk cost. However, at the current point in time, you have a choice: you can sell the machine for \$88,000 or use it for a month and sell it at the end of the month for \$87,000. The opportunity cost of using the machine for this month is exactly \$1,000 in depreciation.

Why does depreciation matter in choosing inputs? Well, suppose workers can do the same job as the machine, or in economics parlance, suppose you can substitute workers for capital. To produce the same amount of pencils as the machine, you need to add labor hours at a rate of \$900 a month. A manager without good economics training might think that since the firm purchased the machine, the machine is free, and since the labor costs \$900 a month, use the machine. But you—a manager well trained in economics—know that the monthly cost of using the machine is the \$1,000 drop in resale value (the depreciation cost), and the monthly cost of the labor is \$900. You will save the company \$100 a month by using the labor and selling the machine.

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7.2 SHORT-RUN COST MINIMIZATION

Learning Objective 7.2: Describe the solution to the cost minimization problem in the short run.

In order to maximize profits, firms must minimize costs. Cost minimization simply implies that firms are maximizing their productivity or using the lowest cost amount of inputs to produce a specific output. In the short run, firms have fixed inputs, like capital, giving them less flexibility than in the long run. This lack of flexibility in the choice of inputs tends to result in higher costs.

In chapter 6, we studied the short-run production function:

$$Q = f(L, \overline{K})$$

where Q is output, L is the labor input, and \overline{K} is capital. The bar over K indicates that it is a fixed input. The short-run cost minimization problem is straightforward: since the only adjustable input is labor, the solution to the problem is to employ just enough labor to produce a given level of output.

Figure 7.1 illustrates the solution to the short-run cost minimization problem. Since capital is fixed, the decision about labor is to choose the amount that, combined with the available capital, enables the firm to produce the desired level of output given by the isoquant.

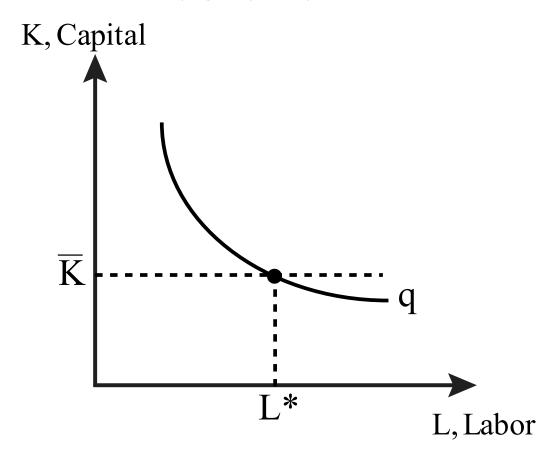


Figure 7.1 Short-run cost minimization

From **figure 7.1**, it is clear that the only cost-minimizing level of the variable input, labor, is at L^* . To see this, note that any level of labor below L^* would yield a lower level of output, and any level of labor above L^* would yield the desired level of output but would be more costly than L^* because each additional unit of labor employed must be paid for.

Mathematically, this problem requires only that we solve the following production function for L:

$$Q = f(\overline{K}, L)$$

Solving the production function requires that we invert it, which we can do only if the function is monotonic. This requirement is satisfied for our production functions because we assume that output always increases when inputs increase.

$$L^*=f^{-1}(\overline{K},q)$$

Let's consider a specific example of a **Cobb-Douglas** production function:

$$Q=10\overline{K}^{rac{1}{2}}L^{rac{1}{2}}$$

To find the cost-minimizing level of labor input, L^* , we need to solve this equation for L^* :

$$L^{rac{1}{2}} = (rac{q}{10\overline{K}^{rac{1}{2}}})^2$$

This simplifies to

$$L^* = \frac{q^2}{100\overline{K}}$$

Note that this equation does not require a specific output target but rather gives us the cost-minimizing level of labor for *every* level of output. We call this an **input-demand function**: a function that describes the optimal factor input level for every possible level of output.

7.3 LONG-RUN COST MINIMIZATION

Learning Objective 7.3: Describe the solution to the cost minimization problem in the long run.

The long run, by definition, is a period of time when all inputs are variable. This gives the firm much more flexibility to adjust inputs to find the optimal mix based on their relative prices and relative marginal productivities. This means that the cost can be made as low as possible, and generally lower than in the short run.

Total Cost in the Long Run and the Isocost Line

For a long-run, two-input production function, Q=f(L,K), the total cost of production is the sum of the cost of the labor input, L, and the capital input, K.

- The cost of labor is called the wage rate, w.
- The cost of capital is called the rental rate, r.
- The cost of the labor input is the wage rate multiplied by the amount of labor employed, wL.
- The cost of capital is the rental rate multiplied by the amount of capital, rK.

The total cost (C), therefore, is

$$C(Q) = wL + rK$$

If we hold total cost C(Q) constant, we can use this equation to find isocost lines. An **isocost line** is a graph of every possible combination of inputs that yields the same cost of production. By picking a cost, and given wage rates, w, and rental rates, r, we can find all the combinations of L and K that solve the equation and graph the isocost line.

Consider the example of a pencil-making factory, where both capital in the form of pencil-making machines and labor to run those machines are utilized. Suppose the wage rate of labor for the pencil maker is \$20 per hour and the rental rate of capital is \$10 per hour. If the total cost of production is \$200, the firm could be employing ten hours of labor and no capital, twenty hours of capital and no labor, five hours of labor and ten hours of capital, or any other combination of capital and labor for which the total cost is \$200. **Figure 7.2** illustrates this particular isocost line.

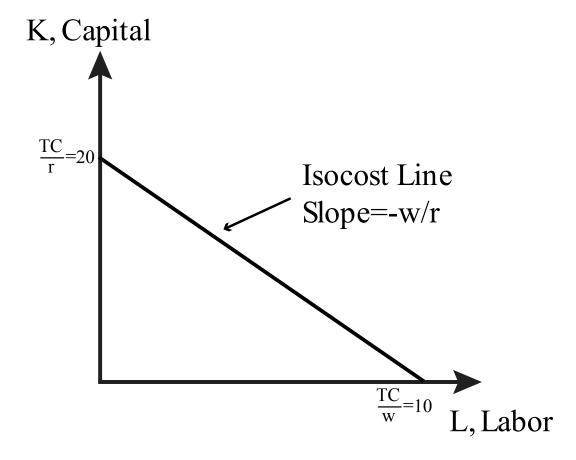


Figure 7.2 An isocost line

This figure represents the isocost line where total cost equals \$200. But we can draw an isocost line that is associated with any total cost level. Notice that any combination of labor hours and capital that is less expensive than this particular isocost line will end up on a lower isocost line. For example, two hours of labor and five hours of capital will cost \$90. Any combination of hours of labor and capital that are more expensive than this particular isocost line will end up on a higher isocost line. For example, twenty hours of labor and thirty hours of capital will cost \$700.

Note that the slope of the isocost line is the ratio of the input prices, -w/r. This tells us how much of one input (capital) we have to give up to get one more unit of the other input (labor) and maintain the same level of total cost. For example, if both labor and capital cost \$10 an hour, the ratio would be -10/10 or -1. This is intuitive—if they cost the same amount, to get one more hour of labor, you need to give up one hour of capital. In our pencil-maker example, labor is \$20 per hour, and capital is \$10 per hour, so the ratio is -2: to get one more hour of labor input, you must give up two hours of capital in order to maintain the same total cost or remain on the same isocost line.

The solution to the long-run cost minimization problem is illustrated in **figure 7.3**. The plant manager's problem is to produce a given level of output at the lowest cost possible. A given level of output corresponds to a particular isoquant, so the cost minimization problem is to pick the point on the isoquant that is the lowest cost of production. This is the same as saying the point that places the firm on the lowest isocost line. We can see this by examining **figure 7.3** and noting that the point on the isoquant that corresponds to the lowest isocost line is the one where the isocost is tangent to the isoquant.

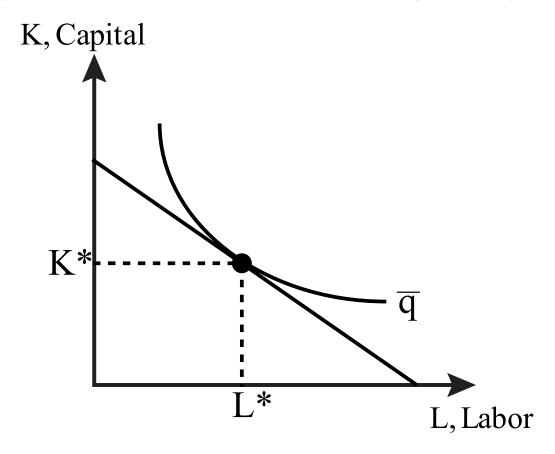


Figure 7.3 Solution to the long-run cost minimization problem

From **figure 7.3**, we can see that the optimal solution to the cost minimization problem is where the isocost and isoquant are tangent: the point at which they have the same slope. We just learned that the slope of the isocost is -w/r, and in <u>chapter 6</u>, we learned that the slope of the isoquant is the marginal rate of technical substitution (MRTS), which is the ratio of the marginal product of labor and capital:

$$MRTS = -rac{MP_L}{MP_K}$$

So the solution to the long-run cost minimization problem is

$$MRTS = -rac{w}{r}$$
 ,

or

$$rac{MP_L}{MP_K} = rac{w}{r}$$
(7.1)

This can be rearranged to help with intuition:

$$rac{MP_L}{w}=rac{MP_K}{r}$$
(7.2)

Equation (**7.2**) says that at the cost-minimizing mix of inputs the marginal products per dollar must be equal. This conclusion makes sense if you think about what would happen if equation ([pb_glossay id="752"]7.2[/pb_glossay]) did not hold. Suppose instead that the marginal product of capital per dollar was more than the marginal product of labor per dollar:

$$rac{MP_L}{w} < rac{MP_K}{r}$$

This inequality tells us that this current use of labor and capital cannot be an optimal solution to the cost minimization problem. To understand why, consider the effect of taking a dollar spent on labor input away, thereby lowering the amount of labor input (raising the MP_L —remember the law of diminishing marginal returns), and spending that dollar instead on capital and increasing the capital input (lowering the MP_K). We know from the inequality that if we do this, overall output must increase because the additional output from the extra dollar spent on capital has to be greater than the lost output from the diminished labor. Therefore, the net effect is an increase in overall output. The same argument applies if the inequality were reversed.

An Example of Minimizing Costs in the Long Run

Consider a specific example of a gourmet root beer producer whose labor cost is \$20 an hour and whose capital cost is \$5 an hour. Suppose the production function for a barrel of root beer, Q, is $Q=10L^{rac{1}{2}}K^{rac{1}{2}}.$ If the output target is one thousand barrels of root beer, they could, for example, utilize one hundred hours of labor, L, and one hundred hours of capital, K, to yield 10(10)(10) = 1,000 barrels of root beer. But is this the most cost-efficient way to do it? More generally, what is the most cost-effective mix of labor and capital to produce one thousand barrels of root beer?

To determine this, we must start with the marginal products of labor and capital, which for this production function are the following:

$$^{(7.3)}\,MP_L = 5L^{-rac{1}{2}}K^{rac{1}{2}} \ ^{(7.4)}\,MP_K = 5L^{rac{1}{2}}K^{-rac{1}{2}}$$

Calculus (Long-Run Cost Minimization Problem)

Mathematically, we express the long-run cost minimization problem in the following way; we want to minimize total cost subject to an output target:

$$rac{min}{(L,K)}wL+rK$$
(7.1C) subject to $Q=f=(L,K)$ (7.2C)

We can proceed by defining a Lagrangian function:

(7.3C)
$$\wedge (L,K,\lambda) = wL + rK - \lambda (f(L,K)-q)$$

where λ is the Lagrange multiplier. The first-order conditions for an interior solution (i.e., L>0 and K>0) are as follows:

$$^{ ext{(7.4C)}}rac{\partial \wedge}{\partial L}=0 \Rightarrow w=\lambdarac{\partial f(L,K)}{\partial L}$$
 $^{ ext{(7.5C)}}rac{\partial \wedge}{\partial K}=0 \Rightarrow r=\lambdarac{\partial f(L,K)}{\partial K}$ $^{ ext{(7.6C)}}rac{\partial \wedge}{\partial \lambda}=0 \Rightarrow Q=f(L,K)$

From <u>chapter 6</u>, we know that $MP_L = rac{\partial f(L,K)}{\partial L}$ and

$$MP_K = rac{\partial f(L,K)}{\partial K}$$

Substituting these in and combining **7.4C** and **7.5C** to get rid of the Lagrange multiplier yields expression (**7.1**):

(7.7C)
$$\frac{MP_L}{MP_K}=rac{w}{r}$$

And **7.6C** is the constraint:

(7.8C)
$$Q=f(L,K)$$

Equations (7.7C) and (7.8C) are two equations in two unknowns, L and K, and can be solved by repeated substitution. Note that these are exactly the conditions that describe **figure 7.3**. Equation (7.7C) is the mathematical expression of MRTS=-w/r, and equation (7.8C) pins us down to a specific isoquant, as MRTS=-w/r holds for a potentially infinite number of isoquants and isocost lines depending on the Q chosen.

And thus the
$$MRTS, -\frac{MP_L}{MP_K}$$
 is $-\frac{K}{L}.$ The ratio $-\frac{w}{r}$ in this case is $-\frac{20}{5}$, or -4 .

So the condition that characterizes the cost-minimizing level of input utilization is $\frac{K}{L}=4$, or K=4L. That is, for every hour of labor employed, L, the firm should utilize four hours of capital. This makes sense when you think about the fact that labor is four times as expensive.

sive as capital. Now, what are the specific amounts? To find them, we substitute our ratio into the production function set at one thousand barrels:

If
$$K=4L$$
, then $1,000=10L^{rac{1}{2}}K^{rac{1}{2}}$ or $L=rac{100}{\sqrt{4}}$, which equals fifty.

If L=50, then K=200. So using fifty hours of labor and two hundred hours of capital is the most cost-effective way to produce one thousand barrels of root beer for this firm.

Calculus

- 1. For the following questions, the $Q=5L^{rac{1}{3}}K^{rac{2}{3}}$, w=\$30 an hour, r=\$15 and hour, and the production target Q=1,200.
 - a. Find the marginal product of labor.
 - b. Find the marginal product of capital.
 - c. Find the MRTS.
 - d. Find the optimal amount of labor and capital inputs.
 - e. For $Q=5L^{rac{1}{3}}K^{rac{2}{3}}$ and w and r , solve for the input-demand functions using

the Lagrangian method.

7.4 WHEN INPUT COSTS AND OUTPUT CHANGE

Learning Objective 7.4: Analyze the effect of changes in prices or output on total cost.

In the previous section, we determined the cost-minimizing combination of labor and capital to produce one thousand barrels of root beer. As long as the prices of labor and capital remain constant, this producer will continue to make the same choice for every one thousand barrels of root beer produced. But what happens when input prices change?

Suppose, for example, an increasing demand for the capital equipment used to make root beer drives the rental price up to \$10 an hour. This means capital is more expensive than before not only in absolute terms but in relative terms as well. In other words, the opportunity cost of capital has increased. Before the price increase, for every extra hour of capital utilized, the root beer firm had to give up $\frac{1}{4}$ of an hour of labor. After the rental rate increase, the opportunity cost has increased to $\frac{1}{2}$ an hour of labor. A cost-minimizing firm should therefore adjust by utilizing less of the relatively more expensive input and more of the relatively less expensive input.

In this case, the ratio $-\frac{w}{r}$ is now $-\frac{20}{10}$, or -2. So the new condition that characterizes the cost-mini-

mizing level of input utilization after the price change is $rac{K}{L}=2$, or $K=\,2\,L$.

The production function for one thousand barrels has not changed:

$$1,000=10L^{rac{1}{2}}K^{rac{1}{2}}$$

So if
$$K=2L$$
, then $1,000=10L^{rac{1}{2}}(2L)^{rac{1}{2}}$, or $L=rac{100}{\sqrt{2}}$, which equals roughly 71. If $L=71$,

then K=2L=142. As expected, the firm now uses more labor than it did prior to the price change and less capital.

We can also calculate and compare the total cost before and after the increase in the rental rate for capital. Total cost is C(Q)=wL+rK, so in the first case where w is \$20 and r is \$5, the total cost is

$$C(Q) = 20(L) + 5(K) = \$20(50) + \$5(200) = \$1,000 + \$1,000 = \$2,000.$$

Now when capital rental rates increase to \$10, total cost becomes

$$C(Q) = 20(L) + 10(K) = \$20(71) + \$10(142) = \$1,420 + \$1,420 = \$2,840.$$

This new higher cost makes sense because the production function did not change, so the firm's efficiency remained constant, wages remained constant, but rental rates increased. So overall, the firm saw a cost increase and no change in productivity, leading to an increase in production costs.

Expansion Path

A firm's expansion path is a curve that shows the cost-minimizing amount of each input for every level of output. Let's look at an example to see how the expansion path is derived.

Equation (7.5) describes the production function set to the specific production target of one thousand barrels of root beer. If we replace one thousand with the output level Q, we get the following expression:

$$^{(7.6)}\,Q=10L^{rac{1}{2}}K^{rac{1}{2}}$$

We use the K=4L ratio of capital to labor that characterizes the cost-minimizing ratio when the wage rate for labor is \$20 an hour and the rental rate for capital is \$5 an hour:

$$oldsymbol{\cdot}$$
 If $K=4L$, then $Q=10L^{rac{1}{2}}(4L)^{rac{1}{2}}$, or $Q=20L$ or $L(q)=rac{q}{20}$.

$$oldsymbol{\cdot}$$
 If $L(q)=rac{q}{20'}$, then $K(q)=rac{4q}{20}=rac{q}{5}$.

So using fifty hours of labor and two hundred hours of capital is the most cost-effective way to produce one thousand barrels of root beer for this firm.

Note that $L(q)=rac{q}{20}$ and $K(q)=rac{4q}{20}=rac{q}{5}$ are both functions of output Q. These are the input-demand functions.

Input-demand functions describe the optimal, or cost-minimizing, amount of a specific production input for every level of output. Note that when the output Q=1,000, L(Q)=50 and K(Q)=200, just as we found before. But from these factor demands, we can immediately find the optimal amount of labor and capital for any output target at the given input prices. For example, suppose the factory wanted to increase output to two thousand or three thousand barrels of root beer:

· At
$$Q=2,000$$
 $L(2,000)=rac{2,000}{20}=100$ and $K(2,000)=rac{2,000}{5}=400$.

$$\cdot$$
 At $Q=3,000$ $L(3,000)=rac{3,000}{20}=150$ and $K(3,000)=rac{3,000}{5}=600$.

We can graph this firm's expansion path (**figure 7.4**) from the input demands when Q equals one thousand, two thousand, and three thousand. We can also immediately derive the long-run total cost curve from these factor demands by putting them into the long-run cost function, C(!) = wL + rK:

$$C(Q)=wL+rK=wL(Q)+rK(Q)=wrac{Q}{20}+rrac{q}{5}$$
 At input prices w = \$20 and r = \$5, the function becomes $C(Q)=20rac{Q}{20}+5rac{Q}{5}=2Q$.

The long-run total cost curve shows us the specific total cost for each output amount when the firm is minimizing input costs.

Graphically, the expansion path and associated long-run total cost curve look like figure 7.4.

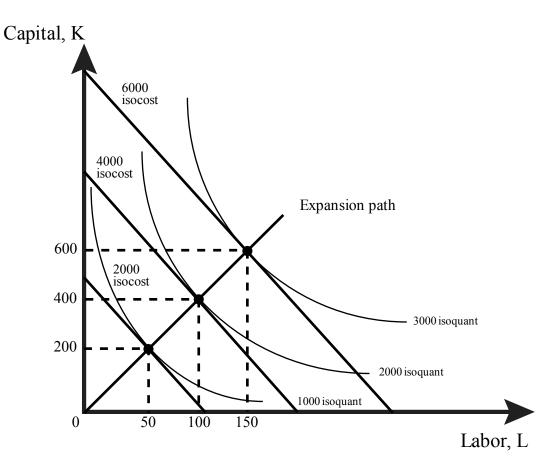


Figure 7.4 The expansion path and long-run cost curve

Figure 7.4 illustrates how the solution to the cost minimization problem translates into factor demands and long-run total cost. We can solve for the factor demands and the total cost function more generally by replacing our specific input prices with w and r in the following way. The solution to the cost minimization problem is characterized by the MRTS equaling the input price ratio: the $MRTS = \frac{K}{L}$ and the input price ratio $= \frac{w}{r}$, so $\frac{K}{L} = \frac{w}{r}$, or rK = wL, or $L = \frac{rK}{w}$. We can plug this into the

production function to get
$$Q=10L^{rac{1}{2}}K^{rac{1}{2}}=10(rac{rK}{w})^{rac{1}{2}}\,K^{rac{1}{2}}=10(rac{r}{w})^{rac{1}{2}}\,K$$
 .

Solving for the input demand for capital yields

$$K^*=rac{Q}{10}(rac{w}{r})^{rac{1}{2}}\cdot$$

Since $L=rac{rK}{w}$, we can find the input demand for labor:

$$L^* = \frac{Q}{10} \left(\frac{r}{w}\right)^{\frac{1}{2}}$$

Now we have input-demand functions that are functions of both output, Q, and the input prices, w and r. Note that when Q rises, the inputs of both capital and labor rise as well. Also note that when the

price of labor, w, rises relative to the price of capital, r, or when $\frac{w}{r}$ rises, the use of the capital input rises and the use of the labor input falls. And when the price of capital rises relative to the price of labor, the use of labor rises, and the use of capital falls. So from these functions, we can see the firm's optimal adjustment to changing input costs in the form of substituting the relatively cheaper input for the relatively more expensive input.

Perfect Complement and Perfect Substitute Production Functions

Perfect complements and perfect substitutes in production are not uncommon. Suppose our pencil-making firm needs exactly one operator (labor) to operate one pencil-making machine. A second worker per machine adds nothing to output, and a second machine per worker also adds nothing to output. In this case, the pencil-making firm would have a perfect complement production function. Alternatively, suppose our root beer producer could either use two workers (labor) to measure and mix up the ingredients or employ one machine to do the same job. Either combination yields the same output. In this case, the root beer producer would have a perfect substitute production function.

Similar to the consumer choice problem, for production functions where inputs are perfect complements or substitutes, the condition that MRTS equals the price ratio will no longer hold. To see this, consider **figure 7.5**.

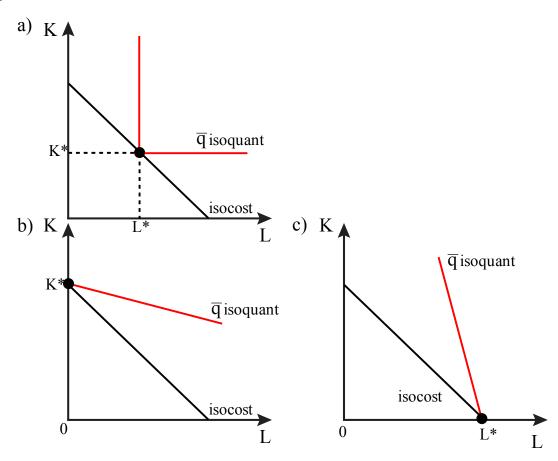


Figure 7.5 The long-run cost minimization solution for perfect complements (a) and perfect substitutes (b, c)

In panel (a), a perfect complement isoquant just intersects the isocost line at the corner of the isoquant. (Take a moment and confirm to yourself that any other combination of labor and capital on the isoquant would be more expensive.) However, at the corner of the isoquant, the slope is undefined, so there is no MRTS. For perfect complements, using inputs in any combination other than the optimal ratio is not cost minimizing. So we can immediately express the optimal ratio as a condition of cost. If the production function is of the perfect complement type, $Q=min[\alpha L,\beta K]$, the optimal input ratio is $\alpha L=\beta K$. And since output is equal to the minimum of the two arguments of the function, that means $Q=\alpha L=\beta K$. So the optimal amount of inputs for any output level q is $L^*=\frac{q}{a'}$ and $K^*=\frac{q}{\beta}$.

Panels (b) and (c) of **figure 7.5** show the optimal solution to the long-run cost minimization problem when the production function is a perfect substitute type. The solution is on one corner or the other of the isocost line, depending on the marginal productivities of the inputs and their costs. In (b), the MRTS or the slope of the isoquant is lower (less steep) than the slope of the isocost line or the ratio of the input prices. Since this is the case, it is much less costly to employ only capital to produce Q. In (c), the MRTS or the slope of the isoquant is higher (steeper) than the slope of the isocost line or the ratio of the input prices. Since this is the case, it is much less costly to employ only labor to produce Q.

Recall that a perfect substitute production function is of the additive type:

$$Q = \alpha L + \beta K$$

The marginal product of labor is α , and the marginal product of capital is β .

Since the MRTS is the ratio of the marginal products, the MRTS is $\frac{\alpha}{\beta}$, which is also the slope of the isoquant.

The ratio of input prices is $\frac{w}{r}$. This price ratio is the slope of the isocost.

From the graphs we can see that if $\frac{\alpha}{\beta}<\frac{w}{r}$, or the isoquant is less steep than the isocost, only capital is used, thus we know that no labor will be employed, or $L^*=0$, and output must equal βK , or $Q=\beta K$. Solving this for K gives us $K^*=\frac{q}{\beta}$. Alternatively, if $\frac{\alpha}{\beta}>\frac{w}{r}$, only labor is used, so $K^*=0$, $Q=\alpha L$, and $L^*=\frac{q}{\alpha}$.

7.5 POLICY EXAMPLE

WILL AN INCREASE IN THE MINIMUM WAGE DECREASE EMPLOYMENT?

Learning Objective 7.5: Apply the concept of cost minimization to a minimum-wage policy.

On May 15, 2014, the city of Seattle, Washington, passed an ordinance that established a minimum wage of \$15 an hour, almost \$5 more than the statewide minimum wage and more than double the federal minimum of \$7.25 an hour.

A minimum wage increase brings up many issues about its impact, particularly for a city surrounded by suburbs that allow much lower rates of pay. One question we can answer with our current tools is how Seattle-based businesses affected by the increased minimum wage are likely to react to the higher cost of labor.

Most businesses that employ labor have many other inputs as well, some of which can be substituted for labor. Consider a janitorial firm that sells floor-cleaning services to office buildings, restaurants, and

industrial plants. The janitorial firm can choose to clean floors using a small amount of capital and a large amount of labor: they can employ many cleaners and equip them with a simple mop.



"Cleaning" from Nick Youngson from picpedia.org is licensed under CC BY-SA

Or they could choose to employ more capital in the form of a modern floor-cleaning machine and employ fewer cleaners.

Our theory of cost minimization can help us understand and predict the consequences of making the labor input for cleaning the floors 50 percent more expensive. **Figure 7.6** shows a typical firm's long-run cost minimization problem. It is reasonable to consider the long run in this case because it would not take the firm very long to lease or purchase and have delivered a floor-cleaning machine. It is also reasonable to assume that floor-cleaning machines and workers are substitutes but not perfect ones—meaning that machines can be used to replace some labor hours, but some machine operators are still needed. The opposite is also true: the restaurant can replace machines with labor, but labor needs some capital (a simple mop) to clean a floor.

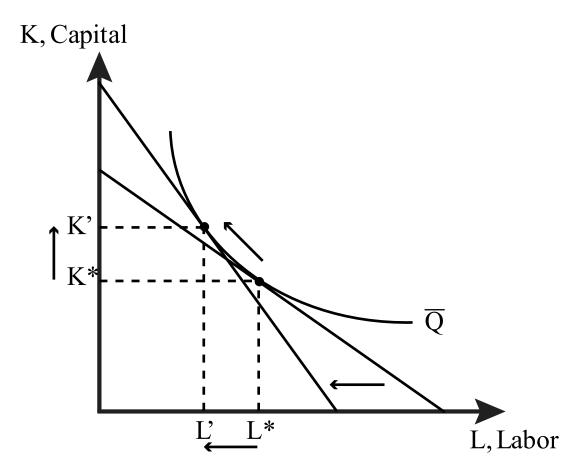


Figure 7.6 Change in inputs due to increase in wages

In **figure 7.6**, the isoquant, \overline{Q} , represents the fixed amount of floor the firm needs to clean each day and the different combinations of capital and labor it can use to achieve that output target. When the cost of labor, w, increases and the cost of capital, r, stays the same, the isocost line gets steeper as w/r increases. We can see in the figure that when this happens, the firm will naturally shift away from using the relatively more expensive input and toward the relatively cheaper input. The restaurant will decrease the amount of labor it employs and increase the amount of capital it uses.

From this specific firm, we can generalize that a dramatic permanent increase in the minimum wage will cause affected firms to employ fewer hours of labor and that employment overall will fall in the affected area. The magnitude of employment change caused by such a policy depends on the production technology of all affected firms—that is, how easy it is for them to substitute more capital. All we can predict with our model currently is the fact that such shifts away from labor will likely occur. Whether the cost of this decrease in employment is outweighed by the benefit of such a policy is beyond the scope of the current analysis, but our model of cost minimization has provided useful insight into the decisions firms will make in reaction to the increase in minimum wage.

EXPLORING THE POLICY QUESTION

- 1. Do you support a national minimum wage increase? Why or why not?
- 2. Do you think the benefits of a minimum wage increase outweigh the costs? Explain your answer.

3. What do you predict would happen if, instead of a minimum wage, a tax on the purchase or rental of capital equipment was imposed?

REVIEW: TOPICS AND LEARNING OUTCOMES

7.1 The Economic Concept of Cost

Learning Objective 7.1: Explain fixed and variable costs, opportunity cost, sunk cost, and depreciation.

7.2 Short-Run Cost Minimization

Learning Objective 7.2: Describe the solution to the cost minimization problem in the short run.

7.3 Long-Run Cost Minimization

Learning Objective 7.3: Describe the solution to the cost minimization problem in the long run.

7.4 When Input Costs and Output Change

Learning Objective 7.4: Analyze the effect of changes in prices or output on total cost.

7.5 Policy Example

Will an Increase in the Minimum Wage Decrease Employment?

Learning Objective 7.5: Apply the concept of cost minimization to a minimum-wage policy.

LEARN: KEY TOPICS

Terms

Fixed cost

A cost that does not change as output changes.

Variable cost

A cost that changes as output changes.

Sunk cost

An expenditure that is not recoverable, i.e., the cost of the paint a business owner uses to paint the leased storefront of his coffee shop.

Depreciation

The loss of value of a durable good or asset over time.

Durable good

A good that has a long usable life.

Input-demand function

A function that describes the optimal factor input level for every possible level of output, i.e.,

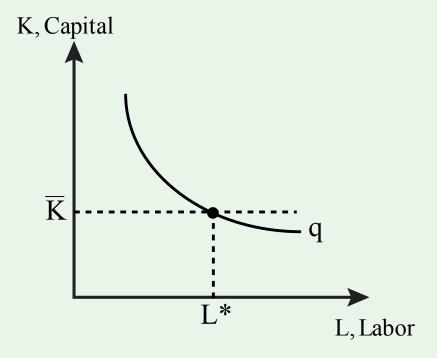
$$L^* = \frac{q^2}{100\overline{K}}$$

Isocost line

A graph of every possible combination of inputs that yields the same cost of production.

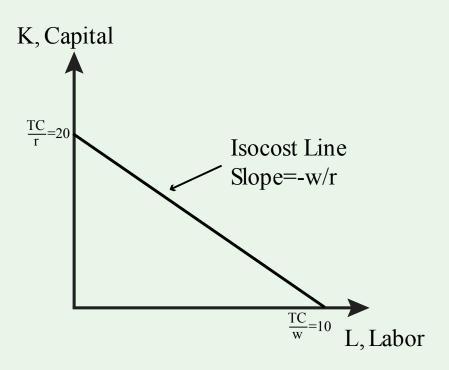
Graphs

Short-run cost minimization



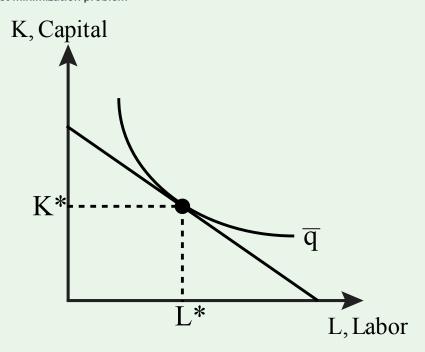
Short-run cost minimization

An isocost line



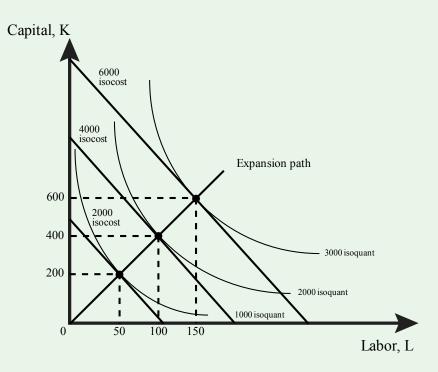
An Isocost Line

Solution to the long-run cost minimization problem



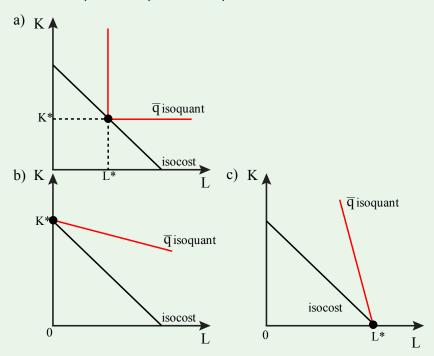
Long-run cost minimization problem

The expansion path and long-run cost curve



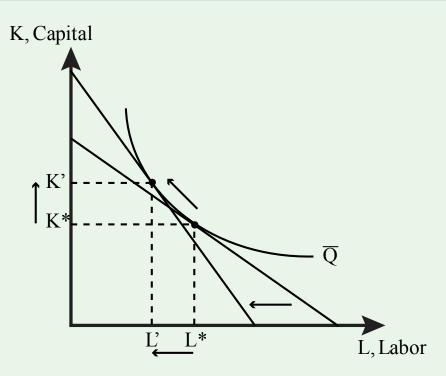
The expansion path and long-run cost curve

The long-run cost minimization solution for perfect complements and perfect substitutes



The long-run cost minimization solution for perfect complements (a) and perfect substitutes (b, c)

Change in inputs due to increase in wages



Changes in inputs due to increase in wages

Equations

Total cost

$$C(Q) = wL + rK$$

Marginal rate of technical substitution (MRTS)

$$MRTS = -rac{MP_L}{MP_K}$$

The MRTS is also the slope of the isoquant

Long-run cost minimization problem

The slope of the isoquant is the MRTS, and the slope of the is

$$-w/r$$

So the solution to the long-run cost minimization problem is

$$MRTS = -rac{w}{r}$$

or

$$rac{MP_L}{w} = rac{MP_K}{r}$$

This formula has many different <u>calculus</u> derived conclusions that should be reviewed.

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CHAPTER 8

Cost Curves

THE POLICY QUESTION

SHOULD THE FEDERAL GOVERNMENT PROMOTE THE DOMESTIC PRODUCTION OF STREETCARS?

In recent years, streetcars have enjoyed a bit of a renaissance in the United States. Streetcars are electric-powered public vehicles that ride on rails embedded into normal city streets and comingle with traffic. Once common in the United States and still common in many European cities, streetcars all but disappeared from US streets in the second half of the twentieth century. Portland, Oregon, is one city that revived the streetcar and subsequently expanded its system.

After initially buying streetcars from the German company Siemens, Portland's transit authority and government, pushed by the federal government, which funds a large portion of urban transit projects, decided to contract with a local firm, Oregon Iron Works, to produce the streetcars locally. Oregon Iron Works had no experience in manufacturing streetcars but created a subsidiary firm to do so called United Streetcar. Other US cities that were introducing streetcars, such as Washington, DC, and Tucson, Arizona, contracted with Oregon Iron Works for their cars as well. In the end, the firm faced severe delays and cost overruns and eventually got very behind on its scheduled delivery. In addition, the expected boom in streetcars slowed considerably with the recession of 2008 and changing municipal priorities. In 2014, United Streetcar ceased production and laid off its workers.

EXPLORING THE POLICY QUESTION

Is the story of United Streetcar an example of a misguided effort to steer business domestically? Would it have succeeded if the market for streetcars in the United States had not dried up? To answer these questions, we need to think about the cost structure of the industry and whether there are aspects of it that would support the decision to start manufacturing streetcars domestically. Cost curves—the subject of this chapter—are critical tools for analyzing a company's cost structure.

LEARNING OBJECTIVES

8.1 Short-Run Cost Curves

Learning Objective 8.1: Derive the seven short-run cost curves from the total cost function.

8.2 Long-Run Cost Curves

Learning Objective 8.2: Derive the three long-run cost curves from the total cost function.

8.3 Short-Run versus Long-Run Costs: The Advantage of Flexibility

<u>Learning Objective 8.3</u>: Explain why long-run costs are always as low as or lower than short-run costs and how more flexibility in choosing inputs is always better than less.

8.4 Multiproduct Firms, Learning Curves, and Learning by Doing

Learning Objective 8.4: Explain how making more than one product, learning over time, and learning by producing can lower costs.

8.5 Policy Example

Should the Federal Government Promote Domestic Production of Streetcars?

<u>Learning Objective 8.5</u>: Use a cost analysis to explain why building streetcars domestically in the United States is or is not a good policy.

8.1 SHORT-RUN COST CURVES

Learning Objective 8.1: Derive the seven short-run cost curves from the total cost function.

A cost curve represents the relationship between output and the different cost measures involved in producing the output. Cost curves are visual descriptions of the various costs of production. In order to maximize profits, firms need to know how costs vary with output, so cost curves are vital to the profit maximization decisions of firms.

There are two categories of cost curves: short run and long run. In this section, we focus on short-run cost curves.

The Seven Short-Run Cost Measures

The short run, as we learned in the previous chapter, is a time period short enough that some inputs are fixed while others are variable. There are seven cost curves in the short run: fixed cost, variable cost, total cost, average fixed cost, average variable cost, average total cost, and marginal cost.

The **fixed cost** (FC) of production is the cost of production that *does not vary with output level*. The fixed cost is the cost of the fixed inputs in production, such as the cost of a machine (capital) that costs the same to operate no matter how much production is happening. An example of such a machine is a conveyor belt in a factory that moves a streetcar chassis through various stages of an assembly line. The belt is either on or off, but the cost of running it does not change depending on how many streetcars it carries at any point in time.

Note that the fixed cost of a piece of capital equipment that the company owns includes the opportunity cost as well. In our example, the fixed cost includes the actual costs of running the conveyer belt, such as power and maintenance, as well as the opportunity cost of using it for the firm's own production rather than renting it out to another company.

The **variable cost** (VC) of production is the cost of production that *varies with output level*. This is the cost of the variable inputs in production—for example, the cost of the workers that assemble the electronic devices along a conveyor belt. The number of workers might depend on how many devices the factory is trying to produce in a day. If its production target increases, it uses more labor. Thus the hourly wages it pays for these workers are a variable cost. Variable cost generally increases with the amount of output produced.

Like fixed cost of production, there is an opportunity cost associated with variable cost of production. In this case, the next best use of these workers is to go to another firm that will employ them. Thus the market wage for workers represents their opportunity cost, and as such, the wage cost of employing them is equivalent to their opportunity cost.

The **total cost** (C) of production is the sum of fixed and variable costs of production:

$$C = FC + VC$$

There are three short-run average cost measures: average variable cost, average fixed cost, and average total cost.

Average variable cost (AVC) is the variable cost per unit of output. Mathematically, it is simply the variable cost divided by the output:

$$AVC = VC/Q$$

Note that since variable cost generally increases with the amount of output produced, the average variable cost can increase or decrease as output increases.

Average fixed cost (AFC) is the fixed cost per unit of output. Mathematically, it is simply the fixed cost divided by the output:

$$AFC = FC/Q$$

Because fixed cost does not change with the amount of output produced, the average fixed cost always decreases as output increases.

Average total cost (AC), or simply **average cost**, of production is total cost per unit of output. This is the same as the sum of the average fixed cost and the average variable cost:

$$AC = AC/Q = AFC + AVC$$

Because it is the sum of the average fixed cost, which is always declining with output, and the average variable cost, which may increase or decrease with output, the average total cost may increase or decrease with output.

Marginal cost (MC) is the additional cost incurred from the production of one more unit of output. Thus marginal cost is

$$MC = rac{\Delta C}{\Delta Q}.$$

The only part of total cost that increases with an additional unit of output is the variable cost, so we can rewrite the marginal cost as

$$MC = rac{\Delta VC}{\Delta Q}.$$

Calculus

The marginal cost is the rate of change of the total cost as output increases, or the slope of the total cost function, C(Q). To find this, we need to simply take the derivative of the total cost function:

$$MC(Q)=rac{dC(Q)}{dQ}$$
 Since $C(Q)=FC+VC(Q)$, we can rewrite this derivative as $MC(Q)=rac{dFC}{dQ}+rac{dVC(Q)}{dQ}$.

$$FC$$
 is a constant, so $rac{dFC}{dQ}=0$. Thus $MC(Q)=rac{dVC(q)}{Q}$.

Since fixed cost does not change as output increases, marginal cost depends only on the variable cost.

Fixed Cost, Variable Cost, and Total Cost Curves

Table 8.1 summarizes a firm's daily short-run costs. The firm has a fixed cost of \$50 per day of production. This cost is incurred whether the firm produces or not, as we can see by the fact that \$50 is still a cost when output is zero. The firm's fixed cost of \$50 does not change with

the amount of output produced. The data in the first two columns of **table 8.1** allow us to draw the firm's fixed cost curve. It is a horizontal line at \$50, as shown in **figure 8.1**.

Table 8.1 An example of the seven short-run cost measures

| Output | Fixed cost | Variable cost | Total cost | Marginal cost | Average fixed cost | Average variable cost | Average cost |
|--------|------------|---------------|------------|---------------|--------------------|-----------------------|--------------|
| Q | FC | VC | C | MC | AFC | AVC | AC |
| 0 | 50 | 0 | 50 | - | - | - | - |
| 1 | 50 | 40 | 90 | 40 | 50.0 | 40.0 | 90.0 |
| 2 | 50 | 70 | 120 | 30 | 25.0 | 35.0 | 60.0 |
| 3 | 50 | 90 | 140 | 20 | 16.7 | 30.0 | 46.7 |
| 4 | 50 | 100 | 150 | 10 | 12.5 | 25.0 | 37.5 |
| 5 | 50 | 120 | 170 | 20 | 10.0 | 24.0 | 34.0 |
| 6 | 50 | 150 | 200 | 30 | 8.3 | 25.0 | 33.3 |
| 7 | 50 | 190 | 240 | 40 | 7.1 | 27.1 | 34.3 |
| 8 | 50 | 240 | 290 | 50 | 6.3 | 30.0 | 36.3 |
| 9 | 50 | 300 | 350 | 60 | 5.6 | 33.3 | 38.9 |
| 10 | 50 | 370 | 420 | 70 | 5.0 | 37.0 | 42.0 |

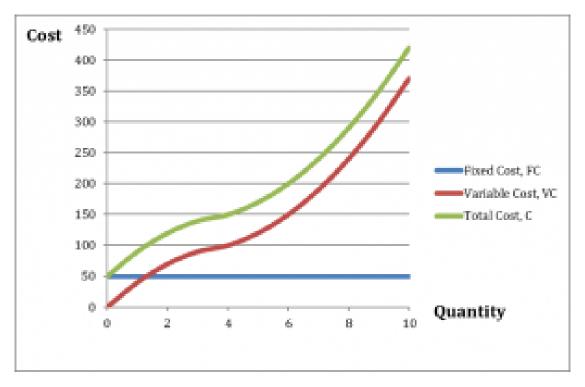


Figure 8.1 Three short-run cost curves: fixed, variable, and total costs

Figure 8.1 also shows variable and total cost curves plotted from data in **table 8.1**. The variable cost increases with output because extra output requires extra variable inputs. As we can see in the graph, the variable cost curve rises as output, Q, increases.

The short-run variable cost curve is determined by and matches the shape of the short-run production function, which we studied in <u>chapter 6</u>. The short-run production function is the same as the total product of labor curve when labor is the variable input in the short run, which we always assume it is. To go from the production function to the variable cost curve requires knowing the price of labor. Let's assume a constant price of labor, say \$10 an hour.

Figure 8.2 presents a typical short-run production function, which leads to the shape of the variable cost curve in **figure 8.1**. The production function exhibits increasing marginal returns to labor initially: as the labor input is increased from zero, the output increases at an increasing rate. Eventually, however, the addition of extra hours of labor leads to additional output at a decreasing rate. This happens as we increase labor input from ten hours of labor.

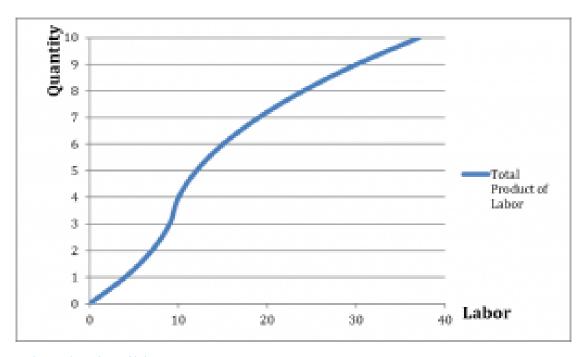


Figure 8.2 The total product of labor curve

If we multiply the amount of labor at every level of output in figure **8.2** by the wage rate of \$10 per hour, we get the variable cost curve from figure **8.1**.

Marginal, Average Fixed, Average Variable, and Average Total Cost Curves

Figure 8.3 presents the four remaining short-run cost curves: marginal cost (MC), average fixed cost (AFC), average variable cost (AVC), and average total cost (AC).

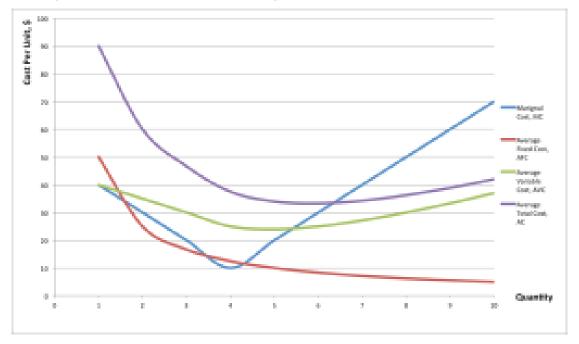


Figure 8.3 Short-run marginal cost, average fixed cost, average variable cost, and average total cost curves

The marginal cost, average variable cost, and average total cost curves are derived from the total cost curve.

From **figure 8.3**, we can see that the marginal cost curve crosses both the average variable cost curve and the average fixed cost curve at their minimum points. This is not random. Since the marginal cost indicates the extra cost incurred from the production of the next unit of output, if this cost is lower than the average, it must be bringing the average down. If this cost is higher than the average, it must pull the average up. Think of your own grade point average: if your average this term is higher than your overall average, your overall average will go up. If your average this term is lower than your overall average, your overall average will go down.

Calculus

- 1. If the total cost curve of a firm is $C(Q)=25+10Q^2$
 - a. What is the marginal cost curve?
 - b. What is marginal cost at Q=125?

8.2 LONG-RUN COST CURVES

Learning Objective 8.2: Derive the three long-run cost curves from the total cost function.

As we learned in previous chapters, in the long run, all inputs are variable, and there are no fixed costs. In this section, we look at the three long-run cost curves—total cost, average cost, and marginal cost—and how to derive them.

Long-Run Total Cost Curve

To determine the long-run total cost (LRTC) for a firm, we must think about the cost minimization problem introduced in <u>chapter 7</u>. Remember that the cost minimization problem answers the question, What is the most cost-effective way to produce a given amount of output? The total cost curve represents the cost associated with every possible level of output, so if we figure out the cost-minimizing choice of inputs for every possible level of output, we can determine the cost of producing each level of output.

When we do this exercise, we are looking for the expansion path of the firm. Recall from <u>chapter 7</u> that the expansion path is the combination of inputs that minimize costs for every level of output, and it can be graphed as a curve. **Figure 8.4** shows the expansion path for a firm that manufactures tablet computers.

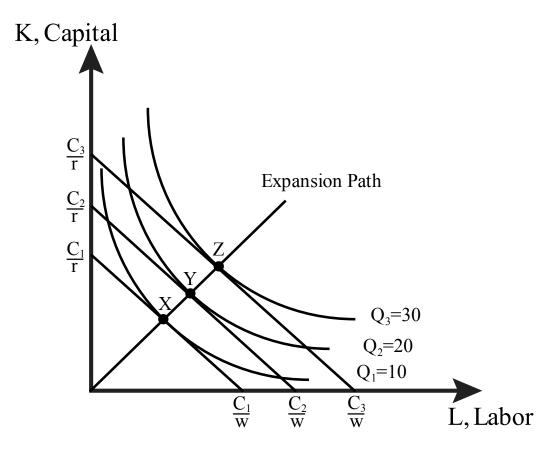


Figure 8.4 Expansion path

Each point on the expansion path is the solution to the cost minimization problem for that particular output. Recall from chapter 7 that r is the rental rate or price of capital and w is the wage rate or price of labor. Consider point X: here the output quantity is set at ten million, and the tangency of the isocost and isoquant at this point establishes the optimal combination of the inputs. To go from this point to the cost, we have only to know the combined cost of the inputs. Fortunately, the isocost line tells us exactly that; the total cost here is C_1 . Now consider point Y, where the output quantity has increased to twenty million. With this, the new production level is associated with a new isocost curve, with total cost at C_2 . Finally, point Z indicates that for an output quantity of thirty million, the total cost is C_3 .

From the expansion path, we can draw the total cost curve. We have three points already, X, Y, and Z. Point X describes a quantity of ten million tablets and a total cost of C_1 . Point Y describes a quantity of twenty million tablets and a total cost of C_2 . Point Z describes a quantity of thirty million tablets and a total cost of C_3 . These three cost-quantity pairs are three points on the long-run total cost curve illustrated in **figure 8.5**.

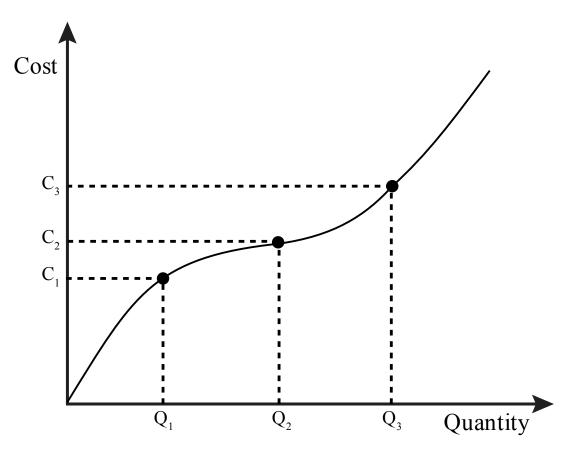


Figure 8.5 The long-run total cost curve

Remember from chapter 7 that the total cost is the sum of the input costs, LRTC = wL + rK. As we expand output, we must use more inputs, and the increase in labor and capital results in increasing overall cost of production.

A firm's **long-run average cost** (**LRAC**) is the cost per unit of output. In other words, it is the total cost, **LRTC**, divided by output, Q:

$$LRAC(Q) = \frac{LRTC(Q)}{Q}$$

A firm's **long-run marginal cost** (**LRMC**) is the increase in total cost from an increase in an additional unit of output:

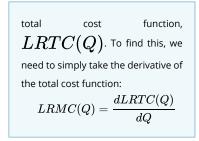
$$LRMC(Q) = rac{\Delta LRTC(Q)}{\Delta Q}$$

where $\Delta LRTC(Q)$ is the change in total cost and ΔQ is the change in output. This is the same thing as the slope of the total cost curve, LRTC(Q).

Figure 8.6 illustrates the relationship between the total cost curve (panel a) and the average and marginal cost curves (panel b).

Calculus

The long-run marginal cost is the rate of change of the total cost as output increases, or the slope of the



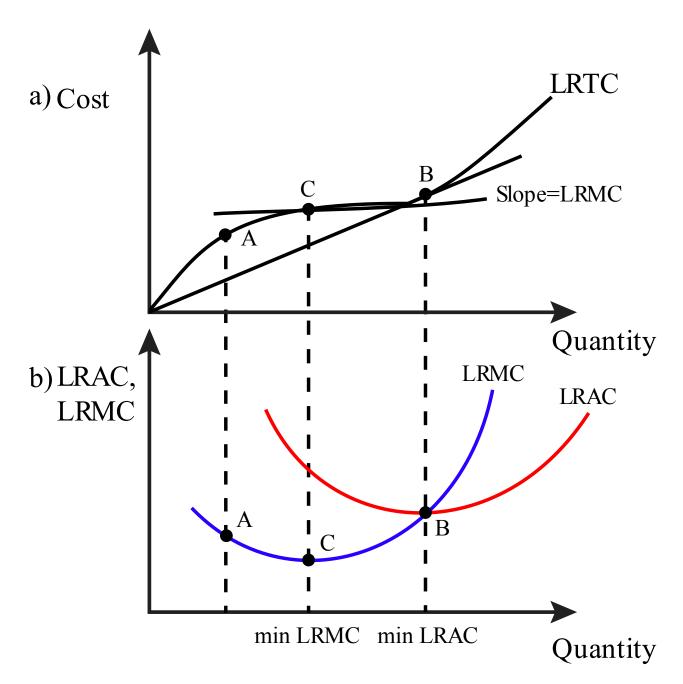


Figure 8.6 Deriving long-run average and marginal cost curves from the long-run total cost curve

To see how long-run total and average costs are related, take point A on the total cost curve in **figure 8.6**. At this point, we can derive the average cost by dividing the vertical distance, which gives us the total cost, by the horizontal distance, which gives us quantity. This is the same thing as the slope of the ray from the origin that connects to point A: it is the "rise" over the "run." So in panel b, we have the same quantity on the horizontal axis but the slope of the ray connecting to point A, or the average cost, on the vertical axis. Point A is, therefore, a point on the average cost curve. Note that as we move out along the total cost curve, the ray from the origin to the total cost curve becomes less and less steep until point B, after which the slope gets steeper. Thus point B is the point of minimum average cost, as illustrated in panel b.

To understand the relationship between long-run total cost and marginal cost, let's go back to point A in panel a. The marginal cost is the same as the slope of the total cost curve, and we can illustrate the slope by using a tangent line: a straight line that passes through point A and has the same slope as the curve at that point. This slope gives us the marginal cost. Note that this slope is not as steep as the ray from the origin that defined average cost at this point. Therefore, in panel b, the marginal cost is lower than the average. We can also observe that as we move along the total cost curve, the slope continues to decrease until point C, after which the slope begins to increase. Thus point C is the minimum marginal cost, as illustrated on the marginal cost curve in panel b.

Finally, note that at point B on the total cost curve, the slope of the ray from the origin and the slope of the total cost curve are identical. At this point, the marginal and the average costs are the same, as seen by the intersection of the two curves in panel b.

This relationship between average and marginal costs is not a coincidence; it is always true. When average cost is above marginal cost, average cost must be decreasing. When average cost is lower than marginal cost, average cost must be increasing. And when average and marginal costs are equal, average cost is not changing. This relationship is described in **table 8.2** and illustrated in **figure 8.7**.

Table 8.2 The relationship between long-run average and marginal costs

| Relationship between AC and MC | Resulting change in AC |
|--------------------------------|------------------------|
| AC(Q) < MC(Q) | AC(Q) increasing |
| AC(Q) > MC(Q) | AC(Q) decreasing |
| AC(Q)=MC(Q) | AC(Q) constant |

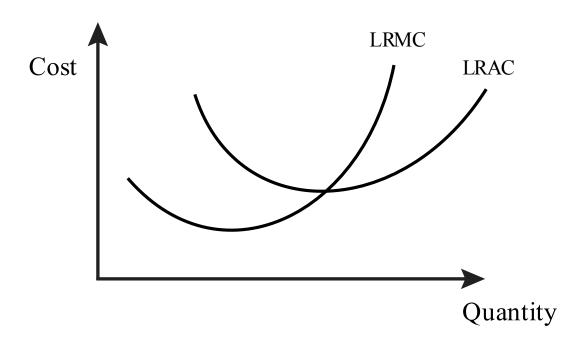


Figure 8.7 Relationship between the long-run average and marginal cost curves

On the left half of **figure 8.7**, the average cost is above the marginal cost, and thus the average cost is falling. In the right half of **figure 8.7**, the average cost is below the marginal cost, and thus the average cost is rising. At the intersection of the two curves, the average cost is at its minimum, and the slope of the average cost curve is zero.

Economies and Diseconomies of Scale

An important economic concept associated with the long-run average cost curve is economies of scale. **Economies of scale** occur when the average cost of production falls as output increases. Similarly, **diseconomies of scale** occur when the average cost of production rises as output increases. In a typical long-run average cost curve, there are sections of both economies of scale and diseconomies of scale. There is also a point or region of **minimum efficient scale** where average cost is at its minimum. This is the point where economies of scale are used up and no longer benefit the firm. **Figure 8.8** illustrates these points.

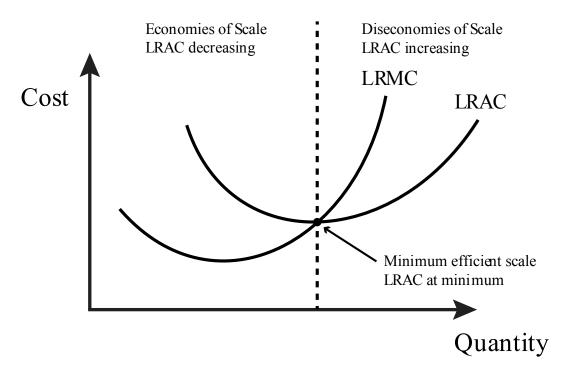


Figure 8.8 Economies, diseconomies, and minimum efficient scale

8.3 SHORT-RUN VERSUS LONG-RUN COSTS: THE ADVANTAGE OF FLEXIBILITY

Learning Objective 8.3: Explain why long-run costs are always as low as or lower than short-run costs and how more flexibility in choosing inputs is always better than less.

Short-run average costs are constrained by the presence of a fixed input. So in the long run, we can always do at least as well as, and often better than, what we do in the short run with respect to cost. We can see this is true by comparing the long-run and short-run average cost curves.

The long-run average cost curve is a type of lower boundary of the short-run cost curves. This can be understood most easily by thinking of a series of short-run average total cost curves, each one for a different level of the fixed input, capital, as shown in **figure 8.9**.

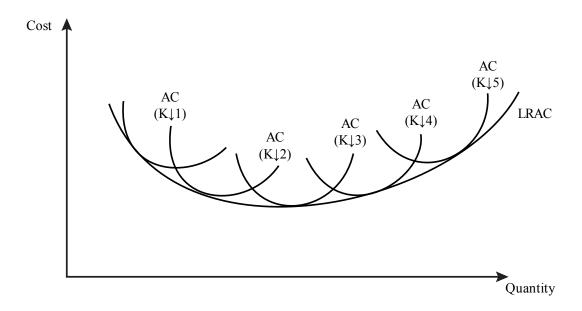


Figure 8.9 The long-run average cost curve as the lower boundary of short-run average cost curves

Since capital is variable in the long run, the long-run average cost is essentially the same as picking among the short-run average total cost curves and combining the capital with the optimal level of labor, or in other words, the minimum ATC.

The long-run average cost curve illustrates the benefit of flexibility: by being able to choose both inputs, the firm can ensure that the efficient mix of the inputs is being used at all times, which keeps costs at their minimum points for all output levels. This flexibility means that we can expect that in the long run, the average cost of production is at least as low as, and generally lower than, what it is in the short run.

8.4 MULTIPRODUCT FIRMS, LEARNING CURVES, AND LEARNING BY DOING

Learning Objective 8.4: Explain how making more than one product, learning over time, and learning by producing can lower costs.

A number of other factors matter in a firm's ability to lower costs. In this section, we look at two of them.

Multiproduct Firms

Often, a firm will make more than one product. This raises the interesting question, When is it better for the same firm to make multiple products than for multiple firms to each make one product? One answer lies in the concept of **economies of scope**: an economy of scope exists when the average cost of one product falls as the production of another product increases.

Take, for example, a firm that makes large LCD televisions. One expensive component of these displays is the flat glass panels needed for the screen. To make these large screens, very large pieces of glass are manufactured and then cut into individual rectangular pieces for the televisions. Often there are smaller glass pieces left over. Rather than discard these pieces, the same company can make smaller LCD displays for computers, cars, appliances, and so on. Since a lot of the other materials, technical know-

how, skilled labor, and the like can be shared across the two types of products, the average cost of both declines when the production of smaller LCD displays for computers is increased.

More formally, we can think of a multiproduct firm as having a cost function that depends on the output of two goods: Q_1 and Q_2 . Such a cost function can be expressed as $C(Q_1,Q+2)$. We say the economies of scope are present if

$$C(Q_1,Q_2) < C(Q_1,0) + C(0,Q_2)$$
.

This equation makes intuitive sense. The left-hand side of the inequality is the cost of a single firm that produced positive quantities of both goods. The right-hand side is the total cost of producing only Q_1 added to the total cost of producing only Q_2 . If it is cheaper to produce the two together, then the inequality holds.

Learning Curves

Sometimes firms get better at making things over time, as they gain experience. Economists call this learning by doing. Learning by doing means that as the cumulative output—the total output ever produced—of the firm increases, the average cost falls.

Learning by doing can take different forms:

- Over time, workers become more efficient at specific tasks they perform repeatedly.
- Managers can observe production and adjust task assignments and other aspects of the production process.
- Engineers can optimize product and plant design to increase efficiency.
- Firms can get better at handling inputs, materials, and inventories.

These and other instances of learning by doing often lower firms' average costs and make them more efficient over time.

The idea of learning by doing can be graphed as a learning curve (**figure 8.10**) where average cost is plotted as a function of either time or cumulative output. The learning curve is different from the typical average cost curve, which represents the total cost divided by current output.

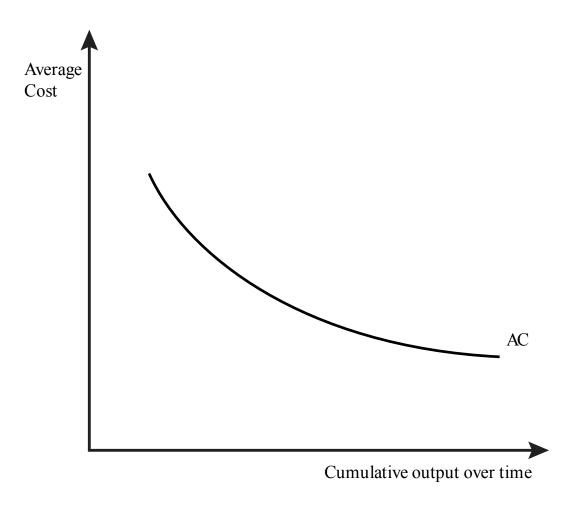


Figure 8.10 The learning curve

This temporal view of average costs makes firms' decisions about operating and investing in the business more complicated. If a firm that is considering shutting down in the face of negative economic profits expects that it will be able to produce more efficiently in the future, it might be willing to accept near-term losses in the expectation of future profits.

The learning curve is potentially important in the policy question. If there is substantial learning involved in the production of a streetcar, then the domestic manufacturer of streetcars might see its production costs decrease significantly as they produce more and more streetcars. So although the short-run costs of production might suggest that domestic promotion is a bad idea, if there is good reason to believe that in the long run, average costs will decrease significantly, a reasonable case could be made for such promotion.

8.5 POLICY EXAMPLE

SHOULD THE FEDERAL GOVERNMENT PROMOTE DOMESTIC PRODUCTION OF STREETCARS?

Learning Objective 8.5: Use a cost analysis to explain why building streetcars domestically in the United States is or is not a good policy.

To understand the business of building streetcars, we must first think about the cost structure. Streetcars are large, heavy, and loaded with specific and sophisticated technology, such as electric propulsion engines, car electronics and controls, and passenger controls. Their manufacture takes a factory of considerable size, and yet they are produced in small quantities. This suggests a few things about their costs:

- There are very large fixed costs because of the machinery and the plant required for constructing these cars. Because of this, the minimum efficient scale is probably far beyond any one manufacturer's current scale. What this means is that the more streetcars a manufacturer produces, the lower the cost per car.
- Because of the complexity, there are likely to be large cost savings over time as a result of learning by doing.
- The complexity of the streetcar itself suggests that the quality of the product from new firms might suffer because they have not had the experience that longtime suppliers have had.

These observations suggest that current suppliers of streetcars, like Siemens, have considerable cost advantages over new firms because of their current production level, which allows them to take advantage of economies of scale, and because they are much farther along the learning curve (see **figures 8.10** and **8.12**). Any new firm likely would take a very long time to reach the current manufacturer's scale efficiencies and cost efficiencies from learning by doing. However, if the demand for streetcars was expected to grow and be sustained for a long period of time, a reasonable case could be made that the domestic industry could mature into a reliable and cost-efficient supplier of streetcars to the United States and even the international market.

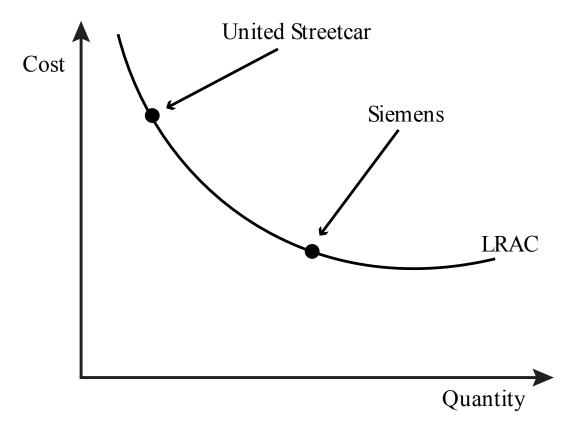


Figure 8.11 Streetcar manufacturers on the long-run average cost curve

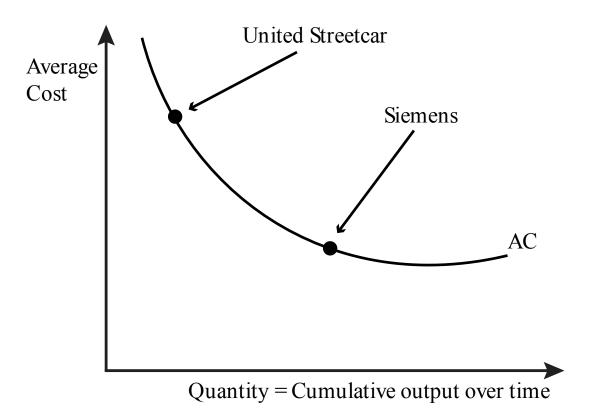


Figure 8.12 Streetcar manufacturers on the learning curve

Unfortunately, the projections of the level of demand for streetcars appear to have been far too optimistic. It seems unlikely that the domestic streetcar industry will have a chance to grow and learn, so we may never know if it would have become cost competitive over time.

EXPLORING THE POLICY QUESTION

- 1. Because of their size and weight, shipping streetcars internationally is costly. How would you include transportation costs in your analysis of the policy question?
- 2. If the market had not dried up, do you think United Streetcar would have succeeded in the long run? Why or why not? Use economic reasoning in your answer.

8.1 Short-Run Cost Curves Learning Objective 8.1: Derive the seven short-run cost curves from the total cost function. 8.2 Long-Run Cost Curves Learning Objective 8.2: Derive the three long-run cost curves from the total cost function.

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8.3 Short-Run versus Long-Run Costs: The Advantage of Flexibility

<u>Learning Objective 8.3</u>: Explain why long-run costs are always as low as or lower than short-run costs and how more flexibility in choosing inputs is always better than less.

8.4 Multiproduct Firms, Learning Curves, and Learning by Doing

<u>Learning Objective 8.4</u>: Explain how making more than one product, learning over time, and learning by producing can lower costs.

8.5 Policy Example

Should the Federal Government Promote Domestic Production of Streetcars?

<u>Learning Objective 8.5</u>: Use a cost analysis to explain why building streetcars domestically in the United States is or is not a good policy.

LEARN: KEY TOPICS

Terms

Fixed cost

The cost of production that does not vary with output level. The fixed cost is the cost of the fixed inputs in production, such as the cost of a machine (capital) that costs the same to operate no matter how much production is happening, i.e., a conveyor belt in a factory that moves a streetcar chassis through various stages of an assembly line. The belt is either on or off, but the cost of running it does not change depending on how many streetcars it carries at any point in time.

Variable cost

The cost of production that varies with output level. This is the cost of the variable inputs in production—i.e., the cost of the workers that assemble the electronic devices along a conveyor belt. The number of workers might depend on how many devices the factory is trying to produce in a day. If its production target increases, it uses more labor, thus the hourly wages it pays for these workers are a variable cost. Variable cost generally increases with the amount of output produced.

Total cost

The sum of fixed and variable costs of production.

Average fixed cost

The fixed cost per unit of output.

Average variable cost

The total cost per unit of output. This is the same as the sum of the average fixed cost and the average variable cost.

Average total cost

The total cost per unit of output. This is the same as the sum of the average fixed cost and the average variable cost.

Marginal cost

The additional cost incurred from the production of one more unit of output.

Long-run total cost

In the long-run, all costs are variable. This represents the total cost of all previously fixed and variable inputs.

Long-run average cost

The cost per unit of output. In other words, it is the total cost, LRTC, divided by output, Q.



The increase in total cost from an increase in an additional unit of output.

Expansion path

A curve that shows the cost-minimizing amount of each input for every level of output.

Economies of scale

When the average cost of production falls as output increases,

Diseconomies of scale

When the average cost of production rises as output increases.

Minimum efficient scale

The point on a cost curve where average cost is at its minimum. This is the point where economies of scale are used up and no longer benefit the firm.

Economies of scope

When the average cost of one product falls as the production of another product increases.

Learning by doing

As the cumulative output—the total output ever produced—of the firm increases, the average cost falls.

Learning curve

The graph of a firm's process of learning by doing. Differs from the typical average cost curve; this is plotted as a function of time or cumulative output.

Graphs

Three short-run cost curves: fixed, variable, and total costs

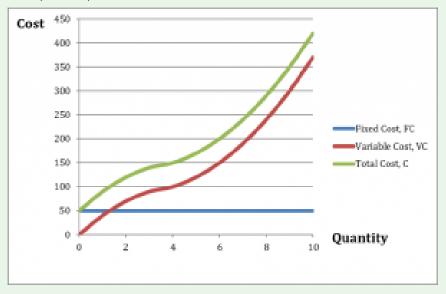


Figure 8.1 Three short-run cost curves: fixed, variable, and total costs

The total product of labor curve

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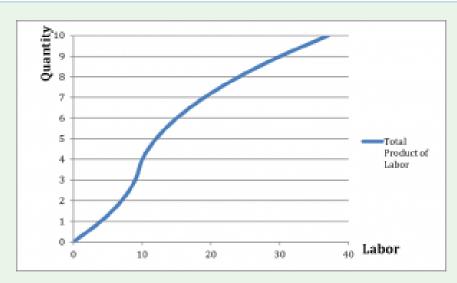


Figure 8.2 The total product of labor curve

Marginal cost, average fixed cost, average variable cost, and average total cost

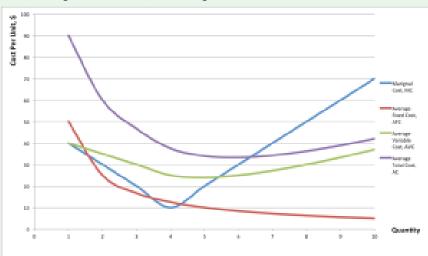


Figure 8.3 Short-run marginal cost, average fixed cost, average variable cost, and average total cost curves

Expansion path

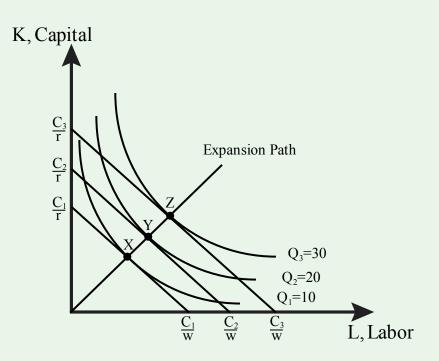


Figure 8.4 Expansion path

The long-run total cost curve

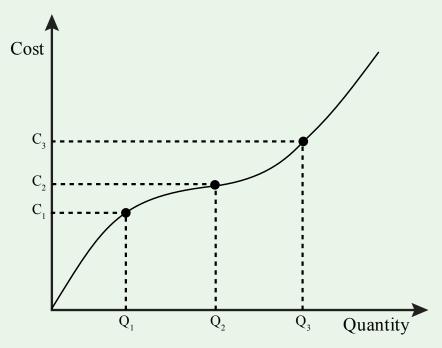
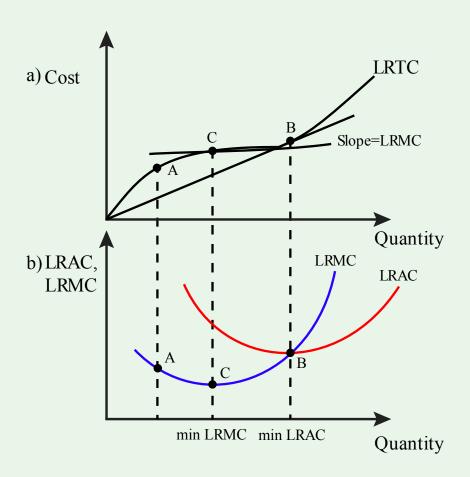


Figure 8.5 The long-run total cost curve

Deriving long-run average and marginal costs curves from the long-run total cost curve

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8.6 Deriving long-run average and marginal cost curves from the long-run total cost curve

Relationship between the long-run average and marginal cost curves

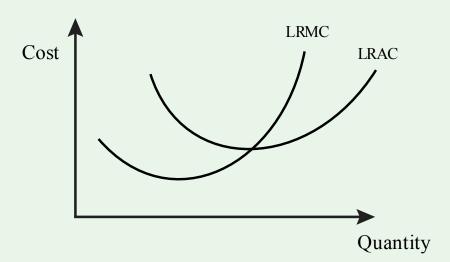


Figure 8.7 Relationship between the long-run average and marginal cost curves

The long-run average cost curve as the lower boundary of short-run average cost curves

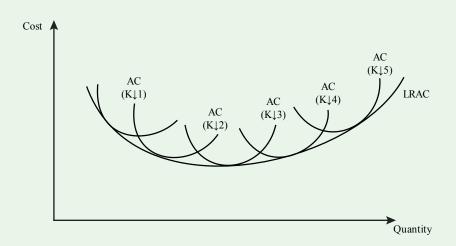


Figure 8.9 The long-run average cost curve as the lower boundary of short-run average cost curves

The learning curve

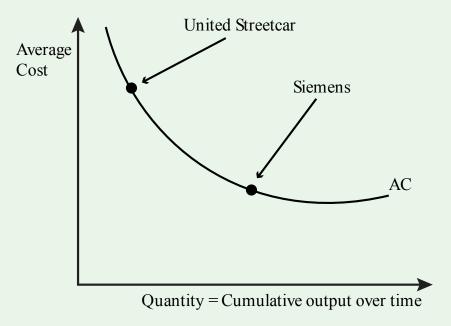


Figure 8.12 Streetcar manufacturers on the learning curve

Equations

Short Run Cost Equations

Fixed Cost

Lacks an exact equation: the fixed cost in the context of short-run curves is the cost even when the output is at zero.

Variable cost

Variable cost varies with output level. Variable costs generally increase with the amount of output produced.

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Total cost

The sum of fixed and variable costs of production.

$$C = FC + VC$$

Average fixed cost

The fixed cost per unit of output.

$$AFC = FC/Q$$

Average variable cost

The variable cost per unit of output.

$$AVC = VC/Q$$

Average total cost

The total cost per unit of output. The sum of the average fixed cost and average variable cost

$$AC = AC/Q = AFC + AVC$$

Marginal cost

The additional cost incurred from the production of one more unit of output.

$$MC = rac{\Delta C}{\Delta Q}$$

Because the only part of total cost that increases with an additional unit of output is the variable cost, we can re-write the marginal cost as

$$MC = rac{\Delta VC}{\Delta Q}$$

Long-run Cost Equations

Long-run cost minimization problem, review.

Long-run cost minimization problem

The slope of the isoquant is the MRTS, and the slope of the is

$$-w/r$$

So the solution to the long-run cost minimization problem is

$$MRTS = -\frac{w}{r}$$

or

$$rac{MP_L}{w} = rac{MP_K}{r}$$

This formula has many different <u>calculus</u> derived conclusions that can be reviewed in <u>chapter 7</u>.

Long-run Total Cost

The sum of the all input costs

$$LTRC = wL + rK$$

Long-run average cost (LRAC)

The cost per unit of output. Because there is no fixedcost in the Long-run, it is the total cost LRTC, divdied by output Q.

$$LRAC(Q) = rac{LRTC(Q)}{Q}$$

Long-run marginal cost

The increase in total cost from an increase in an additional unit of output.

$$LRMC(Q) = rac{\Delta LRTC(Q)}{\Delta Q}$$

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CHAPTER 9

Profit Maximization and Supply

THE POLICY QUESTION

WILL A CARBON TAX HARM THE ECONOMY?

Carbon emissions in the atmosphere due to human activity have been identified as the key component of global warming. We know from earlier chapters that the cost of consumption influences human choices. Therefore, a very popular policy proposal to address global warming is to impose a tax on carbon at the source. For example, the state of California and the Canadian province of British Columbia began imposing a carbon tax in 2015 and 2008, respectively. Carbon taxes generally increase the price of fossil fuels, which have a large carbon component. The result is an increase in energy prices for all users. Critics of these policies suggest that carbon taxes would have an adverse impact on the economy greater than any potential benefit.

To analyze the impact on the economy, we must start with the individual actors upon which the economy depends: the firms themselves. This chapter examines how firms make decisions about how much to produce and how their profits are determined. Once we have developed a general model, we can use it to analyze the impact of a carbon tax on individual firms, understand the firm-level implications of the tax, and know the right questions to ask when trying to determine the cost and benefits of a carbon tax.

In this chapter, we will study the supply side of markets: how firms' cost conditions define and affect their supply curves and the market supply curve. By summing up all producers' supply curves within a given industry, we can construct a market supply curve just as we constructed the market demand curve from individual demand curves. When we have both market demand and market supply, we will be able to study market equilibrium in section 9.3.

EXPLORING THE POLICY QUESTION

How does a tax on carbon affect individual firms' output and profits?

LEARNING OBJECTIVES

9.1 Output Decisions for Price-Taking Firms

Learning Objective 9.1: Explain how competitive, price-taking firms decide on output levels.

9.2 Short-Run Supply

Learning Objective 9.2: Describe how competitive firms make decisions on short-run output and whether to shut down if they experience negative profit.

9.3 Long-Run Supply and Market Equilibrium

<u>Learning Objective 9.3</u>: Describe competitive firms' long-run supply curves and how firms' entry and exit affect the long-run market equilibrium.

9.4 Heterogeneous Firms and Increasing and Decreasing Cost Industries

Learning Objective 9.4: Demonstrate how increasing and decreasing cost industries affect the long-run market supply curve.

9.5 Policy Example
Will a Carbon Tax Harm the Economy?

<u>Learning Objective 9.5</u>: Predict the effect of a carbon tax on the supply and profit maximization decisions of firms on which it is imposed.

9.1 OUTPUT DECISIONS FOR PRICE-TAKING FIRMS

Learning Objective 9.1: Explain how competitive, price-taking firms decide on output levels.

Before considering the production decisions of firms, we need to understand a few foundation ideas. First, we are focusing on the behavior of price-taking firms. A firm is said to be a **price taker** when it has no ability to influence the price the market will pay for its product; it must take the *market price* as determined by the laws of supply and demand in a competitive market. A **perfectly competitive** market is a market in which there are many firms so that each individual firm's output has no impact on market equilibrium, output is identical across firms, firms have the same access to inputs and technology, and consumers have perfect information about prices. All firms in a perfectly competitive market are price takers.

Second, we are focusing on firms that are motivated by profit. Many publicly and privately owned firms have one main objective: to maximize profits. Not-for-profit firms seek to maximize some other objective, like providing a social service such as mental health care to the greatest number of people in need, but these are a tiny fraction of all firms in the world. In this chapter, we will assume that firms' objectives are to maximize profits.

A firm's **profit** (π) is the difference between its total revenue and its total cost:

(9.1)
$$\pi(Q) = TR(Q) - C(Q)$$

The total revenue is the quantity of the goods produced multiplied by the sales price of those goods.

$$TR(Q) = PQ$$

The total cost is the total cost curve C(Q) introduced in <u>chapter 7</u> and represents the **economic cost**. The economic cost is the cost inclusive of all opportunity costs, so it includes both explicit costs and implicit costs. This is distinct from the **accounting cost**, which includes only the explicit costs, or those you would see in an accounting spreadsheet of the firm's costs. So equation (9.1) is an expression of the

economic profits of the firm, which consider economic costs. In economics, we focus exclusively on economic profits because this is the relevant measure when it comes to decision-making.

To understand the difference between accounting cost and economic cost, imagine deciding whether to open up and run a small business making and selling soap infused with organic botanicals. Suppose you figure that your business will achieve annual sales of \$230,000 and your out-of-pocket cost for the ingredients, equipment rental, property rental, and so on is \$155,000 annually. Your accounting profits after a year would be \$230,000-\$155,000=\$75,000, a pretty decent return.

But should you go ahead and start the business? To answer that, you need to think about your opportunity cost. What would you do instead if you decided not to start your own business? Imagine that your friend has offered to hire you to work in her firm, and she will pay you an annual salary of \$90,000. Imagine also that you think you would be equally satisfied working with your friend as running your own business. With this in mind, your annual economic costs of running your business is \$155,000+\$90,000=\$245,000. So your annual economic profit would be \$230,000-\$245,000=-\$15,000. The answer is now clear—your best decision is not to run a business making soap but to work with your friend.

Let's now turn to the output choice of a profit maximizing, price-taking firm. The objective of maximizing profit means that firms must choose the output level that maximizes the difference between total revenue and total profit. To determine this specific level of output, the firm must ask how the production of one more unit of output contributes to both the total revenue and the total cost. For example, if a car manufacturer can produce one more car at a marginal cost of \$15,500 and sell that car for a marginal revenue of \$17,000, it knows that by producing the extra car, its profits will increase by \$1,500. Note that this is not the same as knowing that profits are positive because the calculation does not include fixed costs. Similarly, if the additional car has a marginal cost of \$18,000 to produce and can be sold for \$17,000, then the manufacture and sale of this car would reduce profits by \$1,000.

The term **marginal revenue** (MR), used in our example above, refers to the change in total revenue from a one-unit change in quantity produced. Marginal revenue is expressed as

$$MR = \Delta TR/\Delta Q$$
.

For a price-taking firm, this increase in revenue from the sale of an additional unit is exactly the price of that unit. In other words, for a price-taking firm, MR=P.

Any profit maximizing firm would like to continue to increase output as long as marginal revenue is larger than marginal cost. A profit maximizing firm would also like to reduce output as long as marginal revenue is lower than marginal cost. The incentive

Calculus

The marginal revenue is the rate of change of total revenue as output increases, or the slope of the total revenue functions, TR(Q). To find this, we take the derivative of the total revenue function:

$$MR(Q) = rac{dTR(Q)}{dQ}.$$

to increase or decrease output stops exactly when marginal revenue equals marginal cost. This is known as the *profit maximization rule*: profit is maximized when output is set where marginal revenue equals marginal cost.

From chapter 8, we learned that marginal cost (MC) is the additional cost incurred from the production of one more unit of output:

$$MC = \Delta C/\Delta Q$$

Since the profit maximizing rule stipulates that output should be set where marginal revenue equals marginal cost and since marginal revenue for a price-taking firm is the price of the good, we know that at the profit maximizing output level for the firm,

$$P = MC(Q)$$
.

The expression P=MC(Q) gives us a relationship between the price, P, of a good and the quantity, Q, that a profit maximizing, price-taking firm will produce at that price. In other words, it gives us the individual firm's supply curve. **Figure 9.1** illustrates this relationship.

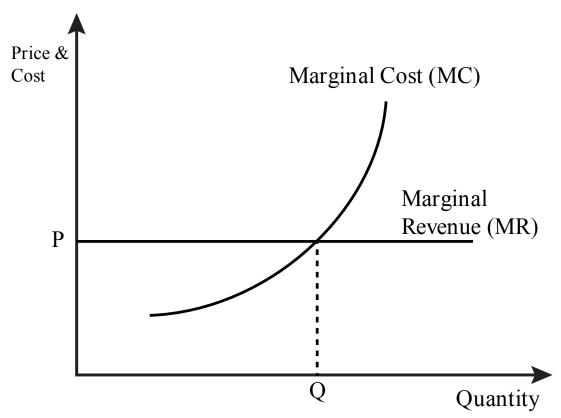


Figure 9.1 Profit maximization for a price-taking competitive firm

In **figure 9.1**, we see that the firm's profit maximizing level of output is where marginal revenue equals marginal cost. For a price-taking firm, marginal revenue is equal to the price. So as price increases, the firm will increase production, and when the price decreases, the firm will decrease production.

9.2 SHORT-RUN SUPPLY

Learning Objective 9.2: Describe how competitive firms make decisions on short-run output and whether to shut down if they experience negative profit.

To understand the short-run supply decision of the firm, we have to be able to measure the firm's profits. The profit maximization rule, to set output so that marginal revenue equals marginal cost, ensures that the firm is maximizing profit, but it does not ensure that the firm is making positive profits. In other words, following the MR=MC rule means that the firm is doing the best it can, which could be minimizing losses instead of making positive profits.

To see how we go from the output decision to profits, consider the following:

$$\Pi = TR - TC$$

$$TR = PQ \ TC = ATC imes Q \ (ext{since } ATC = rac{TC}{Q})$$

Thus,

$$\Pi = (PxQ) - (ATC \times Q)$$

= $(P - ATC)Q$.

Since Q^* , the quantity for which MR=MC, is always positive or zero, whether profit (π) is positive or negative depends on the price (P) relative to the average total cost at that particular $Q^*(ATC^*)$. If $P>ATC^*$, then $\pi>0$, as seen in **figure 9.2**. In the figure, profits (π) are represented graphically by the shaded area. Notice that the height of the rectangular shaded area is P-ATC and the width is Q. Since the area of a rectangle is height times width, the area of this rectangle equals the profit.

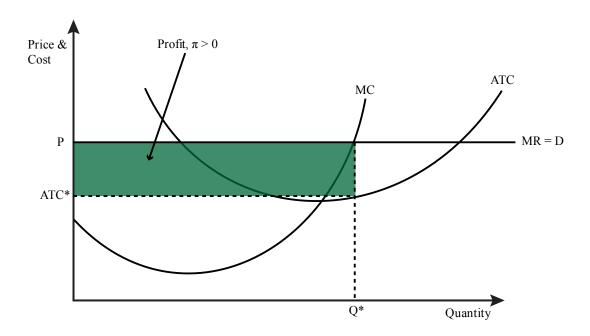


Figure 9.2 Positive profit [latex]P \gt ATC^*[/latex]

If $P=ATC^*$, then $\pi=0$, as seen in **figure 9.3**.

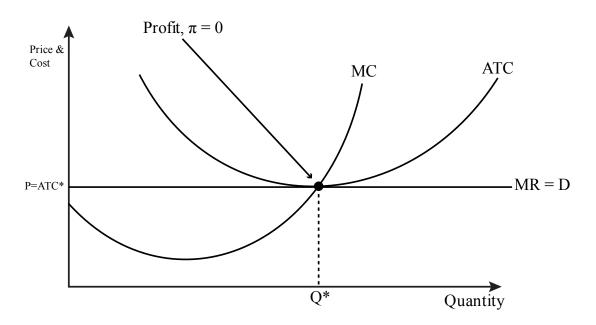


Figure 9.3 Zero profit [latex]P=ATC^*[/latex]

If $P < ATC^*$, then $\pi < 0$, as seen in **figure 9.4**.

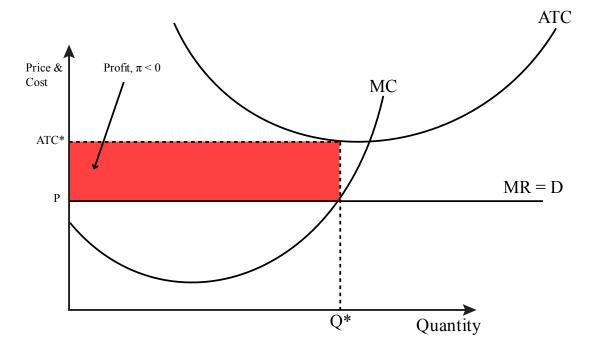


Figure 9.4 Negative profit (loss) [latex]P \lt ATC^*[/latex]

It is tempting to think that if profit is negative, the firm should immediately shut down or cease production of the good. But remember that in the short run, there are fixed inputs that cannot be adjusted immediately. For example, suppose the soap-selling business requires the leasing of a storefront. This is a three-month lease, and three monthly payments of \$1,000 each must be made regardless of whether the store is open or closed. Now suppose that the business is making enough revenue to cover all the

variable costs, like the ingredients for the soap, the electricity bill, your own salary, and *part* of the lease, perhaps \$500 of the \$1,000. If you continue to operate the store, you will lose \$500 per month—the part of the lease payment not covered by revenues. If you shut down, you will lose \$1,000 per month until the lease runs out, because although there are no variable costs, there also is no revenue.

Consider the following expression for profit:

$$\pi = TR - TC \ = TR - FC + VC \ = TR(Q) - FC - VC(Q)$$

The third line in this expression shows that TR and VC are both functions of Q, so if Q=0, then TR=0 and VC=0 as well. Shutting down means to set Q=0.

The level of profit if the firm shuts down is $\pi=0-FC-0=-FC$.

So in the short run, a firm should only shut down if the total revenue is lower than the variable cost, which is the same as the price being lower than the average variable cost.

Figure 9.5 illustrates the situation where the firm is generating a negative profit but should continue to operate in the short run. At Q^* , the firm is making negative economic profits because $(P-ATC^*)$ is negative $\pi=(P-ATC^*)Q^*$). However, the firm is covering all its variable costs $(P>AVC^*)$ and part of its fixed costs. Of course, when the short run ends because the firm is able to adjust its previously fixed input, the firm should shut down if its total revenue is still lower than its total cost.

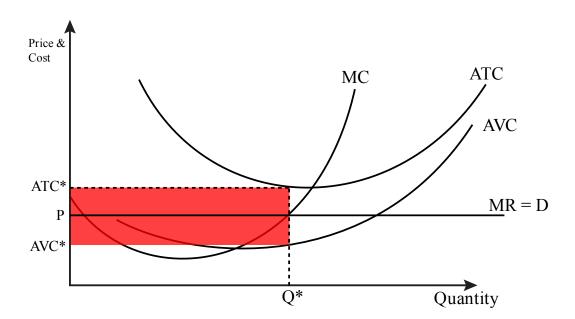


Figure 9.5 Negative profit, but in the short run, firm should continue to operate.

This understanding of the short-run output decision allows us to derive the firm's short-run supply curve. As long as the market price is above the firm's average variable cost, the firm will choose to produce an output where P=MC. In other words, the firm's marginal cost curve above the AVC curve is the firm's supply curve. When price is below AVC, the firm chooses not to produce any output at all, so the supply for prices below AVC is zero. **Figure 9.6** illustrates the firm's short-run supply curve.

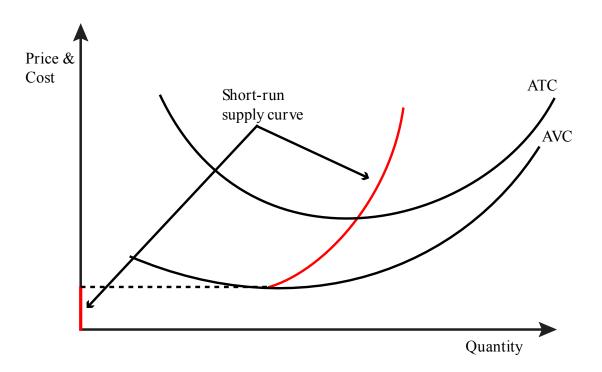


Figure 9.6 Competitive firm's short-run supply curve

Every firm in a given industry has a short-run supply curve, but its precise shape depends on the firm's cost structure—the shape and location of its MC and AVC curves. Because each individual firm supplies a certain amount of output at every price, we can derive the industry supply curve by simply adding up these outputs across all firms in the industry. When we do this, we must take care to sum the quantities at every price, not the other way around.

Figure 9.7 shows how summing up all individual short-run supply curves yields the industry short-run supply curve, which represents the quantity supplied in the short run at every price.

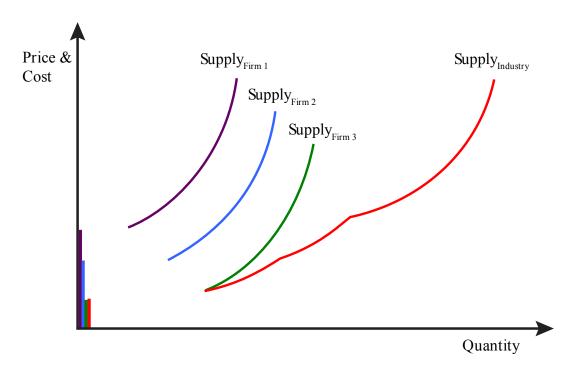


Figure 9.7 Deriving an industry short-run supply curve

9.3 LONG-RUN SUPPLY AND MARKET EQUILIBRIUM

Learning Objective 9.3: Describe competitive firms' long-run supply curves and how firms' entry and exit affect the long-run market equilibrium.

In the long run, firms do not have any fixed costs; all production costs are variable. So a firm's profitability is determined solely by the long-run average total cost curve. A profit maximizing firm still sets output so that marginal revenue equals marginal cost, and since marginal revenue for a perfectly competitive firm is equal to the market price, the marginal cost curve above the long-run average total cost curve (LRATC) represents the firm's supply curve.

As in the short-run case, the firm's profits depend on the price relative to the long-run average total cost at the optimal output level for the firm, Q^* . In **figure 9.8**, the price is above LRATC, so the firm is making positive profits. As long as profits are not negative, the firm will continue to produce.

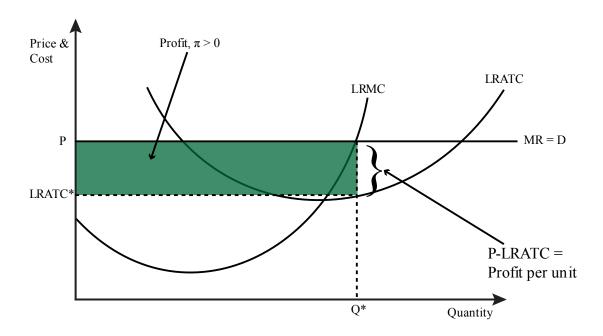


Figure 9.8 Positive profits in the long run

So the portion of the long-run marginal cost (LRMC) that lies above the LRATC is the firm's supply curve, as seen in **figure 9.9**.

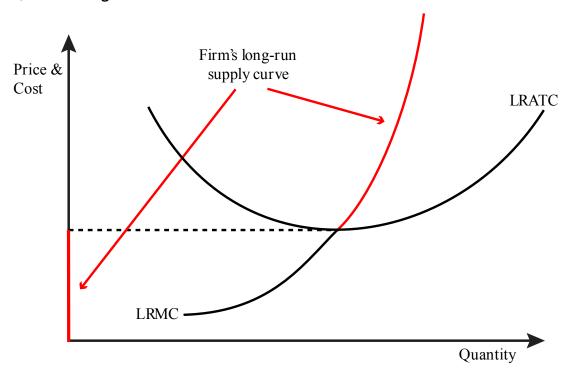


Figure 9.9 The long-run supply curve of a perfectly competitive firm

To derive the long-run market supply curve, we have to think about how firms enter and exit industries in the long run. We assume perfectly competitive industries have **free entry** and **free exit**: there are no special costs, such as technical or legal barriers, to firms entering and exiting the industry. This assump-

tion is critical to perfect competition. Barriers that block firms from entering or exiting will create an environment that has only limited competition.

Barriers to Free Entry and Free Exit

Barriers to entry and exit can be legal, such as patents that limit the production of a good to the firm that invented it, or technical, such as the cost of setting up a network of wires to homes for a company that wishes to provide cable television services. We will study such barriers in more detail when we discuss monopolies in <u>chapter 16</u>.

If free entry and exit exist, the next question to answer is, **When will firms choose to enter and exit a market?** To answer this question, we will assume for now that all firms in a market are homogeneous—that is, they have identical technologies and cost structures, or more simply, they all have the same LRATC and LRMC curves. We will examine firms that have different costs in the next section of this chapter.

Figure 9.8 illustrates the case where the market price is such that the firm is making positive profits. Positive profits in this case mean that the firm is getting better than normal returns or that this is an exceptionally profitable market to be in. Other firms, not currently in the market, will see these profits and decide that this is a good market to enter. When new firms enter the market, they provide their output to the total supply, and the market supply increases.

As illustrated in **figure 9.10**, as new firms, drawn by positive profits, enter the market, the added supply lowers the **equilibrium price**—the price at which quantity demanded equals the quantity supplied. This lowering of the equilibrium price lowers all firms' profits.

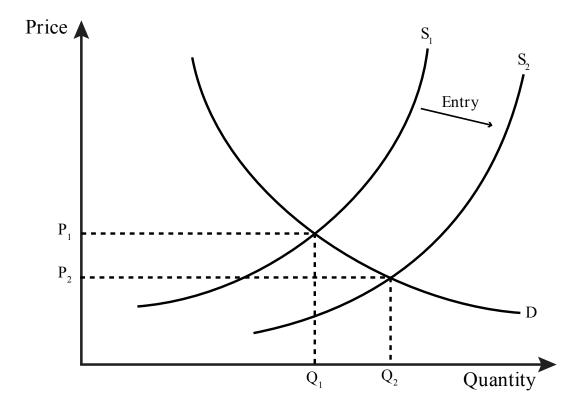


Figure 9.10 New entrants increase market supply and lower equilibrium price.

Entry will continue to occur as long as firms' profits are positive, and so this process will continue until the equilibrium price has reached the point where the LRATC and the LRMC cross, or where there are zero profits, as shown in **figure 9.11**.

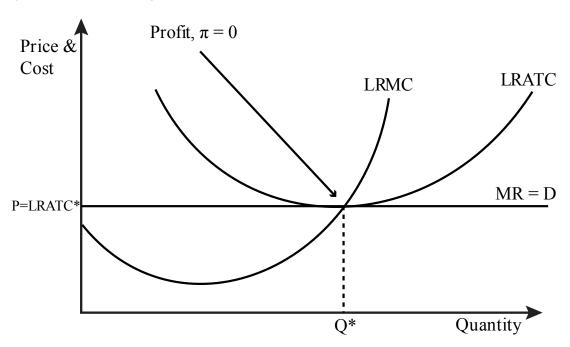


Figure 9.11 Equilibrium with zero profits

Equilibrium with zero profits actually includes two kinds of equilibrium:

- 1. A market equilibrium where the price equates the quantity supplied to the quantity demanded
- 2. An *equilibrium in the number of firms in the market*, as the zero profit experienced by the existing firms in the market does not attract any new entrants

The market exit dynamics work similarly to the market entry dynamics. Firms that are currently producing and supplying their output to a market where the equilibrium price is below their LRATC are making negative profits, which by the definition of opportunity cost means that other opportunities exist that yield higher returns. This fact will cause the existing firm to want to exit the market.

A firm's profit is negative when the equilibrium price is below the firm's LRATC at its profit maximizing level of output. In this case, profit maximization is synonymous with loss minimization—the firm is making the best output choice it can. **Figure 9.12** illustrates a situation of long-run negative profits for a firm.

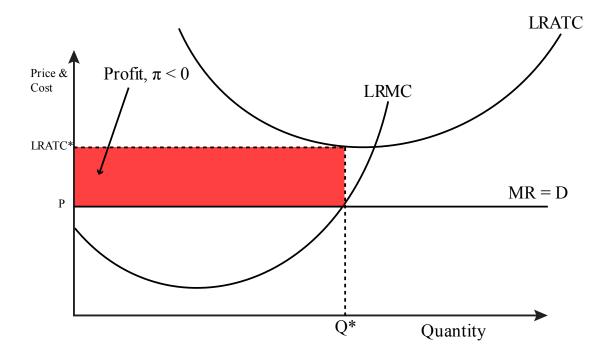


Figure 9.12 Negative profits in the long run

Will all firms exit the market when profits are negative? No, because as the first firms exit the market, supply will fall, and the equilibrium price will rise. **Figure 9.13** illustrates this behavior graphically. Once the price rises to the point where it equals LRATC, there will no longer be an incentive for firms to leave the market.

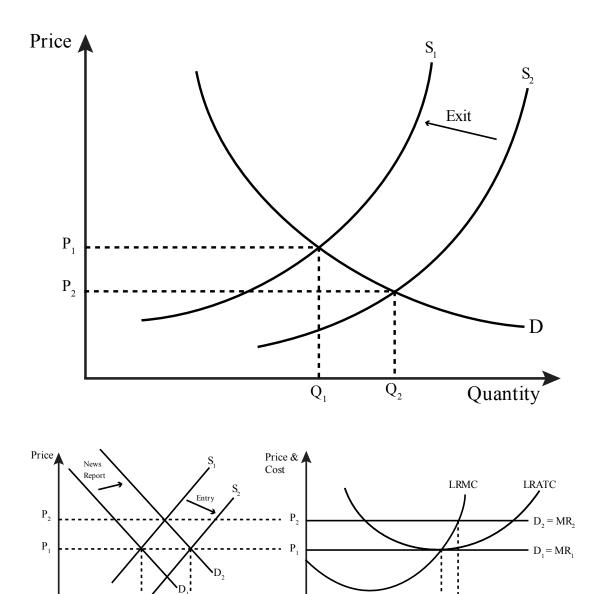


Figure 9.13 Exiting firms cause a market supply decrease and a rise in the equilibrium price

The long-run entry and exit dynamic allows us to understand the long-run market supply curve. Entry and exit dynamics will always force the price back to P_1 in the long run, as new firms enter to satisfy any new demand and existing firms exit when demand falls. The resulting long-run supply curve is horizontal, as shown in **figure 9.14**.

Quantity

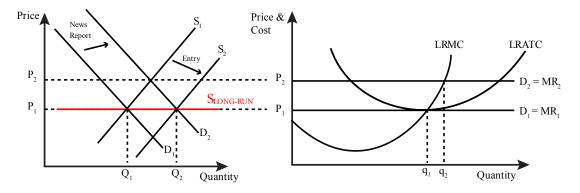


Figure 9.14 The long-run market supply curve

9.4 HETEROGENEOUS FIRMS AND INCREASING AND DECREASING COST INDUSTRIES

Learning Objective 9.4: Demonstrate how increasing and decreasing cost industries affect the long-run market supply curve.

In the previous section, we explicitly assumed homogeneous firms—that is, firms all having identical costs. We also assumed, implicitly, that costs were constant as industry output changed. In this section, we will study what happens when these assumptions do not hold.

Consider first a number of firms that all produce the same good but that all have different costs—that is, heterogeneous firms. It makes sense that the firms with the lowest costs would be the first to provide their output to the market and that they would experience positive profit. Their success would attract new entrants to the market, just as in the case of homogeneous firms. Each new entrant can be expected to be the next lowest-cost firm. Entry will continue until profits reach zero for the most recent entrant, causing it to become the last entrant.

Zero profits will happen when the supply increases enough to push price down to equal the marginal cost of the very last entrant. Since the entrants that came before the last one all have lower costs, they will all continue to experience positive profits. No other firms will enter after the last zero-profit entrant because they are, by assumption, higher-cost firms and will earn negative profits if they do so. After profits reach zero, new entrants will be drawn in only if the price rises.

In the case of heterogeneous firms, the long-run supply curve will be upward sloping, even in the case of perfect competition, as seen in **figure 9.15**.

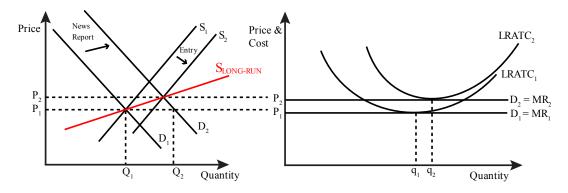


Figure 9.15 Long-run supply in the case of firms with different costs

The second assumption that was implicit in the previous section is that firms are in a **constant-cost industry**: industries where firms' costs do not change as industry output changes. So no matter how much total output there is in the industry, all the LRATC curves remain in the same place.

This assumption does not hold for many industries. Some industries are **increasing-cost industries**: industries where firms' costs increase as industry output increases. This can happen because as an industry expands the demand for inputs or industry-specific capital increases, which can cause the prices to rise. For example, if the demand for coffee increases due to positive news about the health benefits of consumption, the demand for coffee beans will increase as well, which could lead to an increase in their price. As the industry output increases, the costs of all firms will increase, and the long-run supply curve will slope upward, as shown in **figure 9.16(a)**.

Other industries might be **decreasing-cost industries**: industries where firms' costs decrease as industry output increases. This could be because these industries have increasing returns to scale or because increased demand for inputs and capital leads to increased returns to scale on the part of the firms that supply these goods. For example, if the demand for coffee increases the demand for espresso machines, espresso machine manufacturers might invest in cost-saving technologies, such as automating parts of the assembly process. As the coffee industry output increases, the cost of espresso machines decreases, the costs of coffee shops decrease, and the long-run supply curve would be downward sloping, as shown in **figure 9.16(b)**.

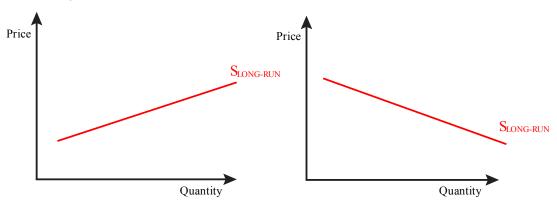


Figure 9.16 Long-run supply curves for increasing and decreasing cost industries

The heterogeneity of a firm's cost structures and the fact that many or most industries could be described as increasing cost industries lead economists to generally draw the market supply curve as upward sloping. From the information learned in this chapter, you can now see that the market supply curve comes from the firms themselves.

9.5 POLICY EXAMPLE

WILL A CARBON TAX HARM THE ECONOMY?

Learning Objective 9.5: Predict the effect of a carbon tax on the supply and profit maximization decisions of firms on which it is imposed.

On July 1, 2008, in response to mounting evidence that human activity is contributing to global climate change and that carbon emissions are a key factor in rising earth temperatures, the Canadian province of British Columbia began collecting a tax on carbon emissions. In so doing, British Columbia became the first North American jurisdiction to levy a carbon tax.

The government of British Columbia charges a tax on revenue from the sale of all fuels: gasoline, diesel, natural gas, propane, jet fuel, and coal. This tax is neutral, meaning the proceeds are returned to the citizens of the province through a reduction in income taxes and tax credits.

Though a carbon tax is a popular policy proposal for groups concerned about climate change and greenhouse gases, pro-business groups generally resist it, arguing that carbon taxes would do great harm to the economy. In this chapter, we have studied how cost conditions translate into firm and market supply. Given this analysis, we can come up with a prediction about the way that a carbon tax would affect firms' production behavior.

Carbon taxes raise the price of energy, which is a production input. Energy usage generally, but not always, varies with the level of output. More intense production is generally associated with higher energy use. So we can assume that the energy input of firms is a variable cost. This means that an increase in the cost of energy will increase not only the total costs of the firms but their marginal costs as well. In **figure 9.17**, we can see the resulting impact on firms and their marginal cost curves.

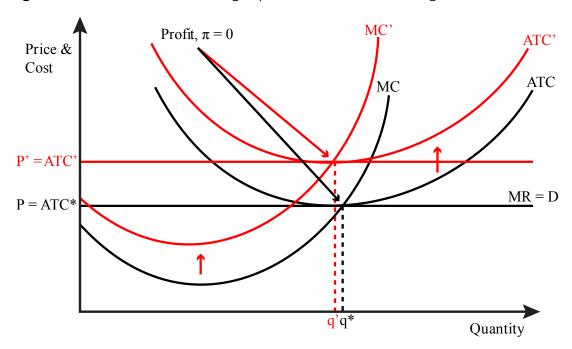


Figure 9.17 Effect of an increase in variable cost

From this we can anticipate that firms' supply curves will rise and that the new equilibrium price will increase. So business groups have a legitimate point in worrying about the effect of a carbon tax on firms' costs. The effect on an individual firm is clear from **figure 9.17**—this tax will lead it to charge higher prices and reduce output.

However, this is only part of the story. Revenue-neutral carbon taxes will increase demand through income tax rebates and credits, which would serve to raise the equilibrium price. This could offset, at least in part, the rise in costs. A true analysis of this policy would also include the economic impact of climate change itself and the benefit of carbon mitigation. This is a subject we will return to in chapter 20, "Externalities."

EXPLORING THE POLICY QUESTION

1. If a carbon tax is imposed, the costs in a perfectly competitive industry would likely rise. If

firms make zero profits prior to the tax and zero profits after the tax, is it correct to say that there is no net effect of the tax?

- 2. Another policy response to combat carbon emissions is to mandate reductions in energy usage on the part of firms. Using the theory of profit maximizing competitive firms, analyze the impact of this alternate policy.
- 3. What else would you want to know about carbon emissions, climate change, and the economy to give a full cost-benefit analysis of a carbon tax?

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

9.1 Output Decisions for Price-Taking Firms

Learning Objective 9.1: Explain how competitive, price-taking firms decide on output levels.

9.2 Short-Run Supply

<u>Learning Objective 9.2</u>: Describe how competitive firms make decisions on short-run output and whether to shut down if they experience negative profit.

9.3 Long-Run Supply and Market Equilibrium

Learning Objective 9.3: Describe competitive firms' long-run supply curves and how firms' entry and exit affect the long-run market equilibrium.

9.4 Heterogeneous Firms and Increasing and Decreasing Cost Industries

Learning Objective 9.4: Demonstrate how increasing and decreasing cost industries affect the long-run market supply curve.

9.5 Policy Example

Will a Carbon Tax Harm the Economy?

<u>Learning Objective 9.5</u>: Predict the effect of a carbon tax on the supply and profit maximization decisions of firms on which it is imposed.

LEARN: KEY TOPICS

Terms

Profit (π)

The difference between its total revenue (TR) and its total cost (TC).

Profit maximization rule (MR=MC)

Profit is maximized when output is set where marginal revenue equals marginal cost.

Marginal revenue (MR)

The change in total revenue from a one-unit change in quantity produced.

Marginal cost (MC)

The additional cost incurred from the production of one more unit of output: $MC = \Delta C/\Delta Q$.

Short-run supply

As long as the market price is above the firm's average variable cost, the firm will choose to produce an output where P=MC. The firm's marginal cost curve above the AVC curve is the firm's supply curve. When price is below AVC, the firm chooses not to produce any output at all, so the supply for prices below AVC is zero. See figures 9.6 and 9.7.

Long-run supply (LRATC)

A profit maximizing firm still sets output so that marginal revenue equals marginal cost, and since marginal revenue for a perfectly competitive firm is equal to the market price, the marginal cost curve above the long-run average total cost curve (LRATC) represents the firm's supply curve. The firm's profits depend on the price relative to the long-run average total cost at the optimal output level for the firm, Q^* . As long as profits are not negative, the firm will continue to produce. See figure 9.8.

Shut-down rule

A firm should continue to operate as long as its **average revenue** covers its **average variable costs**. The short-run objective should be to close the firm if its total revenue is less than variable costs. See figure 9.5.

Constant-cost industry

Industries where firms' costs do not change as industry output changes.

Increasing-cost industry

Industries where firms' costs increase as industry output increases.

Decreasing-cost industry

Industries where firms' costs decrease as industry output increases.

Free entry and exit

When there are no special costs, such as technical or legal barriers, to firms entering and exiting the industry.

Graphs

Profit maximization for a price-taking competitive firm

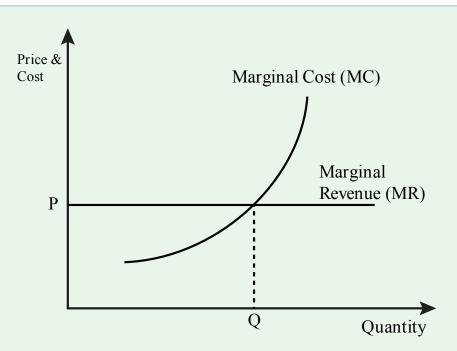


Figure 9.1 Profit maximization for a price-taking competitive firm

Positive profit

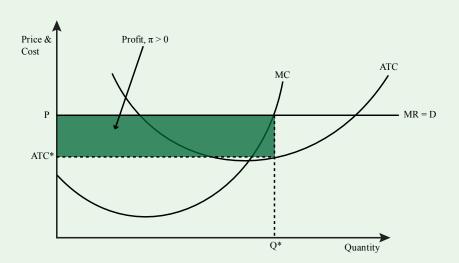


Figure 9.2 Positive profit [latex]P \gt ATC^*[/latex]

Zero profit

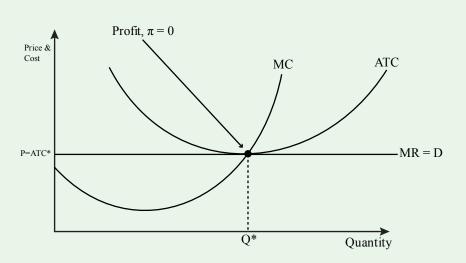


Figure 9.3 Zero profit [latex]P=ATC^*[/latex]

Negative profit (loss)

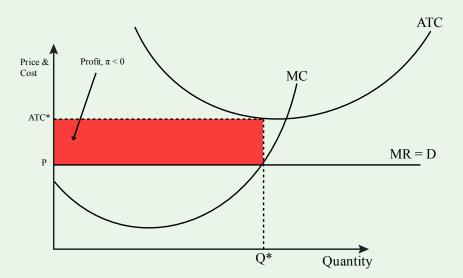


Figure 9.4 Negative profit (loss) [latex]P \lt ATC^*[/latex]

Negative profit, but in the short run, firm should continue to operate

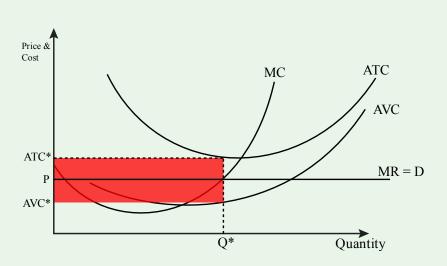


Figure 9.5 Negative profit, but in the short run, firm should continue to operate.

Competitive firm's short-run supply curve

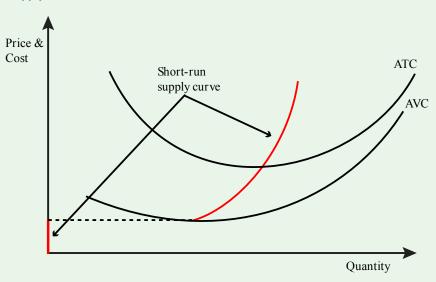


Figure 9.6 Competitive firm's short-run supply curve

Positive profits in the long run

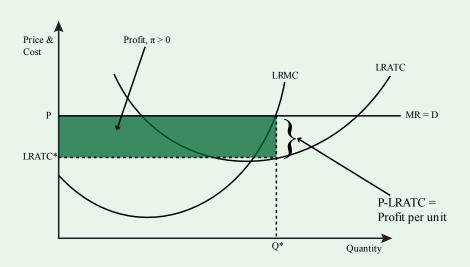


Figure 9.8 Positive profits in the long run

The long-run supply curve of a perfectly competitive firm

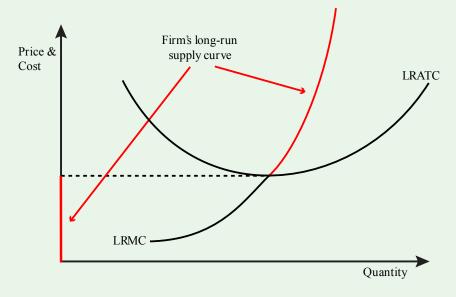


Figure 9.9 The long-run supply curve of a perfectly competitive firm

New entrants increase market supply and lower equilibrium price.

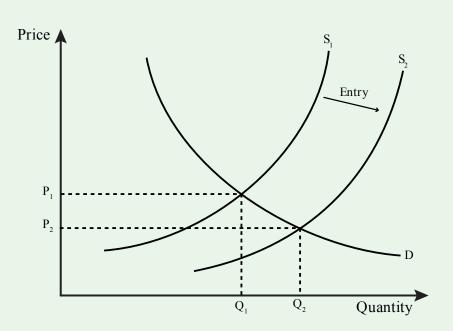


Figure 9.10 New entrants increase market supply and lower equilibrium price.

Equilibrium with zero profits

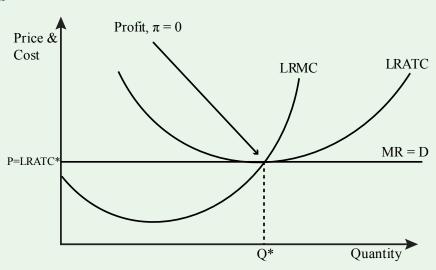


Figure 9.11 Equilibrium with zero profits

Negative profits in the long run

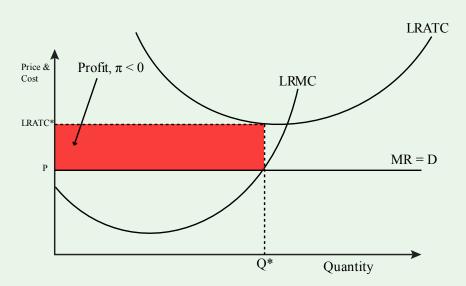


Figure 9.12 Negative profits in the long run

Exiting firms cause a market supply decrease and a rise in the equilibrium price

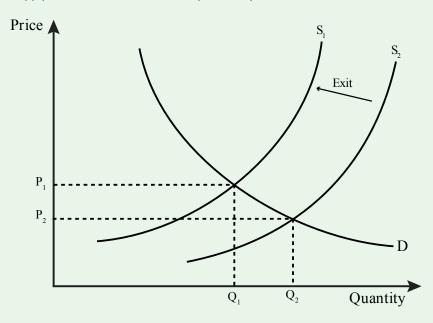


Figure 9.13 Exiting firms cause a market supply decrease and a rise in the equilibrium price

The long-run market supply curve

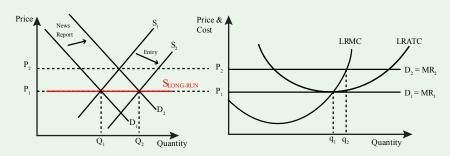


Figure 9.14 The long-run market supply curve

Long-run supply in the case of firms with different costs

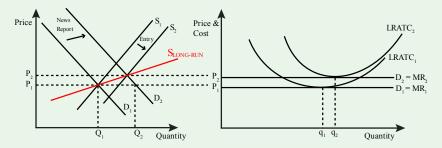


Figure 9.15 Long-run supply in the case of firms with different costs

Long-run cost curves for increasing and decreasing cost industries



Figure 9.16 Long-run supply curves for increasing and decreasing cost industries

Equations

Profit

Profit (π)

A firm's profit (π) is the difference between its total revenue and its total cost

$$\pi(Q) = TR(Q) - C(Q)$$

Total Revenue (TR)

The total revenue is the quantity of the goods produced multiplied by the sales price of those goods.

$$TR(Q) = PQ$$

The total cost is the total cost curve C(Q) introduced in <u>chapter 7</u> and represents the economic cost.

From Output Decision (Q) to Profits (π)

The profit maximization rule (MR=MC) ensures that the firm is maximizing profit, but it does not ensure that the firm is making positive profits; the firm could be minimizing losses instead of making positive profits. The relationship between output decisions and profits can be mathematically expressed:

$$egin{aligned} \Pi &= TR - TC \ TR &= PQ \ TC &= ATC imes Q \end{aligned} \ (ext{since } ATC &= rac{TC}{O}) \end{aligned}$$

Thus,

$$\Pi = (PxQ) - (ATC \times Q)$$
$$= (P - ATC)Q$$

Since Q^* -the quantity for which MR=MC -is always positive or zero, whether profit (π) is positive or negative depends on the price (P) relative to the average total cost at that particular $Q^*(ATC^*)$. If $P>ATC^*$, then $\pi>0$. See figure 9.2 and 9.3.

Marginal cost

Marginal cost (MC) is the additional cost incurred from the production of one more unit of output:

$$MC = \Delta C/\Delta Q$$

The profit maximizing rule stipulates that output should be set where marginal revenue equals marginal cost; marginal revenue for a price-taking firm is the price of the good, therefore

$$P = MC(Q)$$

Marginal revenue

The change in total revenue from a one-unit change in quantity produced. Marginal revenue is expressed as

$$MR = \Delta TR/\Delta Q$$

For a price-taking firm, this increase in revenue from the sale of an additional unit is exactly the price of that unit. In other words, for a price-taking firm,

$$MR = P$$

The Relationship Between Price (P) and Output (Q)

Since marginal cost is the additional cost incurred from the production of one more unit of output:

$$MC = \Delta C/\Delta Q$$

and the profit maximizing rule stipulates that output should be set where marginal revenue equals marginal cost:

$$MR = MC$$

and since marginal revenue for the price-taking firm is the price of the good:

$$MR = P$$

a relationship between output (Q) and price (P) can be established:

$$P = MC(Q)$$

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CHAPTER 10

Market Equilibrium: Supply and Demand

Supply and Demand



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THE POLICY QUESTION

SHOULD THE GOVERNMENT PROVIDE PUBLIC MARKETPLACES?

In the Capitol Hill neighborhood of Washington, DC, the Eastern Market is a large building and grounds owned and operated by the city government. Farmers, bakers, cheese makers, and other merchants of food, arts, and crafts assemble there to sell their wares. Marketplaces like it were once a common feature of cities in the United States and Europe but are now a relative rarity. Many have disappeared due to citizens questioning whether the government should be supporting these marketplaces.

So why does the government play a role in providing some markets? The answer is found in the way markets create benefits for the citizens they serve. In this chapter, we explore how prices and quantities

are set in market equilibrium, how changes in supply and demand factors cause market equilibrium to adjust, and how we measure the benefit of markets to society.

Markets are often private in the sense that the government is not involved in their creation or presence; instead, they are generated by the desire of private individuals to engage in an exchange for a particular good. Sometimes, however, the government plays an active role in establishing and managing markets. At the end of the chapter, we will study why this occurs, using the Eastern Market as an example.

EXPLORING THE POLICY QUESTION

Is public investment in marketplaces justified and if so why?

LEARNING OBJECTIVES

10.1 What is a Market?

<u>Learning Objective 10.1</u>: Identify the characteristics of a market.

10.2 Market Equilibrium: The Supply and Demand Curves Together

Learning Objective 10.2: Determine the equilibrium price and quantity for a market, both graphically and mathematically.

10.3 Excess Supply and Demand

Learning Objective 10.3: Calculate and graph excess supply and excess demand.

10.4 Measuring Welfare and Pareto Efficiency

Learning Objective 10.4: Calculate consumer surplus, producer surplus, and deadweight loss for a market.

10.5 Policy Example

Should the Government Provide Public Marketplaces?

Learning Objective 10.5: Apply the concept of economic welfare to the policy of publicly supported marketplaces.

10.1 WHAT IS A MARKET?

Learning Objective 10.1: Identify the characteristics of a market.

In <u>chapter 9</u>, we found out that the market supply curve comes from the cost structure of individual firms, which in turn comes from their technology, as we discovered in <u>chapter 7</u>. In <u>chapter 5</u>, we found out where the demand curve comes from—the individual utility maximization problems of individual consumers. In both cases, we assumed the demand for and supply of a specific good or service. In other words, we were describing a particular market.

A **market** is characterized as a particular location where a specific good or service is being sold at a defined time. So, for example, we might talk about

- the market for eggs in Nashville, Tennessee, in April 2016;
- the market for rolled aluminum in the United States in 2015; or
- the market for radiological diagnostic services worldwide in the last decade.

In addition, for whatever item, time, and place we describe, there must be both buyers and sellers in order for a market to exist. A market is where buyers and sellers exchange or where there is both demand and supply.

We tend to talk about markets somewhat loosely when studying economics. For example, we might discuss the market for orange juice and leave the time and place undefined in order to keep things simple. Or we might just say that we are looking at the market for denim jeans in the United States. The difficulty with these simplifications is that we can lose sight of the basic assumptions about markets that are necessary for our analysis of them.

The six necessary assumptions for markets are the following:

- 1. A market is for a single good or service.
- 2. All goods or services bought and sold in a market are identical.
- 3. The good or service sells for a single price.
- 4. All consumers know everything about the product, including how much they value it.
- 5. There are many buyers and sellers, and they are known to each other and can interact.
- 6. All the costs and benefits of a transaction accrue only to the buyers and sellers who engage in them.

These assumptions are actually pretty easy to understand. They guarantee that the buyers who value the good more than it costs sellers to produce it will find a seller willing to sell to them. In other words, there are no transactions that don't happen because the buyer doesn't know how much they like the product or because a buyer can't find a seller, or vice versa.

Of course, the assumptions describe an ideal market. In reality, many markets are not exactly like this, and later, in chapters 20, 21, and 22, we will examine what happens when these assumptions fail to hold.

10.2 MARKET EQUILIBRIUM: THE SUPPLY AND DEMAND CURVES TOGETHER

Learning Objective 10.2: Determine the equilibrium price and quantity for a market, both graphically and mathematically.

Market equilibrium is the point where the quantity supplied by producers and the quantity demanded by consumers are equal. When we put the demand and supply curves together, we can determine the **equilibrium price**: the price at which the quantity demanded equals the quantity supplied. In **figure 10.1**, the equilibrium price is shown as P^* , and it is precisely where the demand curve and supply curve cross. This makes sense—the demand curve gives the quantity demanded at every price and the supply curve gives the quantity supplied at every price so there is one price that they have in common, which is at the intersection of the two curves.

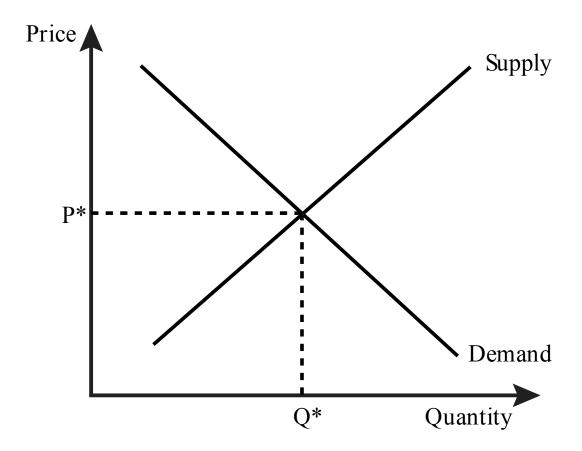


Figure 10.1 The supply and demand curves and market equilibrium

Graphing the supply and demand curves to locate their intersection is one way to find the equilibrium price. We can also find this quantity mathematically. Consider a demand curve for stereo headphones that is described by the following function:

$$Q^D = 1,800 - 20P$$

Note that in general, we draw graphs of functions with the independent variable on the horizontal axis and the dependent variable on the vertical axis. In the case of supply and demand curves, however, we draw them with quantity on the horizontal axis and price on the vertical. Because of this, it is sometimes easier to express the demand relationship as an **inverse demand curve**: the demand curve expressed as price as a function of quantity. In our example, this would be

$$P = 90 - 0.05Q^D$$

This is just the original demand curve solved for P instead of Q^D . In the inverse demand curve, the vertical intercept is easy to see from the equation: demand for headphones stops at the price of \$90. No consumer is willing to pay \$90 or more for headphones.

Similarly, the supply curve can be represented as a mathematical function. For example, consider a supply curve described by the following function:

$$Q^S = 50P - 1,000$$

Similar to the demand curve, we can express this as an **inverse supply curve**: the supply curve expressed as price as a function of quantity. In this case, the inverse supply curve would be

$$P = 0.02Q^S + 20$$

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Here the vertical intercept, \$20, gives us the minimum price to get a seller to sell headphones. At prices of \$20 or less, there will be no supply. So we know that the equilibrium price should be between \$20 and \$90.

Solving for the equilibrium price and quantity is simply a matter of setting $Q^D\equiv Q^S$ and solving for the price that makes this equality happen. In our example, setting $Q^D\equiv Q^S$ yields

$$1,800 - 20P = 50P - 1,000$$

or

$$70P = 2,800$$

or

$$P = $40$$

At P=\$40, the quantity demanded and supplied can be found from the demand and supply curves:

$$Q^D = 1,800 - 20(40) = 1,000$$

$$Q^S = 50(40) - 1,000 = 1,000$$

That these two quantities match is no accident; this was the condition we set at the outset—that quantity supplied equals quantity demanded. So we know that a price of \$40 per unit is the equilibrium price.

These supply and demand curves for headphones are graphed in **figure 10.2** below, and their intersection confirms the equilibrium price we calculated mathematically.

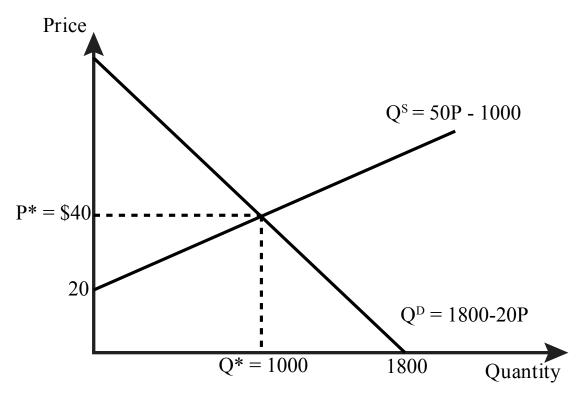


Figure 10.2 Explicit supply and demand curves for headphones

Note that we have also identified the **equilibrium quantity**, Q^* —the quantity at which supply equals demand. At \$40 per unit, one thousand headphones are demanded, and exactly one thousand headphones are supplied. The equilibrium quantity has nothing to do with any kind of coordination or communication among the buyers and sellers; it has only to do with the price in the market. Seeing a unit

price of \$40, consumers demand one thousand units. Independently, sellers who see that price will choose to supply exactly one thousand units.

10.3 EXCESS SUPPLY AND DEMAND

Learning Objective 10.3: Calculate and graph excess supply and excess demand.

It makes sense that the equilibrium price is the one that equates quantity demanded with quantity supplied, but how does the market get to this equilibrium? Is this just an accident? No. The market price will automatically adjust to a point where supply matches demand. Excess supply or demand in a market will trigger such an adjustment.

To understand this equilibrating feature of the market price, let's return to our headphones example. Suppose the price is \$50 instead of \$40. At this price, we know from the supply curve that fifteen hundred units will be supplied to the market. Also, from the demand curve, we know that eight hundred units will be demanded. Thus there will be an excess supply of seven hundred units, as shown in **figure 10.3**.

Excess supply occurs when, at a given price, firms supply more of a good than what consumers demand. These are goods that have been produced by the firms that supply the market and have not found any willing buyers. Firms will want to sell these goods and know that by lowering the price, more buyers will appear. So this excess supply of goods will lead to a price decrease. The price will continue to fall as long as the excess supply conditions exist. In other words, price will continue to fall until it reaches \$40.

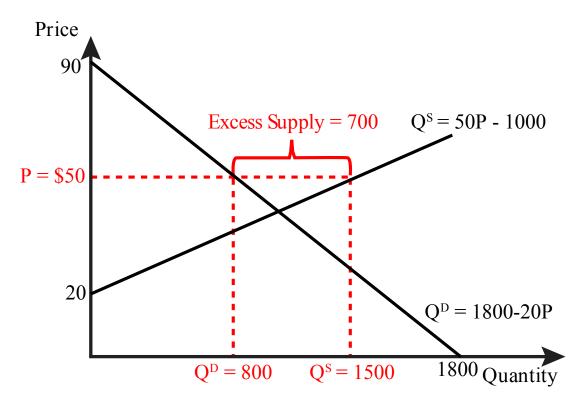


Figure 10.3 Excess supply of headphones at a price of \$50

The same logic applies to situations where the price is below the intersection of supply and demand. Suppose the price of headphones is \$30. We know from the demand curve that at this price, consumers will demand twelve hundred units. We also know from the supply curve that at this price, suppliers will

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supply five hundred units. So at \$30, there will be excess demand of seven hundred units, as shown in **figure 10.4**.

Excess demand occurs when, at a given price, consumers demand more of a good than firms supply. Consumers who are not able to find goods to purchase will offer more money in an effort to entice suppliers to supply more. Suppliers who are offered more money will increase supply, and this will continue to happen as long as the price is below \$40 and there is excess demand.

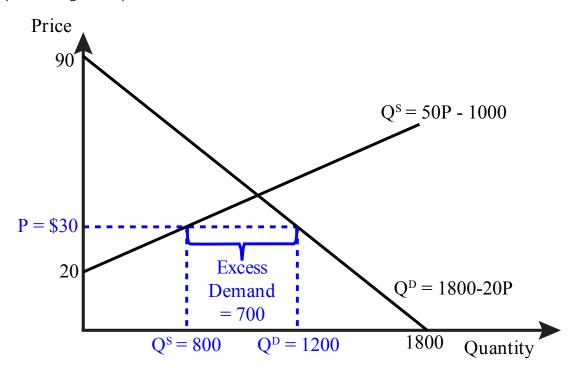


Figure 10.4 Excess demand for headphones at a price of \$30

Only at a price of \$40 is the pressure for prices to rise or fall relieved and will the price remain constant.

10.4 MEASURING WELFARE AND PARETO EFFICIENCY

Learning Objective 10.4: Calculate consumer surplus, producer surplus, and deadweight loss for a market

From our study of markets so far, it is clear that they can contribute to the economic well-being of both buyers and sellers. The term **welfare**, as it is used in economics, refers to the economic well-being of society as a whole, including producers and consumers. We can measure welfare for particular market situations.

To understand the economic concept of welfare—and how to quantify it—it is useful to think about the weekly farmers' market in Ithaca, New York. The market is a place where local growers can sell their produce directly to consumers throughout the summer. It is very successful, and many local residents go to the market to buy produce. Now consider the specific example of tomatoes. What is this market worth to the tomato sellers and buyers that transact in the market?

Suppose a farmer has a minimum willingness-to-accept price of \$1 for an heirloom tomato. This price could be based on the farmer's cost of production or the value she places on consuming the tomato herself. Suppose also that there is a consumer who really wants an heirloom tomato to add to his salad that

evening and is willing to pay up to \$3 for one. If these two people meet each other at the market and agree on a price of \$2, how much benefit do they each get?

The seller receives \$2, and it cost her \$1 to provide the tomato, so she is \$1 better off, the difference between what she received and what she would have accepted for the tomato. Likewise, the buyer pays \$2 but receives \$3 in benefit from the tomato, since that was his willingness to pay; his net benefit is the difference, or \$1. The seller and buyer are both \$1 better off because they had the opportunity to meet and transact. Without this opportunity, the seller would have stayed at home with the tomato and been no better or worse off, and the buyer would not have a tomato for his salad but would be no better or worse off.

The difference between the price received and the willingness-to-accept price is called the **producer surplus** (PS). The difference between the willingness-to-pay price and the price paid is called the **consumer surplus** (CS). The sum of these two surpluses is called **total surplus** (TS). So the producer surplus in the tomato example is \$1, the consumer surplus is \$1, and the total surplus is \$2. This is the surplus generated by one transaction; if we add up all such transactions in the market, we get a measure of the consumer and producer surplus from the market.

Quantifying surplus for an entire market is easy to do with a graph. Let's return to our previous example of headphones and find the consumer and producer surplus.

Figure 10.5 shows that the consumer surplus is the area above the equilibrium price and below the demand curve—the green triangle in the figure. Similarly, the producer surplus is the area below the equilibrium price and above the supply curve—the red triangle in the figure. The area of each surplus triangle is easy to calculate using the formula for the area of a triangle: $\frac{1}{2}bh$, where b is base and b is height.

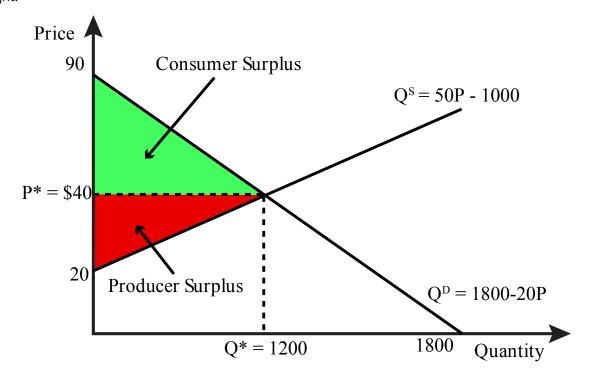


Figure 10.5 Consumer surplus and producer surplus in the market for headphones

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In the case of consumer surplus, the triangle has a base of one thousand, the distance from the origin to Q^* , and a height of \$50, the difference between \$90, the vertical intercept, and P^* , which is \$40.

Consumer surplus =
$$\frac{1}{2}(1,000)(\$50) = \$25,000$$

Similarly,

Producer surplus =
$$\frac{1}{2}(1,000)(\$20) = \$10,000$$
.

Total surplus created by this market is the sum of the two, or \$35,000. This is the measure of how much value the market creates through its enabling of these transactions. Without the ability to come together in this market, the buyers and sellers would miss out on the opportunity to capture this surplus.

We say that a market is efficient when the entire potential surplus has been created. Such a market is an example of **Pareto efficiency**—an allocation of goods and services in which no redistribution can occur without making someone worse off. Think about the distribution of goods in the headphones example. All the buyers and sellers that transact are made better off by the transaction because they gain some surplus from it. If they didn't, they would not voluntarily trade. None of the trades that shouldn't happen do. For example, if there were more than one thousand units exchanged, it would mean sellers were selling to buyers who valued the good less than the sellers' cost of production, where the supply curve is above the demand curve, and one or both of the parties would be worse off because of the exchange.

Another way to see that the market equilibrium outcome is efficient is if we arbitrarily limit the number of goods exchanged to nine hundred. Let's call this maximum quantity restriction \overline{Q} , where the bar above the Q indicates that it is fixed at that quantity. There are one hundred surplus-creating transactions that don't occur; this cannot be an efficient outcome because the entire potential surplus has not been created. The lost potential surplus has a name, $\operatorname{deadweight loss}(DWL)$: the loss of total surplus that occurs when there is an inefficient allocation of resources. The blue triangle in **figure 10.6** represents this deadweight loss.

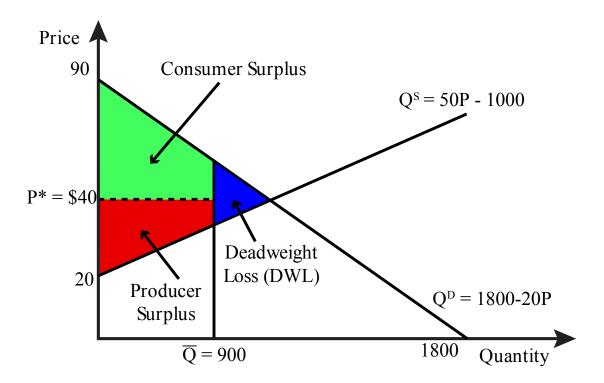


Figure 10.6 Deadweight loss from a quantity constraint

We can calculate the value of the deadweight loss precisely, again using the formula for the area of a triangle. Since the demand function is $Q^D=1,800-20P$, the point on the demand curve that results in a demand of nine hundred is a price of \$45. Similarly, if the supply function is given as $Q^S=50P-1,000$, the point on the supply curve that results in a quantity supplied of nine hundred is a price of \$38. Thus the base of the triangle is \$45 – \$38, or \$7, and the height is the difference between the one thousand units that are sold in the absence of a restriction and the nine-hundred-unit restricted quantity, or one hundred. So

$$DWL = \frac{1}{2}(\$7)(100) = \$350.$$

10.5 POLICY EXAMPLE

SHOULD THE GOVERNMENT PROVIDE PUBLIC MARKETPLACES?

Learning Objective 10.5: Apply the concept of economic welfare to the policy of publicly supported marketplaces.

The first question in determining whether a case can be made for the public provision of marketplaces, such as the Eastern Market in Washington, DC, is what would occur in the absence of such a market. If the buyers and sellers in these markets could easily access other markets, then it would be hard to argue that the marketplace is providing a net benefit. Similarly, if the commercial activity that takes place in this market is simply a diversion of similar activity that would have taken place elsewhere, then it is likely that there is little to no net benefit. So for the sake of this exercise, we will assume that the marketplace is providing an opportunity to these buyers and sellers that they would not otherwise have.

So given this assumption, are these marketplaces valuable? The simple answer, as long as transactions are occurring, is yes. We can see this from a simple diagram of a market for an individual good, let's say fresh apples, that exists within the Eastern Market (**figure 10.7**).

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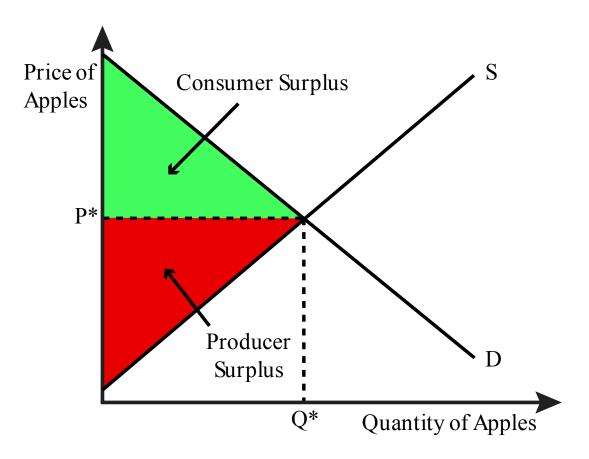


Figure 10.7 The market for apples in the Eastern Market

There is clearly a surplus being created by the apple transactions that take place within the market. This in itself is the primary argument for the marketplace. Buyers and sellers are able to transact and become better off for it. The value to those individuals is measured by surplus.

But a complete answer must compare the value to society of the markets to the cost to society of the marketplace itself. Does the total surplus created by the marketplace justify the cost?

Let's return now to the key assumption—that a market for fresh apples would not exist without government support. Is this a reasonable assumption?

In the nineteenth and early twentieth centuries, when many public markets were founded, transportation was difficult, and bringing fresh food to support urban population centers was something local governments commonly did. Today, transportation is not nearly as difficult or costly. But although many areas are well served by grocery stores, where it is reasonable to expect customers will find fresh fruits and vegetables, other locations are characterized by *food deserts*. Food deserts are defined as urban neighborhoods and rural towns without ready access to fresh, healthy, and affordable food. Instead of supermarkets and grocery stores, these communities may have no food access or are served only by fast-food restaurants and convenience stores that offer few healthy, affordable food options. The lack of access contributes to a poor diet and can lead to higher levels of obesity and other diet-related diseases, such as diabetes and heart disease (US Department of Agriculture [USDA]).

The USDA estimates that 23.5 million people in the United States live in food deserts.

Although the Capitol Hill neighborhood experienced some hard times in the past, today it is prosperous and well served by grocery stores. So the need for government support of the Eastern Market there

is less clear. In <u>chapter 21</u>, we will explore public goods and externalities in detail and become better equipped to fully explore this issue.

EXPLORING THE POLICY QUESTION

- 1. What other kinds of marketplaces can you think of that the government aids by providing infrastructure?
- Airports allow the market for airline travel to exist in a functional way. Most airports in the United States are run by local governments. Using the topics explored in this chapter, give a justification for government expenditures on airports.
- 3. Should the District of Columbia government spend money on a market that primarily serves one neighborhood? Give reasons for and against.

REVIEW: TOPICS AND LEARNING OBJECTIVES

10.1 What is a Market?

<u>Learning Objective 10.1</u>: Identify the characteristics of a market.

10.2 Market Equilibrium: The Supply and Demand Curves Together

Learning Objective 10.2: Determine the equilibrium price and quantity for a market, both graphically and mathematically.

10.3 Excess Supply and Demand

Learning Objective 10.3: Calculate and graph excess supply and excess demand.

10.4 Measuring Welfare and Pareto Efficiency

Learning Objective 10.4: Calculate consumer surplus, producer surplus, and deadweight loss for a market.

10.5 Policy Example

Should the Government Provide Public Marketplaces?

Learning Objective 10.5: Apply the concept of economic welfare to the policy of publicly supported marketplaces.

LEARN: KEY TOPICS

Terms

Market equilibrium

The point where the quantity supplied by producers and the quantity demanded by consumers are equal.

Inverse demand curve

The demand curve expressed as price as a function of quantity:

$$P = 90 - 0.05Q^{D}$$

Inverse supply curve

The supply curve expressed as price as a function of quantity:

$$P = 20 - 0.03Q^S$$

Equilibrium price

The price at which the quantity demanded equals the quantity supplied.

Equilibrium quantity

 Q^* –the quantity at which supply equals demand.

Excess demand

When, at a given price, consumers demand more of a good than firms supply, i.e., the latest video game consoles.

Excess supply

When, at a given price, firms supply more of a good than what consumers demand, i.e., the sales of holiday merchandise once it has passed.

Welfare

In economics, refers to the economic well-being of society as a whole, including producers and consumers.

Producer surplus

The difference between the price received and the willingness-to-accept price.

Consumer surplus

The difference between the willingness-to-pay price and the price paid.

Total surplus

The sum of the consumer surplus and the producer surplus.

Pareto efficiency

an allocation of goods and services in which no redistribution can occur without making someone worse off, i.e., both seller and buyer are gaining from the exchange-sellers are selling an amount that is equal to the demand curve and buyers are paying prices that indicate close to equilibrium price.

Deadweight loss

The loss of total surplus that occurs when there is an inefficient allocation of resources, i.e., a firm produces exactly 900 limited edition headphones worth \$200 each. The demand tests out at 1000. There are 100 surplus-creating transactions that don't occur-resources should have been allocated to make the 1000.

Graphs

The supply and demand curves and market equilibrium

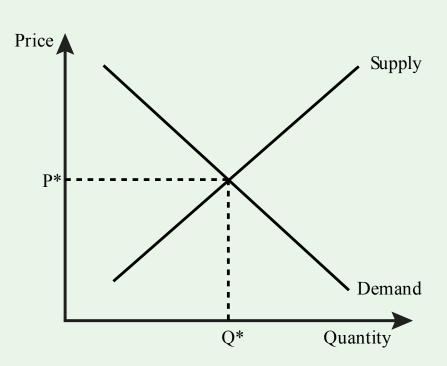


Figure 10.1 The supply and demand curves and market equilibrium

Explicit supply and demand curves

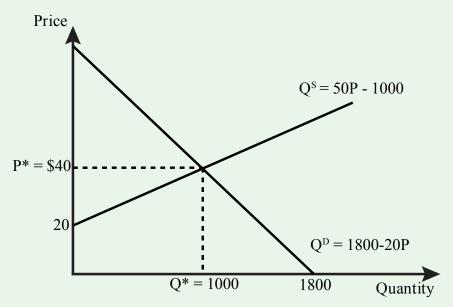


Figure 10.2 Explicit supply and demand curves for headphones

Excess supply at a price of \$50

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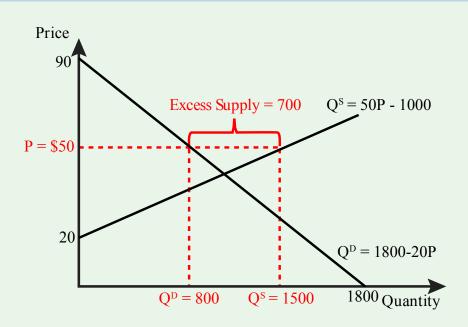


Figure 10.3 Excess supply of headphones at a price of \$50

Excess demand at a price of \$30

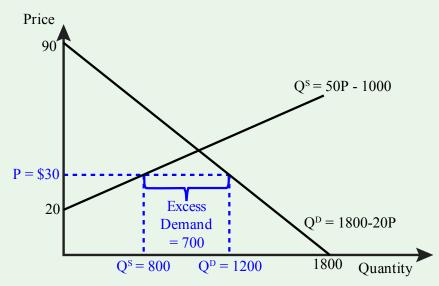


Figure 10.4 Excess demand for headphones at a price of \$30

Consumer surplus and producer surplus

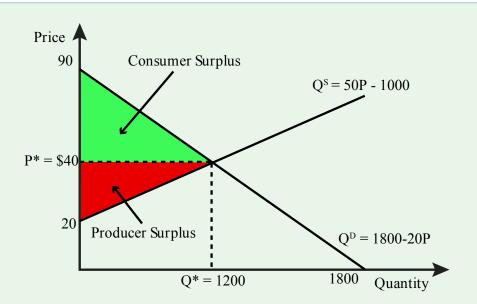


Figure 10.5 Consumer surplus and producer surplus in the market for headphones

Deadweight loss from a quantity constraint

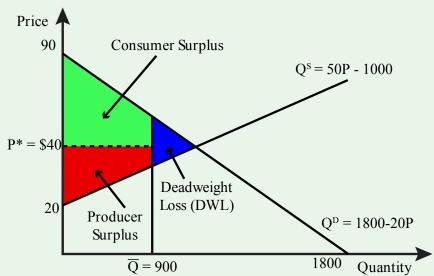


Figure 10.6 Deadweight loss from a quantity constraint

A typical goods market in the eastern market

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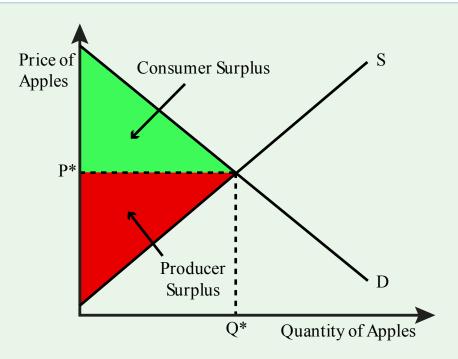


Figure 10.7 The market for apples in the Eastern Market

Equations

Quantity supplied

$$Q^S = 50P - 1000$$

Determining Q* and P*

P=MC(Q)

The above equation utilizes the relationship between quantity and price to determine a starting algorithm for drafting a supply curve. Review this relationship in chapter 9.

Inverse supply curve

$$P = 20 - 0.03Q^{S}$$

Quantity demanded

Derived from max production and minimum price to cover costs with profit.

$$Q^D = 1,800 - 20P$$

Inverse demand curve

$$P = 90 - 0.05Q^{D}$$

The original equation set to solve for P. In this inverse curve, the vertical intercept is very clear: demand for this product stops at \$90. No one is willing to pay more than \$90 for the product.

Solving for equilibrium price (P^*) and equilibrium quantity Q^*

Solving for the equilibrium price and quantity is simply a matter of setting

$$Q^D = Q^S$$

and solving for the price that makes this equality happen. In our example, setting $Q^D \equiv Q^S$ yields

$$1,800 - 20P = 50P - 1,000$$

or

$$70P = 2,800$$

or

$$P = $40$$

At P=\$40, the quantity demanded and supplied can be found from the demand and supply curves:

$$Q^D=1,800-20(40)=1,000 \ Q^S=50(40)-1,000=1,000$$

If the proper P^st and Q^st have been found, the two equations should be equal.

Issues of excess and deadweight loss (DWL)

Quantifying surplus is easy to do with a graph, see figure 10.5 in full-size via link or half-size below:

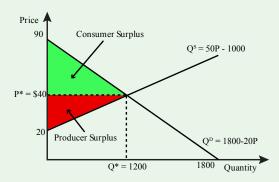


Figure 10.5 Consumer surplus and producer surplus in the market for headphones

the consumer surplus is the area above the equilibrium price and below the demand curve—the green triangle in the figure. Similarly, the producer surplus is the area below the equilibrium price and above the supply curve—the red triangle in the figure. The area of each surplus triangle is easy to calculate using the formula for the area of a triangle, where b is base and b is height:

$$\frac{1}{2}bh$$

Utilizing figures from the graph, the following formulas can be derived:

Consumer surplus

Consumer surplus =
$$\frac{1}{2}(1,000)(\$50) = \$25,000$$

or

Consumer surplus
$$=\frac{1}{2}(b)(h)$$

where the area equals the total dollar amount of producer surplus, the base (b) is the distance from the origin to Q^* , and the height (h) is the difference between the maximum willing to pay price P_{max} , or the y-intercept, and P^* . This can also be written thusly:

$$CS = rac{1}{2}(Q^* - (O)((P_{max} - P^*))$$

where O is the origin of the supply curve and P_{max} is the vertical intercept of the y-axis, and also the maximum price that anyone is willing to pay for the product.

Producer surplus

Producer surplus =
$$\frac{1}{2}(1,000)(\$20) = \$10,000$$

or

$$Producer surplus = \frac{1}{2}(b)(h) = area$$

where the area equals the total dollar amount of producer surplus, the base (b) is the distance from the origin to Q^* , and the height (h) is minimum price. This can also be written thusly:

$$PS=rac{1}{2}(Q^*-O)(P_{min})=area$$

where O is the origin of the supply curve and P_{min} is the minimum willingness-to-accept price.

Total surplus

The sum of CS and PS

$$TS = CS + PS$$

Deadweight loss (DWL)

The loss of total surplus that occurs when there is an inefficient allocation of resources.

$$DWL = rac{1}{2}(P *^- P_Q)(Q *^- Q)$$

Where P_Q is the price determined by the supply/demand curves to be viable at the current output, Q. See Figure 10.6 for full-size or see half-size below. Figure 10.6 illustrates utilizing a graph to develop a DWL equation:

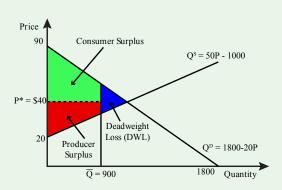


Figure 10.6 Deadweight loss from a quantity constraint

If a firm produces 900 headphones, but the Q^* satates that 1000 is the optimum output, the lost surplus price would then equate to the difference between the price for 900 units $(P_Q, \text{in this case} P_900)$, or \$38, and the P^* , or \$45. Thus the denominator would be 100 (1000-900) and the numerator \$7 (\$45-\$38). The equation would look thus:

$$DWL = \frac{1}{2}(\$7)(100) = \$350$$

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COMPARATIVE STATICS 235

CHAPTER 11

Comparative Statics: Analyzing and Assessing Changes in Markets

Analyzing and Assessing Changes in Markets



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THE POLICY QUESTION

SHOULD THE FEDERAL GOVERNMENT SUBSIDIZE SOLAR POWER INSTALLATIONS?

In 2006, in an effort to spur the use of solar power in the country, the US government created a solar investment tax credit (SITC) allowing US households and businesses to deduct 30 percent of the amount they invested in solar power installations. Since the program began, the growth rate in solar installations has been 76 percent per year.

The program has been seen as very successful in promoting solar energy installations. But what does economics say about the trade-offs of subsidizing these types of installations? Does the economic welfare they provide justify their costs?

This chapter looks at a method for evaluating the effects on price and quantity equilibriums when supply or demand—or both—changes within a market. Subsidies are just one potential cause of such changes. We will also look at the effects of taxes, price floors, and price ceilings. And throughout we will focus on the significance of changes in supply and demand for overall economic welfare.

EXPLORING THE POLICY QUESTION

- 1. Do you think all subsidies work as well as the SITC to increase demand? What variables do you think influence their effectiveness?
- 2. What other kinds of market subsidies are you familiar with, and how would you evaluate their success?

LEARNING OBJECTIVES

11.1 Changes in Supply and Demand

Learning Objective 11.1: Describe the causes of shifts in supply and demand and the resulting effects on equilibrium price and quantity.

11.2 Welfare Analysis

Learning Objective 11.2: Apply a comparative static analysis to evaluate economic welfare, including the effect of government revenues.

11.3 Price Ceilings and Floors

Learning Objective 11.3: Show the market and welfare effects of price ceilings and floors in a comparative statics analysis.

11.4 Taxes and Subsidies

Learning Objective 11.4: Show the market and welfare effects of taxes and subsidies in a comparative statics analysis.

11.5 Policy Example

Should the Federal Government Subsidize Solar Power Installations?

<u>Learning Objective 11.5</u>: Apply a comparative static analysis to evaluate government subsidies of solar panel installations.

11.1 CHANGES IN SUPPLY AND DEMAND

Learning Objective 11.1: Describe the causes of shifts in supply and demand and the resulting effects on equilibrium price and quantity.

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The competitive market supply-and-demand model is one of the most powerful tools in economics. With it we can predict the impact of economic changes on consumers' consumption decisions, producers' supply decisions, and the market itself. We call the analysis of such changes **comparative statics**: the analysis of how equilibrium prices and quantities change when other exogenous variables—variables that shift demand and supply curves—change. The term static emphasizes the fact that we are comparing two different market equilibriums at discrete points in time—one before and one after the changes occur—as opposed to analyzing the dynamic process of price and quantity changes.

Changes in Demand

Since we know where supply and demand curves come from, we know precisely what can cause them to shift. Let's start with demand. Recall the consumer choice problem: consumers want to maximize their individual utilities by choosing bundles of goods available to them in their budget sets. How do these bundles change? Price is one of the main mechanisms, but this is accounted for in the curve itself. As price falls, demand increases and vice versa—this is what the slope of the demand curve represents. But how do other factors affect demand?

A change in income.

It will shift the budget line and cause changes in quantities demanded. For example, if a tax refund causes consumers to demand more automobiles, the demand curve shifts to the right.

Changes in preferences.

They can alter the ultimate quantity choice. For example, a new study that finds negative health effects of drinking coffee could lower the demand for coffee, which would be reflected in a shift of the demand curve to the left.

Changes in the prices of goods that are substitutes or complements.

This can also affect the demand for a good. For example, if the price of Coca-Cola increases, the demand for Pepsi Cola might increase, causing a rightward shift in the demand curve.

Figure 11.1 shows the effect on price and quantity equilibriums when demand increases, and **figure 11.2** shows the effect when demand decreases.

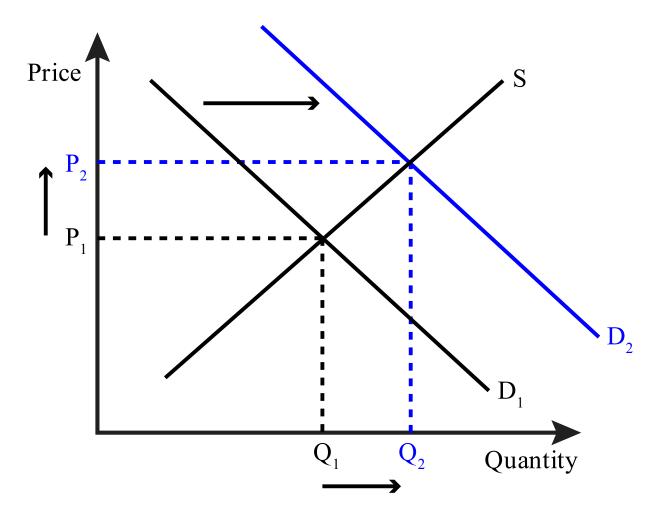


Figure 11.1 Increase in demand causes equilibrium price and quantity to rise.

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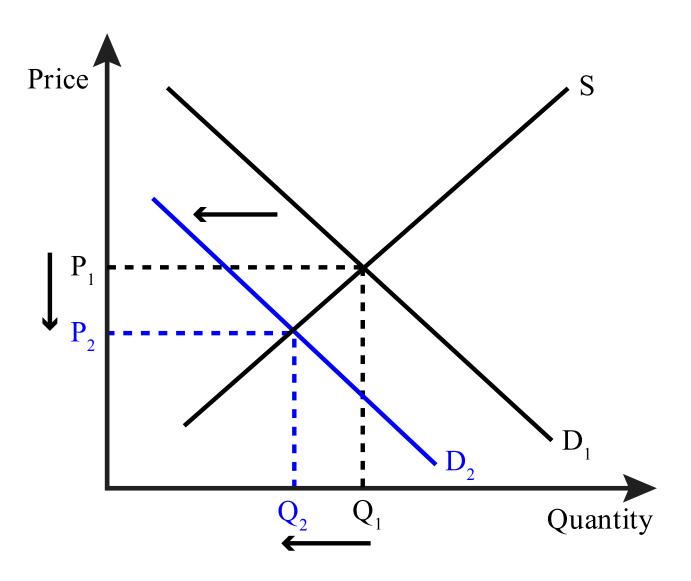


Figure 11.2 Decrease in demand causes equilibrium price and quantity to fall

Changes in Supply

Shifts in supply arise from changes in the following:

The cost of production for the firms.

For example, autoworkers in the United States represented by a union might negotiate a new labor contract for higher wages. This represents a cost increase on the part of firms and will result in a leftward shift of the supply curve.

• Technology that affects the production function.

For example, a new robotic technology that aids in the assembly of automobiles in the factory could improve the efficiency of the plant, resulting in a rightward shift of the supply curve.

The number of sellers in the market.

For example, perhaps a new company, like Tesla, decides to begin to manufacture cars in the United States, or a foreign company, like FIAT, begins to sell in the US market—either way, the number of sellers has increased, and the number of cars for sale is likely to increase as well, leading to a rightward shift in the supply curve.

The presence of alternative markets for sellers.

For example, an economic boom in Canada might cause US auto manufacturers to send more of the cars they produce to Canada instead of selling them in the United States, leading to a lower supply of cars in the US market represented by a leftward shift in the supply curve.

Figure 11.3 shows the effect on price and quantity equilibriums when supply decreases, and **figure 11.4** shows the effect when supply increases.

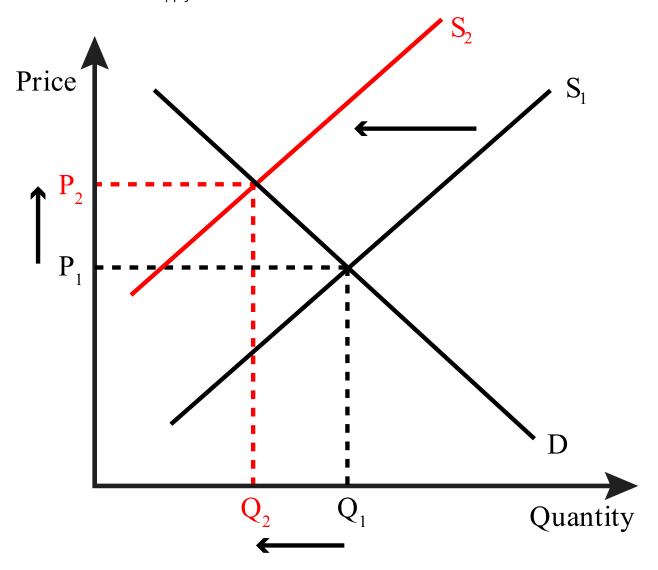


Figure 11.3 Decrease in supply causes equilibrium price to rise and quantity to fall

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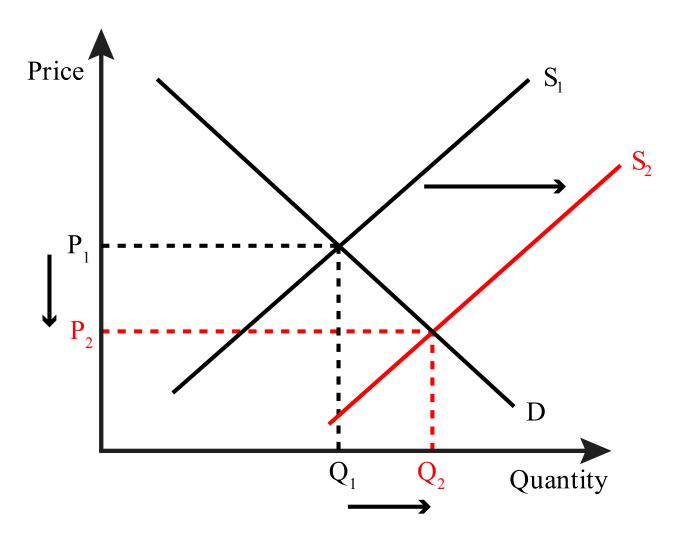


Figure 11.4 Increase in supply causes equilibrium price to fall and quantity to rise.

Changes in Both Supply and Demand

To see what happens when both supply and demand change, let's consider an example of each individually and then combined. On the demand side, a tax refund increases consumers' incomes and results in an increase in demand for automobiles. The rightward shift in the demand curve will lead to a new equilibrium price and quantity. Compared to the original equilibrium price and quantity, the new equilibrium is characterized by higher prices and greater quantity.

On the supply side, we might have a situation of increased productivity resulting from the introduction of new robotic technology in automobile manufacturing. This would shift the supply curve to the right. Compared to the old equilibrium price and quantity, the new equilibrium price is lower and the new equilibrium quantity is greater.

What if both changes occurred at the same time? Both the demand curve and the supply curve would shift to the right. The effect on equilibrium quantity is clear: the new quantity would be greater than the original quantity, as both shifts move the quantity in the same direction. The effect on equilibrium price is ambiguous, since the demand shift puts upward pressure on price and the supply shift puts downward pressure on price. In the end, the actual change is the net of these two effects and will depend on the

shape of the two curves and the magnitude of the two shifts. **Figure 11.5** illustrates the situation where price rises, and **figure 11.6** illustrates the situation where price falls.

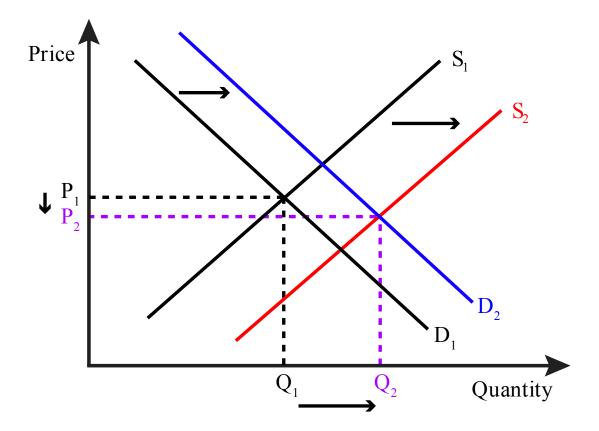


Figure 11.5 Increase in demand and supply that causes equilibrium price and quantity to rise

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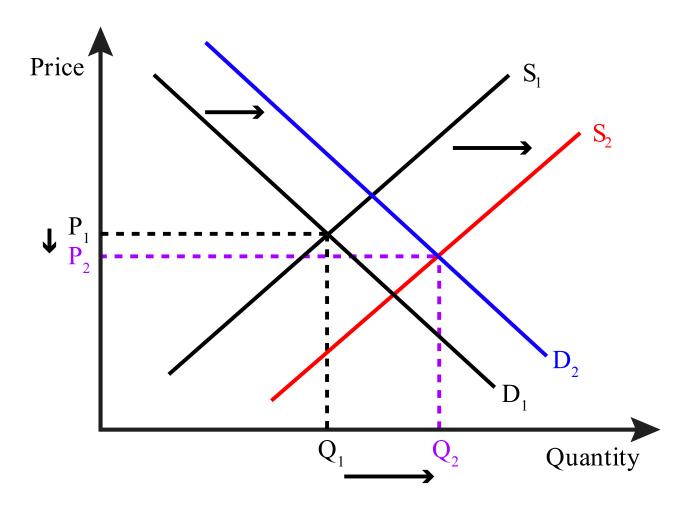


Figure 11.6 Increase in demand and supply that causes equilibrium quantity to rise and price to fall

Similarly, for a simultaneous demand and supply decrease, quantity would unambiguously fall, but the effect on price will depend on the magnitude of the shifts, so without more information, we cannot predict the direction of the change.

What happens when supply and demand changes are in opposite directions? **Figure 11.7** illustrates the situation when demand increases and supply falls. In this situation, the change in price is unambiguous—it will rise—but the effect on quantity depends on the relative magnitude of the shifts in the curves. Quantity can rise, fall, or remain unchanged. In figure **11.7**, the quantity increases slightly.

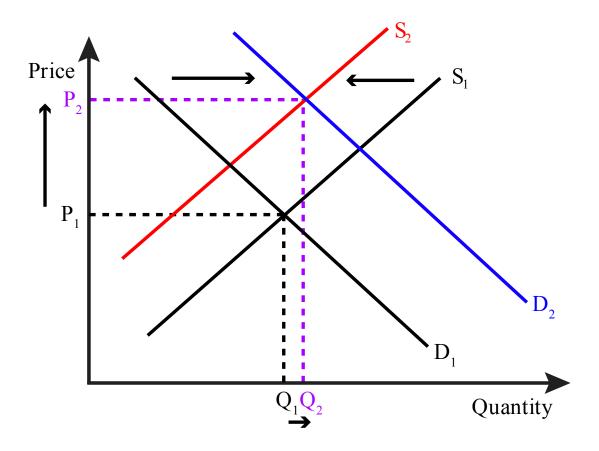


Figure 11.7 Increase in demand and decrease in supply cause equilibrium price to rise and have an ambiguous effect on quantity

Table 11.1 Effects of shifts in demand and supply

| Demand | Supply | Change in price | Change in quantity |
|-----------|-----------|-----------------|--------------------|
| Increase | No change | + | + |
| Decrease | No change | - | - |
| No change | Increase | - | + |
| No change | Decrease | + | - |
| Increase | Increase | ? | + |
| Increase | Decrease | + | ? |
| Decrease | Increase | - | ? |
| Decrease | Decrease | ? | - |

To summarize, when one curve moves and the other doesn't, we can make predictions about the direction of the change in both price and quantity. When both curves move, we can make predictions about the direction of the change in one but not of both price and quantity. **Table 11.1** summarizes the effects on price and quantity for changes in demand and supply.

Calculating and Comparing the New Market Equilibrium

So far, we have not considered the magnitude of the changes in equilibrium price and equilibrium quantity due to shifts in supply and demand. Without knowing the specific demand and supply functions, it is

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impossible to determine the precise magnitudes. With specific supply and demand functions, however, we can perform comparative statics analyses by solving for the original and the new equilibrium price and quantity and comparing them.

Let's return to the demand and supply functions from chapter 10:

$$Q_1^D=1,800-20P \ Q_1^S=50P-1,000$$

In <u>chapter 10</u>, we solved these and found the equilibrium price of \$40 and the equilibrium quantity of one thousand.

Now suppose two things happen. One, some new information causes demand to increase. The new, higher demand is now described by the demand function:

$$Q_2^P = 2,400 - 20P$$

Two, a new manufacturing process increases the productivity of firms, resulting in an increase in supply. The new increased supply is described by the supply function:

$$Q_2^S = 50P - 400$$

Solving for the new equilibrium, we get

$$2,400-20P=50P-400 \ 2,800=70P \ P_2^S=\$40 \ Q_2^*=1,600$$

Comparing these to the original equilibrium price and quantity reveals that quantity increased by six hundred and that price remained at \$40. From **table 11.1**, we expected the quantity to increase, but we could not predict the direction of the change in price. For this specific example, we see that price has not changed. The graphical model is useful in making predictions about the directions of some equilibrium price and quantity changes, but we need a specific model in order to pin down the magnitude of changes in both price and quantity.

11.2 WELFARE ANALYSIS

Learning Objective 11.2: Apply a comparative static analysis to evaluate economic welfare, including the effect of government revenues.

We can apply the principles of comparative static analysis to measuring economic welfare. In chapter 10, we looked at welfare in terms of consumer surplus, producer surplus, and their combination, total surplus. For purposes of evaluating overall economic welfare, the total surplus is what economists care about. So we measure the effect of changes in supply and demand on welfare by comparing the total surplus before and after the change.

Figure 11.8 illustrates the change in welfare from an increase in demand. Increased demand leads to more transactions and to more consumer and producer welfare from all transactions. The blue-shaded area shows the net increase in welfare that results from the increased demand.

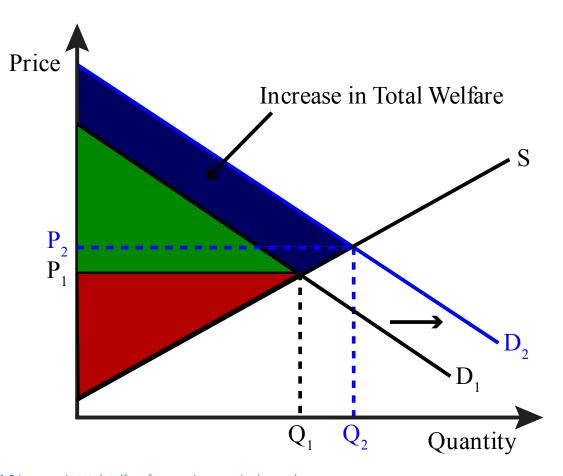


Figure 11.8 Increase in total welfare from an increase in demand

Predicting the effect on total welfare is straightforward when one curve shifts but complicated when both curves shift. Any increase in only supply or demand will increase total welfare, and any decrease in only supply or demand will decrease total welfare. It is also easy to see that welfare will increase when both supply and demand increase and will decrease when both supply and demand decrease. But what happens when one increases and the other decreases?

Figure 11.9 shows a situation where demand increases at the same time that supply decreases. The blue triangle represents the original total welfare, the red triangle represents the new total welfare, and the purple triangle represents neither a gain nor a loss in welfare. Whether there is a net gain or loss in welfare depends on the relative sizes of the areas marked "gain in welfare" and "loss in welfare." As is easy to see, whether this is a net loss or gain depends on the magnitude and position of the shifting curves and can easily go either way.

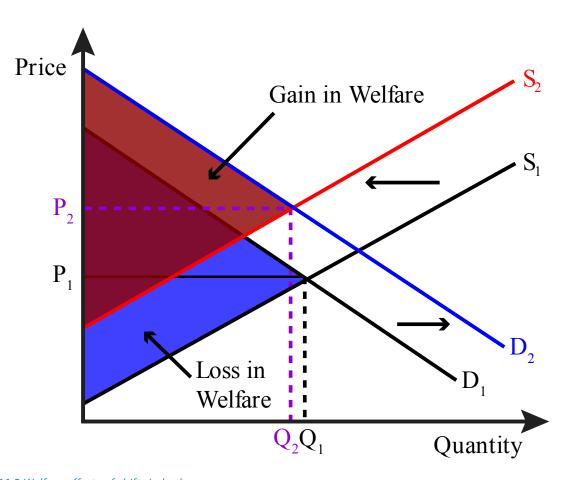


Figure 11.9 Welfare effects of shifts in both curves

Sometimes the government takes actions that lead to positive government revenue (e.g., imposing a tax) or negative government revenue (e.g., spending money). Economists account for government revenues or expenditures by including them in the total surplus calculations. Government revenues are public resources and spending is with public money, so both should be accounted for the same way consumer and producer surpluses are—they are all part of the societal gains or losses that we consider in total surplus:

Total Surplus = Consumer Surplus + Producer Surplus + Government RevenueNote that government revenue can be positive (tax receipts) or negative (government spending).

11.3 PRICE CEILINGS AND FLOORS

Learning Objective 11.3: Show the market and welfare effects of price ceilings and floors in a comparative statics analysis.

Price ceilings and **price floors** are artificial constraints that hold prices below and above, respectively, their free-market levels. Price ceilings and floors are created by extra-market forces, usually the government. A classic example of a price ceiling is a rent-control law like those that exist in New York City. **Figure 11.10** illustrates the effect of a price ceiling in a market for rental housing. The price ceiling holds prices below the market equilibrium price, and there are more consumers wishing to rent apartments at the ceiling price than there are rental units available. The result is excess demand for rental housing.

Market equilibrium price is sometimes referred to as the **market-clearing price**. This term references the fact that the market is cleared of all unsatisfied demand and excess supply at the equilibrium price.

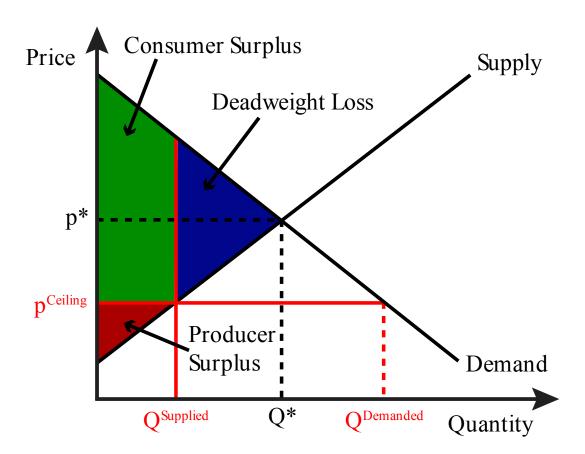


Figure 11.10 Welfare effects of a price ceiling

The effect of a rental price ceiling on welfare is clear. Fewer apartments will be rented than at the market equilibrium price, and all the surplus that would have been created by those rentals is not realized, resulting in deadweight loss. Of the total surplus that is created, a greater proportion accrues to the consumers than the producers, but in welfare terms, only the total surplus matters. So price ceilings do two things:

- 1. They lower total surplus and create deadweight loss.
- By creating excess demand, they create winners and losers among consumers. In the case of a rental price ceiling, some consumers are lucky enough to find an apartment to rent at the ceiling price, while others cannot.

The consumer surplus shown in **figure 11.10** assumes that the market will somehow allocate the apartments to the users whose valuation of them is the highest (those that represent the highest points on the demand curve). But no mechanism exists to assure that this will happen. Instead, there is likely to be a random assignment of apartments among those willing to pay the ceiling price. This means that **figure 11.10** likely overstates the resulting consumer surplus and understates the deadweight loss. We will continue with the assumption of efficient allocation of apartments to keep the analysis simple, but it is important to understand the consequences of this assumption.

Figure 11.11 illustrates the situation for a price floor. When the price of a good is not allowed to sink to its market equilibrium level, a situation of excess supply occurs where producers would like to make and sell more goods than customers would like to buy. The price floor creates a deadweight loss in the same way a price ceiling does: it limits the number of goods that are bought and sold and therefore limits the

amount of surplus created relative to the potential surplus. In the case of the price floor, more of the surplus that is created is in the form of producer surplus than consumer surplus. An example of a price floor might be the regulated fares for taxis in many cities. The success of Uber and Lyft, so-called ride-sharing services, suggests that there is indeed an excess supply of potential taxis that would be quite happy to give rides for less.

This analysis assumes that firms with the lowest marginal cost supply the good, but there is nothing in the market that ensures this. So the true welfare effects are likely to be lower producer surplus and higher deadweight loss than depicted in **figure 11.11**.

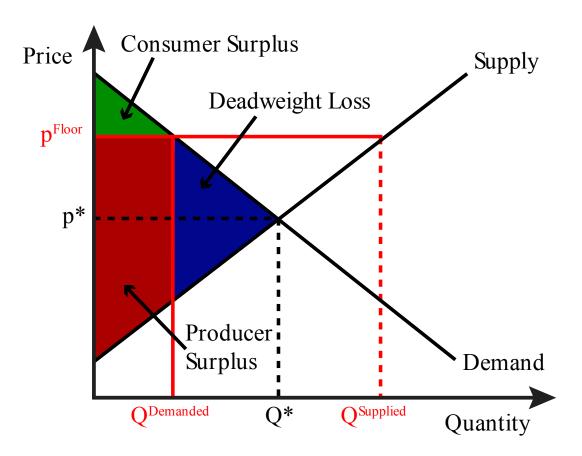


Figure 11.11 Welfare effects of a price floor

For both price ceilings and price floors, the welfare impact is clear: there is a reduction in total surplus relative to the market equilibrium price and quantity.

11.4 TAXES AND SUBSIDIES

Learning Objective 11.4: Show the market and welfare effects of taxes and subsidies in a comparative statics analysis.

Governments levy taxes to raise revenues in many areas. Governments at all levels—national, state, county, municipality—tax things such as income, hotel rooms, purchases of consumer goods, and so on. They tax both producers of goods and consumers of goods. Governments also subsidize things, such as the production of dairy goods or the purchase of electric cars. In this section, we will explore how taxes and subsidies affect the supply-and-demand model and the impact of supply and demand on welfare. We will discover that it does not matter upon whom you levy a tax or to whom you provide a subsidy,

producers or consumers; the burden or benefits will end up being shared among producers and consumers in identical proportions.

Taxes on Sellers

To examine the effects of a tax on a market, let's perform a comparative static analysis. We will start with a market without a tax and then compare it to the same market with a tax. Let's consider the market for tomatoes at the farmers' market in Lawrence, Kansas. The current equilibrium price is \$1.00 per tomato, and the equilibrium quantity is five hundred. Now suppose that the city of Lawrence decides it needs to raise revenues to support the improvement of infrastructure at the market and imposes a sales tax on tomatoes to do so. What would be the impact of this tax on the market?

A sales tax on tomatoes can be imposed on either buyers or sellers. Generally, sales taxes are collected by sellers and then remitted to the government. This means that for a \$1 tomato that has a 10 percent tax, the seller collects both the \$1 and the \$0.10 for the government. We call this type of tax an *ad valorem* tax because it depends on the value of the good itself. Alternatively, the government could have imposed a set amount, like \$0.20, on one tomato, regardless of the price of the tomato itself—this is known as a *specific tax*. For this analysis, we will use a specific tax because it is easier to analyze, but either way, the analysis is similar. So let's consider a \$0.20 tax on each tomato to be paid by sellers. Since the seller collects the tax, we can illustrate its effect on the market through the supply curve.

Consider any single point on the supply curve. This point is the seller's willingness-to-accept price for a tomato at a certain supply quantity. Suppose this price is \$0.50 at a given point. If the government imposes a \$0.20 tax on each tomato, the seller's new willingness-to-accept price will rise to \$0.70. This price is the sum of the original willingness-to-accept price and the \$0.20 that the seller will collect from the buyer and give to the government. The same logic applies to every point on the supply curve, so the tax has the effect of creating a new supply curve shifted upward by \$0.20 from the original supply curve. Figure 11.12 shows the original supply curve (S_1) and the shifted supply curve (S_2).

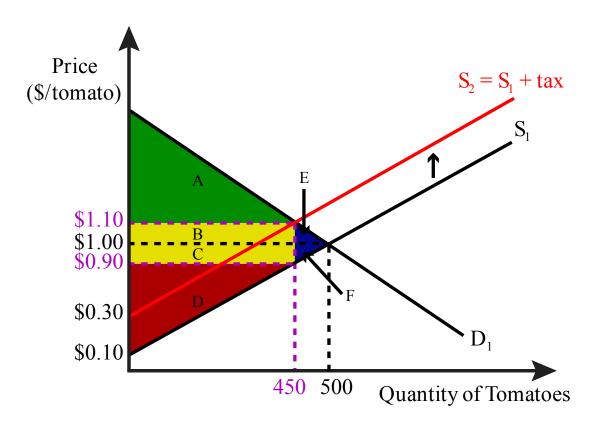


Figure 11.12 Effect of a tax on sellers of tomatoes at the Lawrence farmers' market

The original equilibrium price of a tomato is \$1. With the new tax, there is a difference between what consumers pay and what producers receive—the difference being the \$0.20 tax per tomato. So equilibrium price is no longer a single value at which quantity supplied is equal to quantity demanded. Now in order for the market to be in equilibrium, the quantity demanded at the price consumers pay, which includes the tax, must equal the quantity supplied at the amount the sellers receive after the government takes out the tax.

Figure 11.12 shows the new equilibrium. For now, don't worry about where the prices and quantities come from; we will take them as given. In figure 11.12, the new equilibrium quantity is shown as 450, the price paid by consumers is \$1.10, and the price received by producers is \$0.90. The consumer surplus was A+B+E but is now only A, and the producer surplus used to be C+D+F but is now only D. The revenue generated by the government from the tax on tomatoes is the area B+C. The tax creates a deadweight loss from the reduction in sales, and the deadweight loss is E+F. Total surplus includes consumer surplus, producer surplus, and government revenue: A+B+C+D. What policy makers must decide in general is whether the objectives achieved by the tax are worth the loss in efficiency represented by the deadweight loss, E+F.

Taxes on Buyers

Suppose the city of Lawrence decided to collect the \$0.20 tax from consumers as they left the farmers' market. For example, there might be a person with whom you have to check out as you leave, and this person counts your tomatoes and charges you the \$0.20 per tomato. How does this scenario change the graphical analysis?

Since the value to the consumer of a tomato has not changed, the willingness to pay remains the same. Thus a consumer that was willing to pay \$1 for a tomato is still willing to do so, but \$0.20 of that \$1 now goes to the city. So in essence, the consumer was willing to pay the farmer \$1 for the tomato but is now only willing to pay the farmer \$0.80. This is represented by the blue demand curve (D_2) in figure 11.13, which is the same as the previous demand curve but lowered by \$0.20, or the amount of the tax.

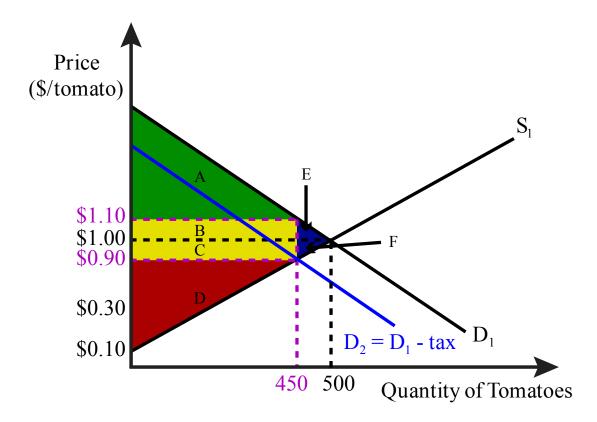


Figure 11.13 Effect of a tax on buyers of tomatoes at the Lawrence farmers' market

The effect on the new market equilibrium of a tax on buyers is identical to the effect of the tax on sellers. The tax itself creates a wedge between what buyers pay and what sellers receive, and the new equilibrium quantity is the same as before. Consumer surplus, producer surplus, government revenue, and deadweight loss are all the same as before. The lesson here is that it makes no difference on whom the government levies the tax; the tax does not stay where the government puts it. In this example, whether the tax is applied to the consumer or the seller, the consumer pays \$0.10 more than without the tax, and the seller receives \$0.10 less than without the tax.

Distribution of the Tax Amount

In our tomato tax example, the tax amount is shared equally between the sellers and buyers (\$0.10 each), but is this always true? The answer is no. How much of the tax burden falls on buyers and sellers depends on the elasticities of the supply and demand curves. The following figures illustrate this concept. **Figure 11.14** shows a relatively elastic demand curve with a relatively inelastic supply curve. The original pre-tax equilibrium price is P_1 , the post-tax price buyers pay is P_B , and the post-tax price sellers receive is P_S . In this case, the greater share of the burden of the tax falls on sellers, as can be seen by the fact that

 $P_1-P_S>P_B-P_1.$ We call the division of the burden of a tax on buyers and sellers the ${f tax}$ incidence.

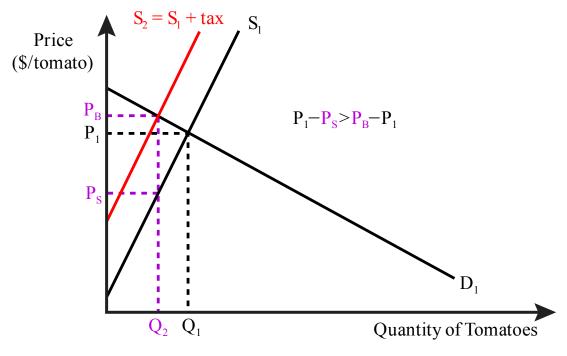


Figure 11.14 Tax incidence with inelastic supply and elastic demand

In **figure 11.15**, the supply curve is relatively elastic, the demand curve is relatively inelastic, and the majority of the tax incidence falls on the buyers, as can be seen by the fact that $P_B-P_1>P_1-P_S$

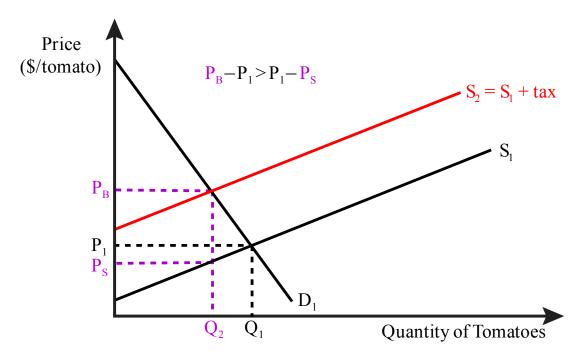


Figure 11.15 Tax incidence with elastic supply and inelastic demand

These tax-sharing effects make sense intuitively if we think about the meaning of elasticity. A more elastic curve means a larger quantity response to a change in price. Only a small part of the tax burden can be given to market participants that are more responsive to price and a larger part can be given to those that are less responsive to price because the quantity demanded and supplied must equal in the end.

Subsidies for Buyers

The effects of subsidies on markets are similar to taxes in that they create a difference between what consumers pay and what suppliers receive. They are also similar in that it does not matter if you subsidize the purchase of a good or the sale of a good; the market equilibrium effects are the same. In the next section, we'll consider in more detail the market equilibrium effects of a government policy to subsidize buyers of solar power installations. For now, we'll examine a simpler example to understand the mechanics of such a subsidy.

Let's go back to the Lawrence farmers' market. Suppose the city government decides that it is important to support the tomato growers. It will subsidize consumers in the amount of \$0.20 for each tomato they purchase. Suddenly, potential buyers who would have bought a tomato if the price was \$1 are now willing to buy a tomato that is priced at \$1.20 because their out-of-pocket cost is the same. We can see this effect in figure 11.16. In the figure, the demand curve is shifted up by the amount of the subsidy leading to an increased quantity purchased, Q_2 , and an increased equilibrium price, P_S .

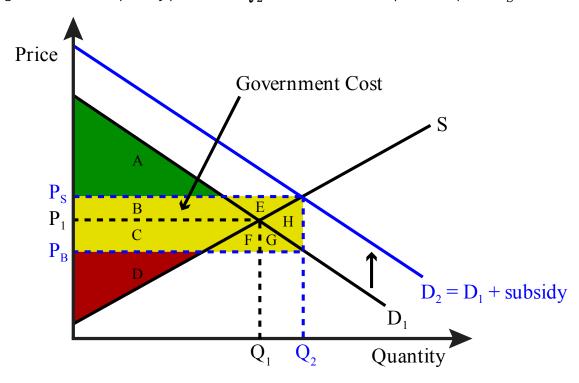


Figure 11.16 Effect of a subsidy on tomatoes at the Lawrence farmers' market paid to buyers

Tomato sellers are certainly helped by this policy. Producer surplus was C+D, and it is now B+C+D+E, so it has increased by B+E. Consumer surplus has also increased. Originally it was A+B. After the subsidy, it is A+B+C+F+G, so it has increased by C+F+G. To see this, remember that consumers are actually spending P_C on each tomato. So both consumer and producer surpluses have increased.

The government spends \$0.20 on each tomato sold, and Q_2 are sold, so the cost to the government of this policy is shown as the area B+C+E+F+G+H.

And how does welfare change with the implementation of the subsidy? Within the area of government expense, B+E is the new producer surplus, and C+F+G is the new consumer surplus. That leaves only the area H as government expenditure not offset by the new surplus. Therefore, H is the area of deadweight loss, and net welfare has decreased by H.

Subsidies for Sellers

Suppose instead of giving \$0.20 to buyers of tomatoes, the government gives it to the sellers of tomatoes. This subsidy is shown in figure 11.17 where the supply curve is shifted down by the amount of the subsidy. In this case, sellers who would have been willing to accept \$0.70 for a tomato will now accept \$0.50 for the same tomato because the government will give them the extra \$0.20. The effect on the market with respect to consumer surplus, producer surplus, government expenditure, and deadweight loss is identical to the case where the subsidy is paid to the buyers.

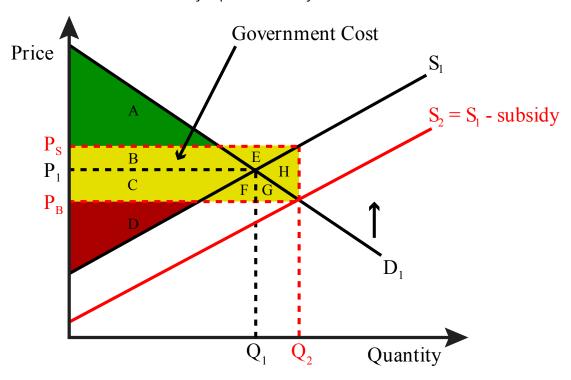


Figure 11.17 Effect of a subsidy on tomatoes at the Lawrence farmers' market paid to sellers

In fact, for both forms of subsidies, the true benefit is not the \$0.20 paid by the government but the price paid by consumers relative to the price without the subsidy. So the consumer benefit is P_1-P_C . Similarly, the producer benefit is the difference between the new post-subsidy price and the pre-subsidy price, or P_S-P_1 . The distribution of these benefits depends on the relative elasticities of the two curves, just as we saw with taxes.

11.5 THE POLICY QUESTION

SHOULD THE FEDERAL GOVERNMENT SUBSIDIZE SOLAR POWER INSTALLATIONS?

Learning Objective 11.5: Apply a comparative static analysis to evaluate government subsidies of solar panel installations.

The SITC is a 30 percent federal tax credit to buyers of solar systems for residential and commercial properties. This credit reduces the federal income taxes that a person or company pays dollar for dollar based on the amount of investment in solar property.

We know from <u>section 11.4</u> that the impact of a subsidy on a market does not depend on the designated receiver of the subsidy. In this case, the subsidy is paid to buyers of solar panels, both residential and commercial. What we need to properly analyze in this market is some notion of elasticity of the demand and supply for solar panels.

In general, studies have found residential energy usage to be fairly inelastic. This is because measures that consumers can take to save energy in response to price increases—like lowering the thermostat in winter and raising it in summer, turning off lights diligently, and using more energy-efficient light-bulbs—can only mitigate usage somewhat.

If this logic carries over to the solar panel market, the effect of the subsidy would look like **figure 11.18**. In this figure, the consumer surplus increases C+F+G, and the producer surplus increases B+E. It is clear from the figure that the larger share of the benefits from this policy accrues to consumers, but there is still a fair amount of deadweight loss, H. If the goal of the policy is to increase the consumption of solar panels, it has clearly succeeded, shifting consumption from Q_1 to Q_2 .

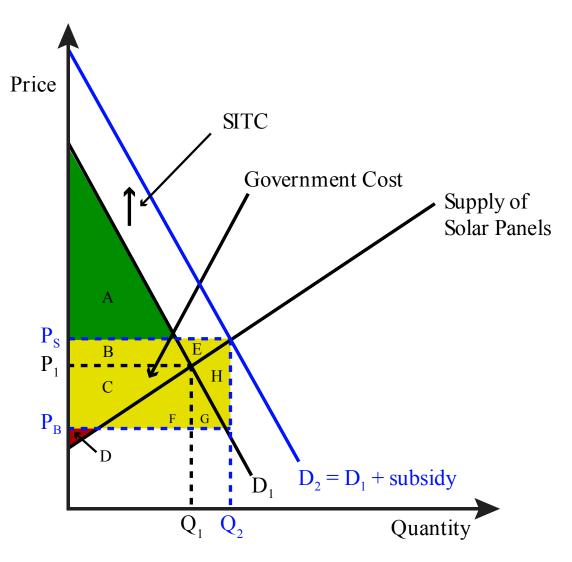


Figure 11.18 Effect of the solar investment tax credit (SITC) program on the market for solar panels with inelastic demand

However, it is probably not the case that the market for solar panels is the same as the market for residential energy. This is because solar panels represent only one form of energy, and close substitutes such as electricity delivered from the power plant, natural gas, and propane exist and are easily accessible for most homeowners. So it is quite likely that consumers have demands for solar panels that are quite elastic, as small movements in price could alter the comparative calculus between solar and other forms of energy a lot. If this is true, then our market would look a lot more like **figure 11.19**.

While similar to <u>figure 11.18</u>, **figure 11.19** is different in one crucial aspect. Our subsidy is likely to increase consumption more with an elastic demand curve than with an inelastic demand curve. It is also true that the increases in consumer and producer surplus are more equal and that there is still substantial deadweight loss.

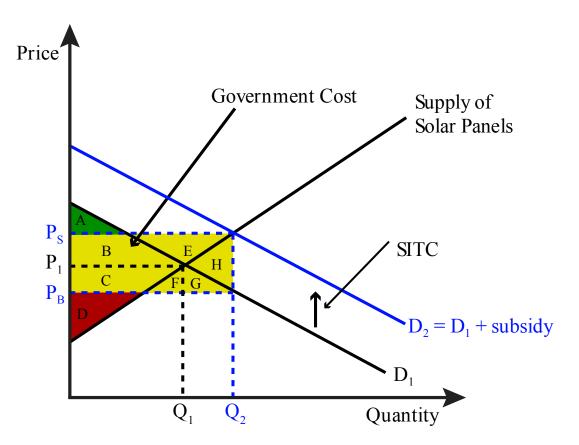


Figure 11.19 Effect of the solar investment tax credit (SITC) program on the market for solar panels with elastic demand

Our analysis shows that the SITC is likely to be successful in increasing the consumption of solar panels, but it will also be quite costly and create a lot of deadweight loss. Is it worth it? To answer this question, policy makers have to evaluate the benefit to society of increased reliance on solar power and compare it to the cost of the program in terms of both accounting costs (B+C+E+F+G+H) and deadweight loss (H).

EXPLORING THE POLICY QUESTION

- 1. What other ways could the government sponsor the installation of solar energy systems, and how would their effects differ from a subsidy to buyers?
- 2. Do you support the SITC subsidy? Why or why not?

REVIEW: TOPICS AND LEARNING OBJECTIVES

11.1 Changes in Supply and Demand

Learning Objective 11.1: Describe the causes of shifts in supply and demand and the resulting effects on equilibrium price and quantity.

11.2 Welfare Analysis

<u>Learning Objective 11.2:</u> Apply a comparative static analysis to evaluate economic welfare, including the effect of government revenues.

11.3 Price Ceilings and Floors

Learning Objective 11.3: Show the market and welfare effects of price ceilings and floors in a comparative statics analysis.

11.4 Taxes and Subsidies

Learning Objective 11.4: Show the market and welfare effects of taxes and subsidies in a comparative statics analysis.

11.5 Policy Example

Should the Federal Government Subsidize Solar Power Installations?

Learning Objective 11.5: Apply a comparative static analysis to evaluate government subsidies of solar panel installations.

LEARN: KEY TOPICS

Terms

Price ceiling

An artificial constraint that holds prices below their free-market levels.

Price floor

An artificial constraint that holds prices above their free-market levels.

Market-clearing price

An alternative term for <u>market equilibrium</u>; references the fact that the market is cleared of all unsatisfied demand and excess supply at the equilibrium price.

Tax

Money collected by a government from buyers or sellers directly or indirectly against services provided to the community.

Subsidy

An economic incentive given to remove some type of burden in the interest of market welfare. A subsidy drives a wedge, decreasing the price consumers pay and increasing the price producers receive, with the government incurring an expense.

Tax incidence

The division of the burden of tax between buyers and sellers. See figure 11.14 in sub-section "Distribution of the Tax Amount."

Graphs

Increase in demand causes equilibrium price and quantity to rise.

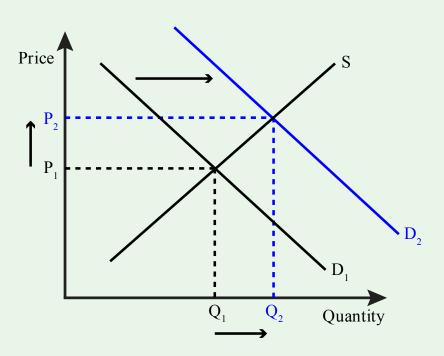


Figure 11.1 Increase in demand causes equilibrium price and quantity to rise.

Decrease in demand causes equilibrium price and quantity to fall.

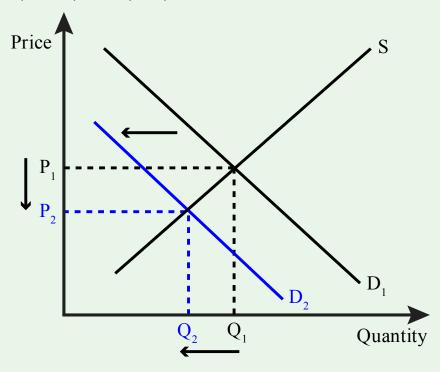


Figure 11.2 Decrease in demand causes equilibrium price and quantity to fall.

Decrease in supply causes equilibrium price to rise and quantity to fall.

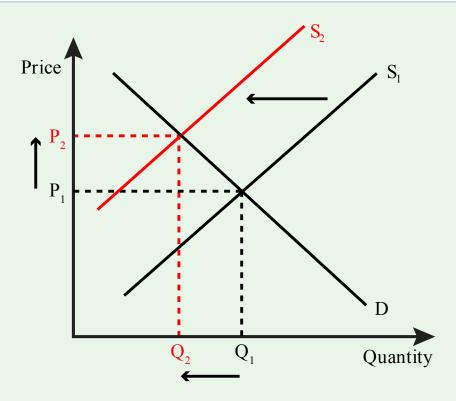


Figure 11.3 Decrease in supply causes equilibrium price to rise and quantity to fall.

Increase in supply causes equilibrium price to fall and quantity to rise.

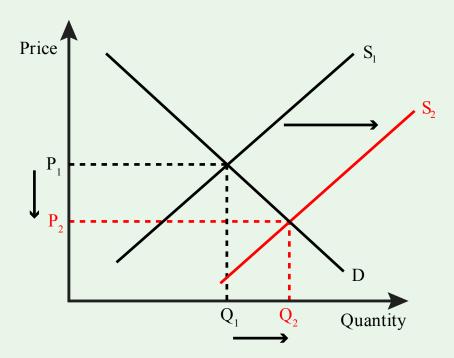


Figure 11.4 Increase in supply causes equilibrium price to fall and quantity to rise

Increase in demand and supply that causes equilibrium price and quantity to rise

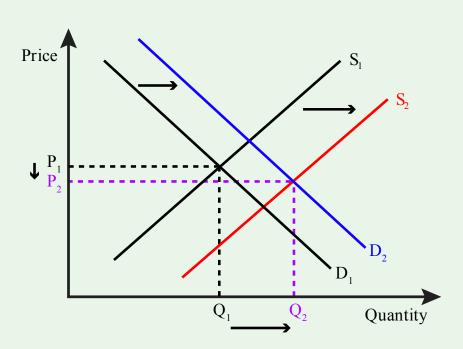


Figure 11.5 Increase in demand and supply that causes equilibrium price and quantity to rise

Increase in demand and supply that causes equilibrium quantity to rise and price to fall

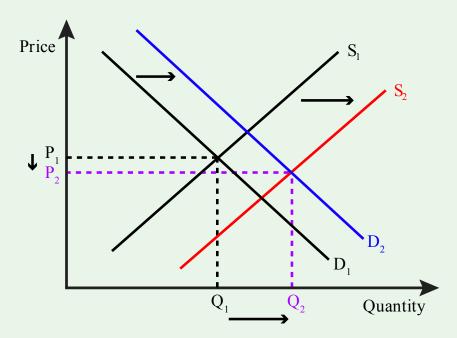


Figure 11.5 Increase in demand and supply that causes equilibrium price and quantity to rise

Increase in demand and decrease in supply cause equilibrium price to rise and have an ambiguous effect on quantity

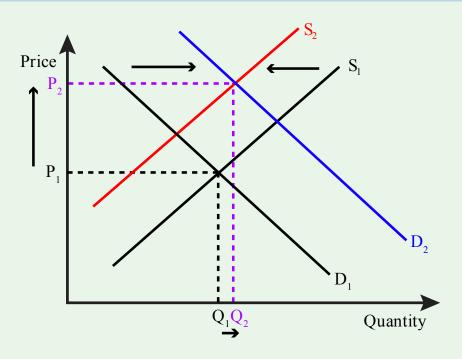


Figure 11.7 Increase in demand and decrease in supply cause equilibrium price to rise and have an ambiguous effect on quantity.

Increase in total welfare from an increase in demand

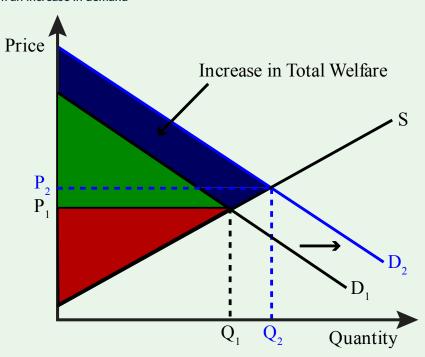


Figure 11.8 Increase in total welfare from an increase in demand

Welfare effects of shifts in both curves

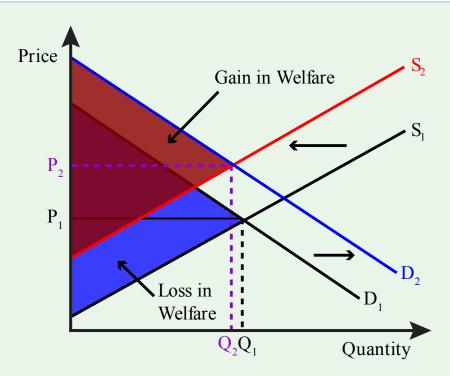


Figure 11.9 Welfare effects of shifts in both curves

Welfare effects of a price ceiling

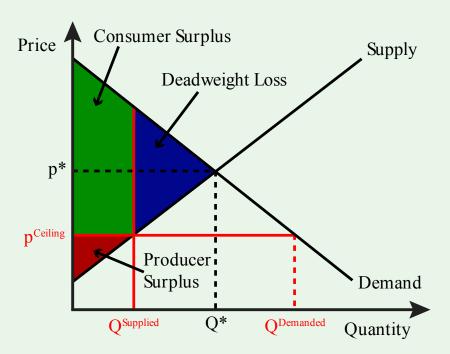


Figure 11.10 Welfare effects of a price ceiling

Welfare effects of a price floor

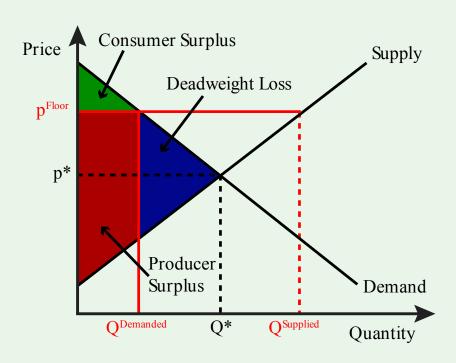


Figure 11.11 Welfare effects of a price floor

Effect of a tax on sellers of tomatoes at the Lawrence farmers' market

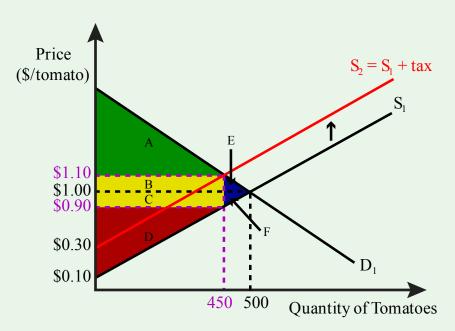


Figure 11.12 Effect of a tax on sellers of tomatoes at the Lawrence farmers' market

Effect of a tax on buyers of tomatoes at the Lawrence farmers' market

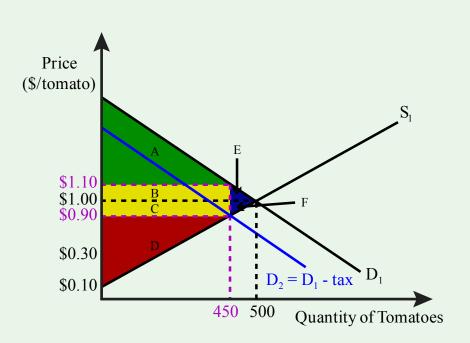
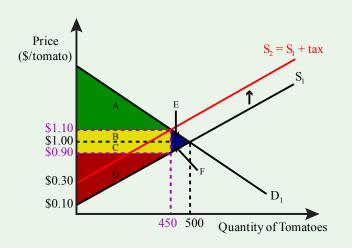
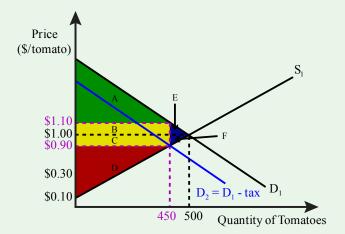


Figure 11.13 Effect of a tax on buyers of tomatoes at the Lawrence farmers' market

Figure 11.12 and 11.13 side by side for comparison





Tax incidence with inelastic supply and elastic demand

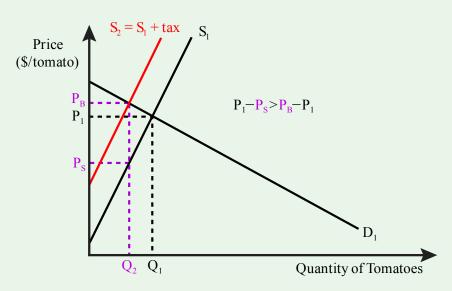


Figure 11.14 Tax incidence with inelastic supply and elastic demand

Tax incidence with elastic supply and inelastic demand

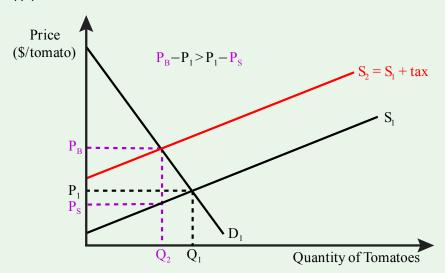


Figure 11.15 Tax incidence with elastic supply and inelastic demand

Effect of a subsidy on tomatoes at the Lawrence farmers' market paid to buyers

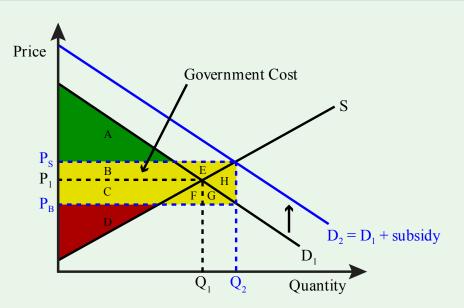


Figure 11.16 Effect of a subsidy on tomatoes at the Lawrence farmers' market paid to buyers

Effect of a subsidy on tomatoes at the Lawrence farmers' market paid to sellers

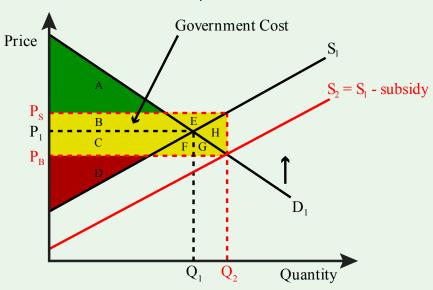


Figure 11.17 Effect of a subsidy on tomatoes at the Lawrence farmers' market paid to sellers

Effect of the solar investment tax credit (SITC) program on the market for solar panels with inelastic demand

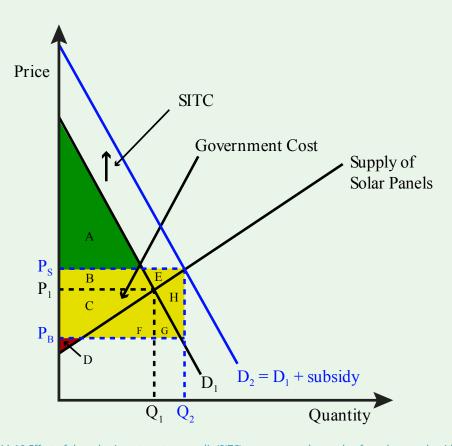


Figure 11.18 Effect of the solar investment tax credit (SITC) program on the market for solar panels with inelastic demand

Effect of the solar investment tax credit (SITC) program on the market for solar panels with elastic demand

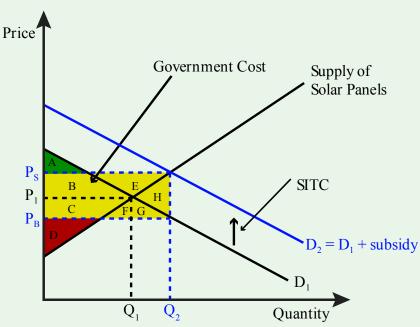


Figure 11.19 Effect of the solar investment tax credit (SITC) program on the market for solar panels with elastic demand

Price
SITC

Government Cost
Supply of
Solar Panels

Ps
P1
C
F G

 $D_2 = D_1 + subsidy$

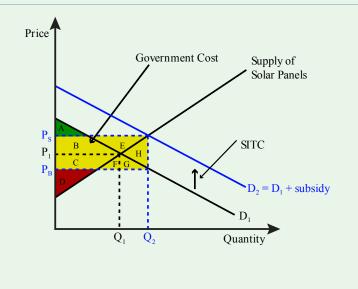


Figure 11.18 and 11.19 side by side for comparison

Table

Effects of shifts in both demand and supply

A table summarizing effects on price and quantity when demand and supply shift. Often the resut is ambiguous, as it depends on the market in question.

Table 11.1 Effects of shifts in demand and supply

| Demand | Supply | Change in price | Change in quantity |
|-----------|-----------|-----------------|--------------------|
| Increase | No change | + | + |
| Decrease | No change | - | - |
| No change | Increase | - | + |
| No change | Decrease | + | - |
| Increase | Increase | ? | + |
| Increase | Decrease | + | ? |
| Decrease | Increase | - | ? |
| Decrease | Decrease | ? | - |

Results of adjustments to demand and supply graphs in a grid for comparison

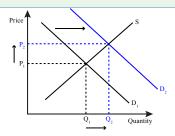


Figure 11.1 Increase in demand causes equilibrium price and quantity to rise.

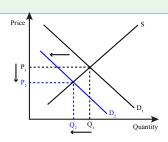


Figure 11.2 Decrease in demand causes equilibrium price and quantity to fall.

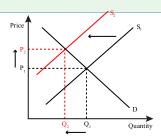


Figure 11.3 Decrease in supply causes equilibrium price to rise and quantity to fall.

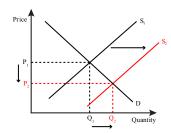


Figure 11.4 Increase in supply causes equilibrium price to fall and quantity to rise

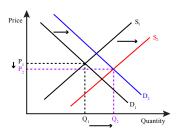


Figure 11.5 Increase in demand and supply that causes equilibrium price and quantity to rise

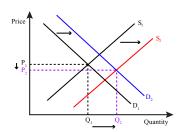


Figure 11.6 Increase in demand and supply that causes equilibrium quantity to rise and price to fall

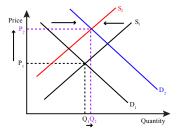


Figure 11.7 Increase in demand and decrease in supply cause equilibrium price to rise and have an ambiguous effect on quantity.

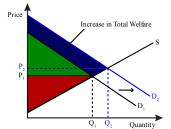


Figure 11.8 Increase in total welfare from an increase in demand

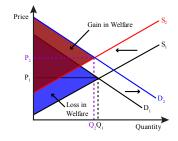


Figure 11.9 Welfare effects of shifts in both curves

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CHAPTER 12

Input Markets

THE POLICY QUESTION

SHOULD THE STATES OF OREGON AND NEW JERSEY PROHIBIT SELF-SERVICE GAS?

Only two states in the United States do not allow self-service gas stations: in Oregon and New Jersey, customers are not permitted to pump their own gas. Originally, this policy was driven by safety concerns—gasoline was considered a hazardous substance due to its flammability and the adverse health effects of touching it or inhaling fumes. However, advances in pump technology have made the self-pumping of gas safe enough that forty-eight states and the District of Columbia have allowed self-service gas for decades. Efforts to repeal the prohibition in Oregon and New Jersey have failed, and one of the key arguments from groups that defend the policy is that the repeal would lead to job losses. Economists often claim that policies that mandate employment are inefficient and cause a drag on the economy itself.

In this chapter, we will look at input markets and study labor markets in particular. Labor is an input in retail gas, so we will be able to study this policy in depth and think about the economic implications. We can also use what we have learned so far about product markets to think through the implications for consumers.

EXPLORING THE POLICY QUESTION

- 1. Do you think prohibiting self-service gas is a good policy? Why or why not?
- 2. Do you think that policies such as this one help ensure that there is adequate employment?

LEARNING OBJECTIVES

12.1 Input Markets

Learning Objective 12.1: Explain how changes in input markets affect firms' cost of production.

12.2 Labor Supply

<u>Learning Objective 12.2</u>: Describe how individuals make their labor supply decisions and how this can lead to a backward-bending labor supply curve.

12.3 Competitive Labor Markets and Monopsonist Labor Demand

Learning Objective 12.3: Explain how monopsonist labor markets differ from competitive labor markets.

12.4 Minimum Wages and Unions

Learning Objective 12.4: Show the labor market and welfare effects of minimum wages in a comparative statics analysis.

12.5 Policy Example

Should the Government Prohibit Self-Service Gas?

<u>Learning Objective 12.5</u>: Apply a comparative statics analysis to evaluate government prohibitions of self-service gas on labor markets and the market for retail gas.

12.1 INPUT MARKETS

Learning Objective 12.1: Explain how changes in input markets affect firms' cost of production.

In <u>chapter 6</u>, we learned that when firms produce a good or service, they do so by combining various inputs. These inputs, also known as factors of production, have a price. For example, we learned that capital has a price called the rental rate and labor has a price called the wage. But inputs can be almost anything, like aluminum for auto manufacturers, cocoa beans for chocolate makers, or fresh produce for a restaurant. When firms buy these inputs, they do so in goods markets and act as consumers just like those in our demand models. In that way, input markets are just the same as the markets we have already studied. In most cases, the markets work like the goods markets we have studied, but there are some important exceptions, and we will study two in this chapter.

The first exception comes from the input used by virtually every producer, labor. Labor markets have particular features that make them different than normal product markets. The first is that labor is not a good or service supplied by a firm but the physical and mental effort exerted by individuals in exchange for a wage. There are both physical constraints on the supply of labor—a person cannot supply more than twenty-four hours' worth in a day—and constraints that come from individuals' decisions to consume leisure time as well as tangible goods and services.

The second exception comes from the fact sometimes suppliers of inputs supply a single company. Thus the purchasing company acts as a **monopsonist**: a single buyer for goods or services sellers. **Monopsony** is the term used to describe a market in which there exists only one buyer for a good. Monopsonies are rare, but they do exist. Examples are the market for sophisticated weaponry for which there is only one legal buyer, the Department of Defense, and the market for labor in "company towns" where one firm employs most of the workers in the town.

Before studying the exceptions, let's take a look at a typical input market that acts as a normal goods market, with many sellers and many buyers. Consider a company like Dell that sells PC computers fully assembled and ready to use. This company may make component parts themselves but also likely purchases component parts from other suppliers as well. Let's suppose that Dell buys computer hard drives (HDD) from various suppliers. There are many manufacturers of computer hard drives and many potential buyers, including individuals who wish to build or upgrade their own computers, so the computer hard drive market is very typical of a standard goods market.

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Note that the hard drive market is both an input market, as hard drives are inputs in the manufacture of Dell computers, and a final goods market, as hard drives are also final purchases of consumers. Some goods, like raw iron, are almost exclusively inputs because there is no demand for raw iron as a final consumer good. A good that is used as an input to produce other goods is called an **intermediate good**. Other goods, like a pair of denim jeans pants, are purchased by the end user. Such a good is called a **final good**. And some goods, like computer hard drives, are both intermediate and final goods.

Manufacturers like Dell purchase computer hard drives in product markets along with regular consumers, though they typically buy direct from the manufacturers and not through retailers, as do consumers. Regardless, the price they pay for their hard drives is set by the hard drive goods market, as illustrated in **figure 12.1**, which shows the market for one particular type of drive: the one-terabyte HDD (1TB HDD).

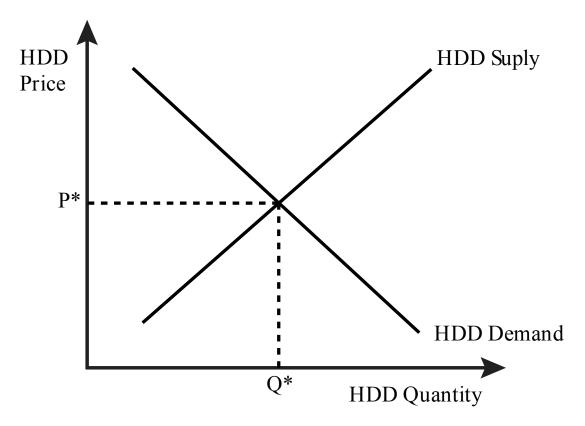


Figure 12.1 The market for one-terabyte computer hard drives (1TB HDD)

In **figure 12.1**, there are many suppliers of hard drives and many demanders. The demanders are both manufacturers and consumers. Since this is the market for wholesale 1TB HDDs, consumers are represented by retailers like Best Buy, Amazon, and New Egg. The price of a 1TB HDD is determined by the market as P^* . This P^* is an input price for computer manufacturers, just like the rental rate on capital, r, and the wage rate for labor, w, as we studied in <u>chapter 6</u>. The same market dynamics of goods markets apply here: when demand or supply changes, prices will change as well. For example, if new manufacturers of 1TB HDD enter the market, the price for these goods will fall. If there is a new substitute for 1TB HDD, like solid-state hard drives, demand could fall, which would also lower the price of the good.

Price changes in the input markets will affect the cost conditions of firms, as we saw in <u>chapter 6</u>, and will, in turn, affect the supply of the final good. As input prices rise, the supply curve in the final good

market shifts to the left, and the price of the final good rises. As input prices fall, the supply curve of the final good market shifts to the right, and the price of the final good falls.

As noted above, the typical behavior of input markets changes when the input is labor or when the buyer of the input is the only buyer. We study these two instances in the next two sections.

12.2 LABOR SUPPLY

Learning Objective 12.2: Describe how individuals make their labor supply decisions and how this can lead to a backward-bending labor supply curve.

Almost every final good produced has some labor input involved, if not as part of the manufacturing process then as an ancillary contribution through administration, marketing, sales, and so forth. For this reason alone, labor has an outsized role in production and deserves special attention. Another particular aspect of labor that requires special attention is the fact that it is an input provided by individuals making optimal decisions about work and leisure.

The labor market is where labor prices, or wages, are set and is defined by the same supply-and-demand dynamics as other input markets. The supply of labor is determined by the labor-leisure choice of individuals. Individuals think about the trade-off between working more and earning more money, which can be used to purchase goods and services, and working less and having more time to enjoy leisure activities and perform chores that are necessary but for which there is no monetary compensation.

The labor-leisure choice is the starting point for thinking about labor markets. We can model this choice just as we do consumers deciding between bundles of two different goods. Both leisure and the income from labor are goods that reflect standard preferences: individuals would prefer more of both, and a mix of both income and leisure is preferable to too much of one or the other. Thus we can describe an individual's preferences by a utility function of income (I) and leisure (I):

$$U = U(I, l)$$

Individuals cannot spend more than twenty-four hours per day in either activity. We can write down a constraint that describes this as

$$H=24-l_{r}$$

where H is the hours spent working in a day and I is the amount of leisure consumed in a day. For a given hourly wage rate, w, the income earned by a consumer, I, is given as

$$I=wH$$
.

Recall that in <u>chapter 4</u>, where we studied the consumer choice problem, we took income (I) as given to the consumer. In this discussion, we will see that I is a result of a decision the individual makes about how much labor to supply to the labor market.

Figure 12.2 shows the optimal choice between leisure and income for an individual, Asha, and how it is determined. Asha's income is measured on the vertical axis, and the amount of leisure hours per day she consumes is measured on the horizontal axis. Since there are only twenty-four hours in a day, Asha cannot consume more than twenty-four hours of leisure. Note that the less leisure she consumes, the more time she spends on labor and the more income she earns.

Figure 12.2 shows Asha's budget constraint line in black. If the wage rate is w_1 , the budget constraint has the slope of $-w_1$. This is because for every extra hour of leisure she consumes, she loses w_1 in income. The highest indifference curve Asha can achieve is given as U_1 and is shown in red. Maximizing her utility at the wage rate of w_1 yields a choice of I_1 in income and I_1 in leisure.

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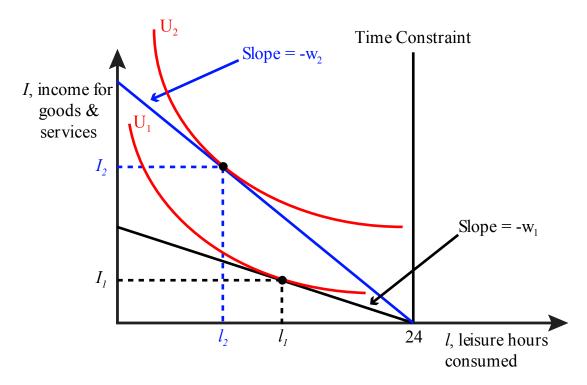


Figure 12.2 The optimal labor-leisure choice problem

Now, what happens when the wage rate increases to w_2 ? Asha's new budget constraint, shown in blue, lies above the old budget constraint. This is because at a higher wage, Asha gets more income for every hour spent working or not consuming leisure. The highest indifference curve she can achieve at this budget constraint is given as U_2 . How does Asha adjust her consumption? Since the opportunity cost of leisure has increased, she gives up more income when she consumes leisure and she consumes less leisure. Maximizing her utility at the wage rate of w_2 yields a choice of I_2 in income and I_2 in leisure.

From the solutions to this optimal labor–leisure choice problem, we can derive the demand curve for leisure for Asha (**figure 12.3**).

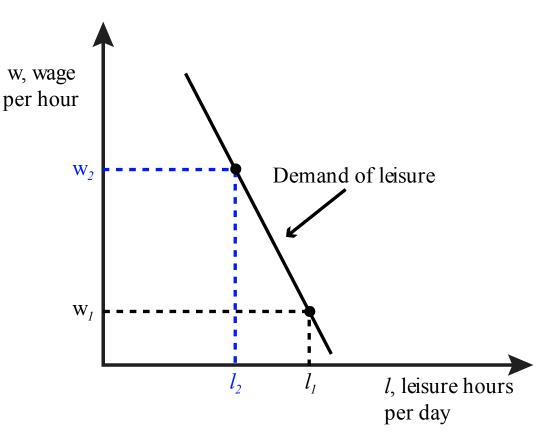


Figure 12.3 An individual's leisure demand curve

At wage w_1 , Asha consumes l_1 hours of leisure, and at wage w_2 , Asha consumes l_1 hours of leisure. Her demand for leisure is a curve that connects these two points. Note that the wage rate is the cost or price of leisure; as it increases, Asha demands less leisure. Going from Asha's demand for leisure to her supply of labor simply requires that we subtract her leisure demand from the twenty-four hours available to Asha to spend on both labor and leisure, H=24-1, where H=24-1 is the work hours per day. Figure 12.4 illustrates Asha's labor supply curve.

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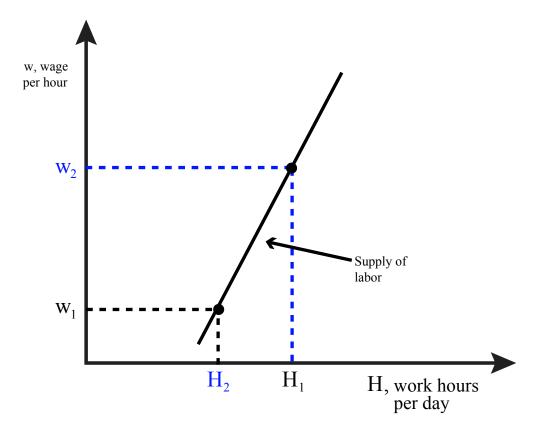


Figure 12.4 An individual's labor supply curve

Asha's labor supply curve, as depicted in **figure 12.4**, is an upward-sloping curve. The curve shows that the effect of an increase in the wage is an increase in hours of labor supplied from H_1 to H_2 . This change, however, is the net effect of both the income and substitution effects, which we studied in chapter 5.6. The income effect refers to the fact that as the wage rises, Asha has more money to spend on both leisure and other goods, and if the goods are both normal, she will want to consume more of both. The substitution effect refers to the fact that as the wage rises, leisure becomes more expensive relative to the consumption of other goods, and Asha will naturally substitute away from leisure and toward the increased consumption of other goods, as enabled by more work at the higher wage. If the substitution effect dominates the income effect, then her labor supply will be upward sloping, as in figure 12.4.

Suppose, however, that the income effect dominates the substitution effect. In this case, Asha will choose to consume more leisure as her wage rises, and her labor supply curve will be backward bending. This might be more likely as wages rise high enough that individuals can satisfy much of their material consumption desires *and* increase their consumption of leisure. Put another way, there may be a point where increased income causes individuals to actually choose to work less so that they can have more time to enjoy the consumption of their goods, services, and leisure. **Figure 12.5** shows three different wages and the corresponding leisure choice for each. **Figure 12.6** illustrates the resulting labor supply curve, which starts positively sloped but then bends backward at higher wages.

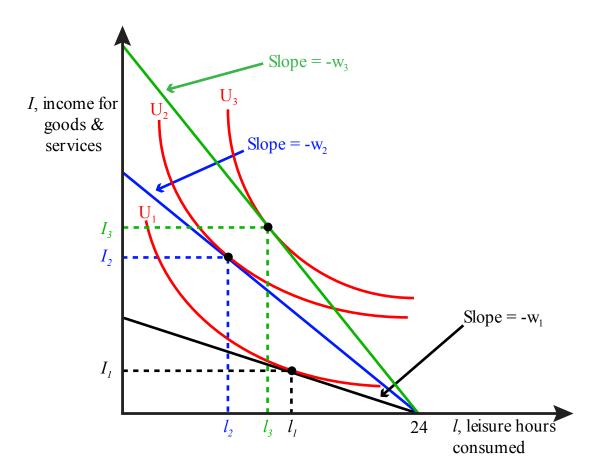


Figure 12.5 The backward-bending labor supply curve: the labor-leisure choice

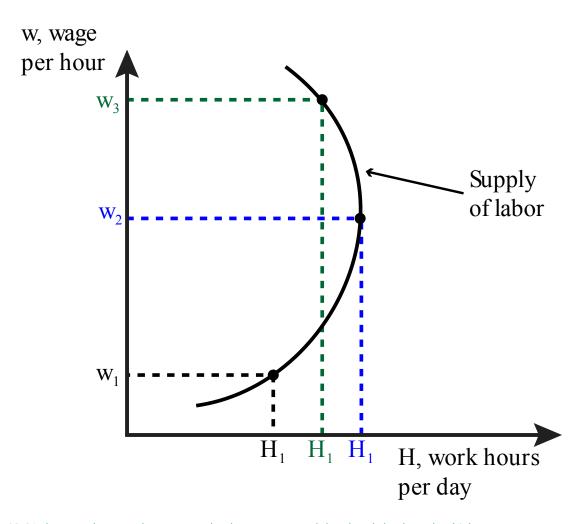


Figure 12.6 Labor supply curve slopes upward at lower wages and then bends backward at higher wages.

When the wage rises from w_1 to w_2 , Asha decides to work more hours and consume less leisure. However, when wages rise from w_2 to w_3 , Asha decides that her income is high enough that she would like to consume more leisure and work less. That is, her new wage allows her to consume more of both goods (leisure and all other goods). In this case, the income effect, which causes her to want to consume more of both goods, outweighs the substitution effect, which causes her to substitute away from the relatively more expensive good, leisure, and toward the relatively less expensive good, consumption of other goods.

This analysis shows that a backward-bending labor supply is theoretically possible, but do such labor supply curves actually exist? Only empirical research can answer this question. But there are some assumptions that are not quite accurate for many workers, the first being the characterization of the labor-leisure choice. Most workers cannot choose independently how many hours per day they work. Many jobs have specified work hours, and in the United States, many jobs are forty hours a week with very little room for adjustment. So when employers raise wages, there may be no way for employees to adjust their hours in response. Empirical research suggests that for men, this rigidity in hours might be very important, as their labor supply curves have been estimated to be nearly vertical.

12.3 COMPETITIVE LABOR MARKETS AND MONOPSONIST LABOR DEMAND

Learning Objective 12.3: Explain how monopsonist labor markets differ from competitive labor markets.

Another way that input markets can be different than a typical goods market is when there is only one buyer of an input. Monopsony is the situation where there are many sellers but only one buyer of a good. Consider an advanced weapon system that by law can only be sold to the government or a factory town where almost all the resident workers are employed by a single factory.

The case of professional American football players in the United States is a good example. The National Football League (NFL) is the only major professional American football league in the world, and while there are a few other options, like the Canadian Football League, they pale in comparison to the NFL. In labor market terms, the NFL acts a lot like a single entity with strict rules about hiring that prevent teams from competing with each other for new talent. Each year there are many sellers of labor, the football players, and one buyer, the NFL.

Competitive Firms' Employment Behavior

How are monopsonists different than competitive firms in a labor market? To answer this, let's first look at competitive firms' hiring decisions. In a competitive labor market, each firm has no influence on the equilibrium market wage, so no matter how many workers or worker hours a firm employs, the wage will remain constant. Thus a firm's decision is to continue to employ workers as long as the value of their marginal product of labor (MP_L) is greater than the wage. Recall that MP_L is the extra output achieved from the addition of a single unit of labor. For our discussion here, the unit is an hour of work. The **marginal** revenue **product of labor** (MRP_L) is the value of the marginal product of labor—it is the extra revenue a firm receives for an additional unit of labor. Therefore, the MRP_L is the product of the marginal product of labor and the marginal revenue, MR, that accrues to the firm from one additional unit of output:

$$MRP_L = MR \times MP_L$$

A firm will continue to add additional hours of labor as long as that additional labor adds positively to profits. The cost of an hour of labor is w, and the benefit is precisely the MRP_L . So as long as $MRP_L>w$, the firm is adding to its profits. If the $MRP_L< w$, the firm can increase its profits by reducing the number of labor hours it uses. The firm maximizes its profits from its employment decisions only at the point where the $MRP_L=w$. So we can characterize the firm's employment rule as

$$MRP_L=w$$

In a competitive output market, the MR is equal to the price that each unit sells for in the market, or the market price, p. So $MRP_L=p\times MP_L$. The firm's employment rule becomes

(12.1)
$$p imes MP_L = w$$

Dividing both sides by MP_L yields

$$p=w/MP_L$$

We know from <u>chapter 9</u> that profit maximizing firms produce to the point where marginal revenue equals marginal cost. Marginal revenue is p, as we just discussed, so the profit maximizing rule is

$$p = MC$$

Putting together the employment rule and the profit maximization rule, we get

$$p=w/MP_L=MC$$

Recall from section 6.3 that as the firm adds incremental units of labor, the MP_L increases up to a certain point and then begins to fall due to inefficiency. Beyond this point, the firm must reduce units of labor in order to increase MP_L . We can combine this fact with the expression of labor demand in equation (12.1) to explain the firm's employment behavior.

Specifically, with p fixed from the final goods market, as w rises, the firm will reduce worker hours in order to increase MP_L and so maintain the equality in (12.1). We can see this in **figure 12.7**, which shows in black the labor demand curve, D, when price is p. At wage w_1 , the firm will employ L_1 hours of labor; when wages rise to w_2 , the firm will reduce employment to L_2 . This is a shift along the labor demand curve as wages change.

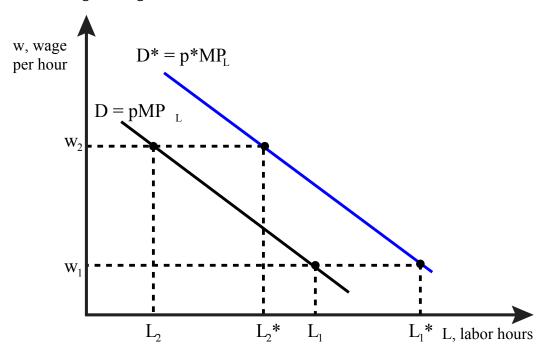


Figure 12.7 The labor demand curve and wage and price changes

What happens when the price of the final good changes? Well suppose the price rises from p to p^* . This means that the MRP_L rises as well, and so temporarily, the $p \times MP_L > w$. The firm can now add more workers to lower the MP_L until the equality of the MRP_L to w is restored. We see this in **figure 12.7** as a shift in the labor demand curve from p (in black) to p^* (in blue). Now at wage p^* , the firm will employ p^* hours of labor, and when wages rise to p^* , the firm will reduce employment to p^* .

To summarize the results of wage and price changes on the labor demand curve,

- a change in wage results in a shift along the labor demand curve, and
- a change in *price* results in a shift *of* the labor demand curve.

Wages and Labor Market Equilibrium

How is the wage amount set in a competitive labor market? To find labor market equilibrium, we must first derive the market supply of labor and the market demand for labor.

The market supply of labor is simply the sum of the labor supplied by all individual workers. **Figure 12.4** showed an individual labor supply curve; the market labor supply curve is illustrated in **figure 12.8**. Labor hours, L, is simply all the individual work hours per day, H, for every potential worker. As the wage increases, the number of workers and the number of hours each worker is willing to work increase as well, and the result is an upward-sloping curve.

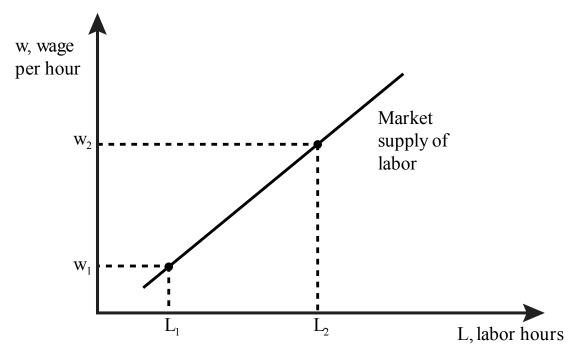


Figure 12.8 The market supply of labor

We find the market demand for labor by summing up the individual firms' labor demands. Once we have the market demand for labor, we can graph it together with the market supply of labor, as shown in **figure 12.9**. Doing so reveals the labor market equilibrium, identical to the equilibrium in other goods markets, and the resulting equilibrium wage rate, w^* , and total employment, L^* .

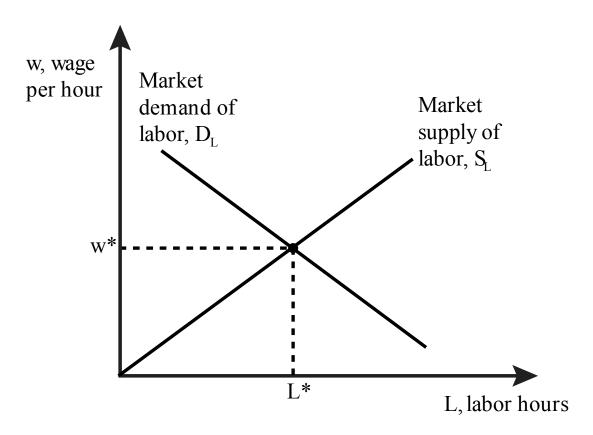


Figure 12.9 Labor market equilibrium

As **figure 12.9** shows, we call the market demand for labor D_L and the market supply of labor S_L . Where they cross is the equilibrium point, and the wage and labor hours at that point are the equilibrium wage rate, w^* , and equilibrium employment, L^* , respectively.

Monopsony Employment Behavior

In a competitive labor market, the wage amount is set by the market equilibrium of labor supply and demand, and the firm must pay that wage in order to attract workers. But when the firm is a monopsonist in the labor market, it has the power to influence the wage amount, w, and does not take it as fixed.

A competitive firm takes the wage as given and can hire as many work hours as it likes at that wage. We call the **marginal expenditure** (ME) the extra cost of hiring one more unit of labor. The ME for a competitive firm of an additional hour of labor is simply the market wage.

A monopsonist must also pay a wage to attract workers, but this wage depends on the labor supply curve. For example, suppose that at a wage of \$20 per hour, a monopsonist firm attracts one thousand hours of workers per week for a total weekly wage bill of \$20,000. Now suppose the price of its product has increased, and it wants to increase production. To do so, the firm will have to hire more work hours by raising the wage.

Suppose that at \$25 per hour, the firm now attracts twelve hundred hours of workers. The firm's total wage bill has now increased not just by the extra two hundred hours of work at \$25, or \$5,000, which would increase its wage bill to \$25,000. Rather, it now pays for all of its labor hours at \$25. This increases the wage bill to \$30,000 ($1,200 \times \25). So the marginal expenditure, ME, of an additional hour of

labor is not just the additional wage the firm has to pay for that hour of work but the additional wage the firm has to pay for all hours of work.

Figure 12.10 illustrates the marginal expenditure curve for a monopsonist firm. The ME curve lies above the market supply of labor curve because of the fact that the firm cannot pay for one additional hour of work at a slightly higher rate than the rest. It must pay the same wage for all hours of work. The firm is therefore setting its MRP_L equal not to the wage but to the ME. We can state this insight about labor market equilibrium in the case of a monopsonist firm as

$$MRP_L = ME$$
.

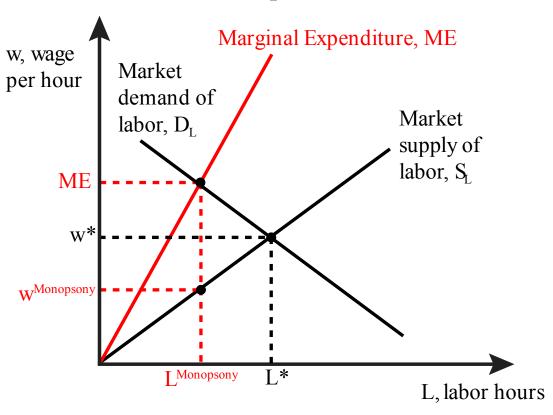


Figure 12.10 Monopsony and the marginal expenditure curve

For a monopsonist firm, the MRP_L curve is the labor demand curve. The firm's optimal employment decision is where $ME=D_L$. This occurs at $L^{\mathrm{Monopsony}}$. To attract this amount of labor, the firm must pay $w^{\mathrm{Monopsony}}$ —the point on the supply curve that yields precisely $L^{\mathrm{Monopsony}}$. We can see from **figure 12.10** that the monopsonist will hire fewer hours of labor ($L^{\mathrm{Monopsony}}$) than would occur in a competitive market (L^*) and pay a lower wage ($w^{\mathrm{Monopsony}}$) than in a competitive market (w^*).

12.4 MINIMUM WAGES AND UNIONS

Learning Objective 12.4: Show the labor market and welfare effects of minimum wages in a comparative statics analysis.

In a monopsonist labor market, the *buyer* of labor—the firm—has some power to set wages rather than accepting a market-driven rate. In other contexts, the *sellers* of labor—workers—may enjoy an advantage in determining wage rates, employment levels, or both. These advantages can be achieved through collective bargaining, for example, or public policy approaches, such as setting a minimum wage.

In the United States, it is illegal to pay workers below the federally mandated minimum wage, currently set at \$7.25 an hour. Many states have set minimum wages above this level; in 2015, Washington was the state with the highest minimum wage, at \$9.47 an hour. There are many reasons for these policies, but the most common rationale, often expressed by those who champion even higher minimum wages, is that wages are too low and do not represent a "living wage"—a wage high enough to afford the basic necessities of food, shelter, and clothing. In other words, minimum wages are a policy tool to address poverty.

To analyze minimum wages, we start by recognizing that they are price floors in the labor market, similar to the price floors in goods markets that we studied in chapter 11. A minimum wage set above the market equilibrium wage moves the market leftward on the market demand for labor curve, as **figure 12.11** shows. As a result, fewer employers are able to enter or remain in the market, and existing employers demand fewer hours of labor at the minimum wage than at the market equilibrium wage, w^* . At the same time, more workers are interested in entering the market, and existing workers are willing to work more hours at the higher minimum wage than at the market equilibrium wage. This difference between the number of hours that workers would like to work (L^{supplied}) and the number of labor hours that employers demand (L^{demanded}) leads to an excess supply of labor at the minimum wage, as shown in **figure 12.11**.

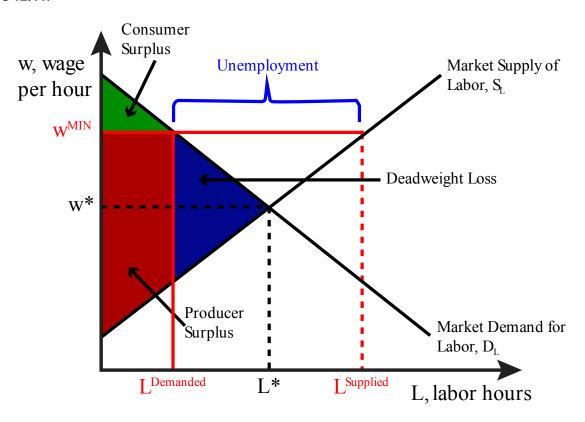


Figure 12.11 Minimum wage in a labor market

Economists describe the difference between the employment level at the equilibrium wage, L^* , and the employment level at the minimum wage, L^{demanded} , as the **disemployment effect**: the amount of employment lost due to the minimum wage. We refer to the difference in the amount workers would like to work at the minimum wage and the amount they actually do work as unemployment. **Unemployment**

occurs when there are people who would like to work at a given wage but are unable to find employment.

Unions are labor groups that bargain collectively for wages for a group of workers in a company. Their objective is to leverage collective bargaining to achieve higher wages than would have occurred in the individual labor market. In this sense, then, we can think of the result of unions in a similar way to minimum wages set by governments: they create a price floor in labor markets.

How do wage floors affect the welfare of workers and firms? Put another way, how do wage floors affect producer surplus and consumer surplus? Remember that in the context of labor, workers are the producers and firms are the consumers.

Let's start by looking at the producers. Those workers able to find employment at the new wage and equal in hours to what they had at the previous wage are better off because they receive higher compensation for the same work. Workers who are unable to find work at the new wage and who had work at the old wage are worse off; they want to work but cannot and so have no compensation. Workers who did not work prior to the minimum wage and continue not to work after it see no change in their welfare.

Producer surplus for those that have work rises. But remember the caveat from <u>chapter 11</u>: this assumes that we are employing only those on the lowest part of the supply curve. There is no mechanism to ensure this, so the producer surplus shown in <u>figure 12.11</u> is really a maximum possible surplus, and it is likely to be substantially lower.

On the firm side, consumer surplus falls. This occurs because firms must pay more for the workers they employ, and they employ fewer workers. Overall, societal welfare falls unequivocally, as seen in **figure 12.11**. The new wage creates deadweight loss, signifying a lower level of total surplus than prior to the wage floor due to the lower overall level of employment.

Studies that have looked at the impact of minimum wage laws have found different results. The broad picture appears to be that minimum wages do have a disemployment effect but that the effect tends to be quite small. The likely reason for this is the relative inelasticity of labor supply and demand curves at the bottom edge of the wage scale.

Inelastic labor demand and supply mean that the labor demanded and labor supplied are very insensitive to changes in wages. **Figure 12.12** shows this inelasticity as very steeply sloped labor demand and supply curves. The graph shows that as wage is raised to a minimum above the competitive wage, there is very little impact on labor demanded and labor supplied. As a result, the difference between the two—that is, unemployment at the minimum wage—is relatively small, as is the deadweight loss.

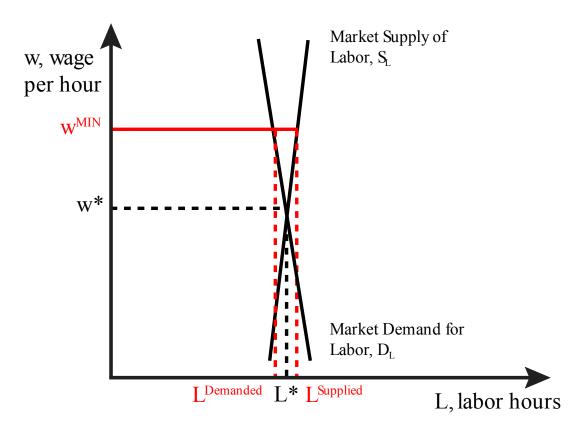


Figure 12.12 Minimum wages with inelastic labor demand and supply

A final question we might ask is whether minimum wages are effective poverty-fighting tools. In this case, the evidence is more mixed. In the United States, relatively few of those working for minimum wages are key income earners for poor households. Many of these jobs are held by teens and young adults who work part time for some extra income and are from wealthier households. So while there seems to be a fairly limited detrimental impact associated with minimum wages, economists tend to prefer more targeted policies for fighting poverty, like the earned income tax credit, which transfers money directly to the poorest working households.

12.5 POLICY EXAMPLE

SHOULD THE GOVERNMENT PROHIBIT SELF-SERVICE GAS?

Learning Objective 12.5: Apply a comparative statics analysis to evaluate government prohibitions of self-service gas on labor markets and the market for retail gas.

The prohibition on self-service gas in New Jersey and Oregon is, in essence, a mandate that retail gas stations employ workers who perform the task of pumping gas into cars. In the labor market for gas station workers, this policy has the effect of increasing the demand for labor. In fact, such a policy has the double effect of increasing both employment and wages, as shown in **figure 12.13**.

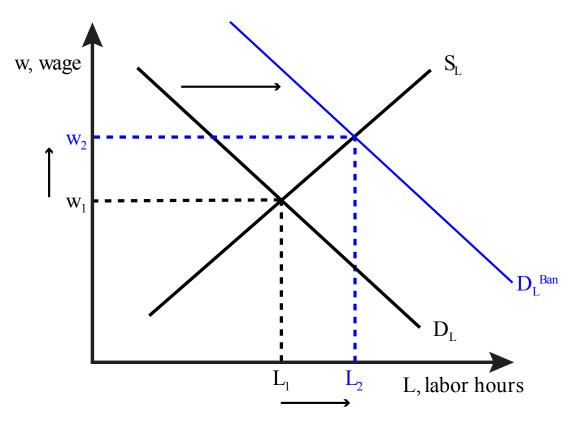


Figure 12.13 Effect on wages and labor hours due to a ban on self-service gas

To analyze our policy question, let's suppose that a state that does not currently have a ban on self-service gas imposes one. The resulting change in the demand for labor is the blue curve in **figure 12.13**.

Here we see that employment in the form of labor hours increases from L_1 to L_2 and wages increase from w_1 to w_2 . If this was the end of the story, we might be tempted to conclude that the ban on self-service gasoline is unequivocally good.

However, we now have enough economic analysis tools to understand that labor is an input in the production of retail gas and that when the cost of this input increases, the supply curve of retail gas shifts up, as **figure 12.14** shows. The increase in the cost of the labor input is due not only to the increased wage but also to the increased amount of labor required to pump gas. The increased cost of supplying a gallon of gas will cause retailers to supply less, shifting the supply curve leftward from S to $S^{\rm Ban}$.

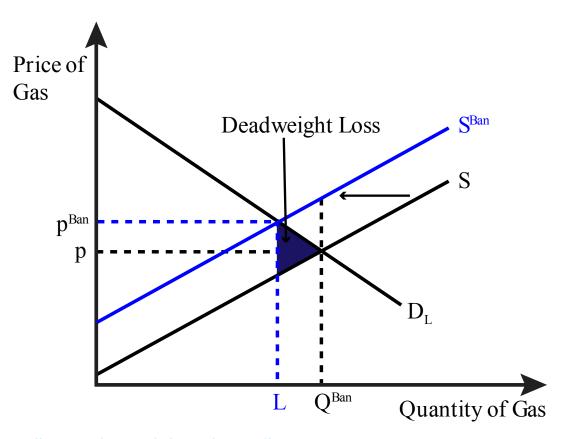


Figure 12.14 Effect on retail gas supply due to a ban on self-service gas

The leftward supply shift has the effect of increasing the price of gas to consumers and decreasing the amount they purchase, leading to deadweight loss. The policy question becomes, "How big is this deadweight loss to society compared to the benefit to society of the increased employment among gas station attendants?"

We can gain some insight into this question by comparing the states of Oregon and Washington. Oregon prohibits self-service gas, while its neighbor, Washington, does not. According to the <u>US Energy Administration</u>, in 2010, Washington had roughly twice the population of Oregon but almost identical gas consumption per capita of four hundred gallons per year. Additionally, Oregon employed roughly 3.5 more people per gas station than did Washington, and there were fewer stations per capita in Oregon. Extrapolating from the difference in employment, economists have estimated that the additional cost from the ban adds roughly five cents to the price of a gallon of gas in Oregon compared to Washington. Given that the number of extra attendants in Oregon appears to be in the vicinity of three thousand and the population of Oregon is about four million, it is likely that the deadweight loss that comes from the higher price of retail gasoline is quite large relative to the societal benefit of the relatively few added employees.

EXPLORING THE POLICY QUESTION

- 1. Do you support the ban on self-service gas? Why or why not?
- 2. Suppose the government mandated that grocery stores must have employees carry customers' groceries to their cars. What effect on prices and employment would you expect?

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

12.1 Input Markets

Learning Objective 12.1: Explain how changes in input markets affect firms' cost of production.

12.2 Labor Supply

Learning Objective 12.2: Describe how individuals make their labor supply decisions and how this can lead to a backward-bending labor supply curve.

12.3 Competitive Labor Markets and Monopsonist Labor Demand

Learning Objective 12.3: Explain how monopsonist labor markets differ from competitive labor markets.

12.4 Minimum Wages and Unions

Learning Objective 12.4: Show the labor market and welfare effects of minimum wages in a comparative statics analysis.

12.5 Policy Example

Should the Government Prohibit Self-Service Gas?

<u>Learning Objective 12.5</u>: Apply a comparative statics analysis to evaluate government prohibitions of self-service gas on labor markets and the market for retail gas.

LEARN: KEY TOPICS

Terms

Final good

Goods that are purchased by the end user, i.e., a pair of jeans; a laptop; a couch.

Intermediate good

A good that is used as an input to produce other goods, i.e., denim in the jeans; harddrive in the laptop; fabric for the couch.

Monopsonist

A single buyer for goods and services, i.e., exclusive contracts of sales of inputs to final goods; seen often in agriculture where large farms sell only to one buyer.

Monopsony

A market in which there exists only one buyer for a good, i.e., The Department of Defense and sophisticated weaponry (there is only one *legal* buyer in this case).

Marginal revenue product of labor (MRP_L)

The value of the marginal product of labor [latex](MP_L)[/latex]—it is the extra revenue a firm receives for an additional unit of labor.

Unemployment

Occurs when there are people who would like to work at a given wage whom are unable to find employment.

Disemployment effect

the amount of employment lost due to the minimum wage. Studies show that the impact of minimum wage laws are quite small—the likely reason is the relative inelaticity of labor supply and demand curves at the bottom edge of the wage scale. See figure 12.12.

Graphs

The market for one-terabyte computer hard drives (1TB HDD)

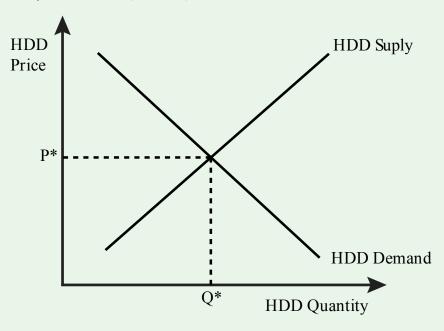


Figure 12.1 The market for one-terabyte computer hard drives (1TB HDD)

The optimal labor-leisure choice problem

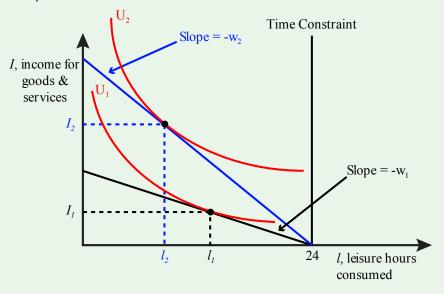


Figure 12.2 The optimal labor–leisure choice problem

An individual's leisure demand curve

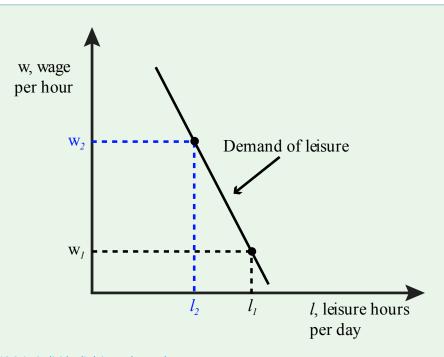


Figure 12.3 An individual's leisure demand curve

An individual's labor supply curve

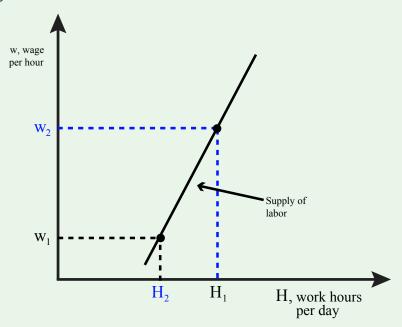


Figure 12.4 An individual's labor supply curve

The backward-bending labor supply curve

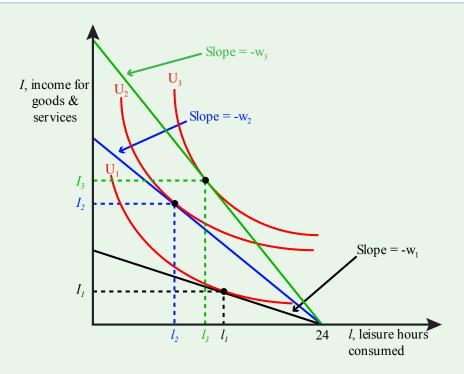


Figure 12.5 The backward-bending labor supply curve: the labor-leisure choice

The labor demand curve and wage and price changes

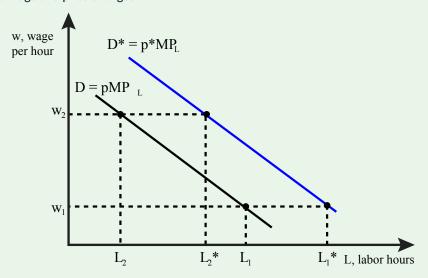


Figure 12.7 The labor demand curve and wage and price changes

The market supply of labor

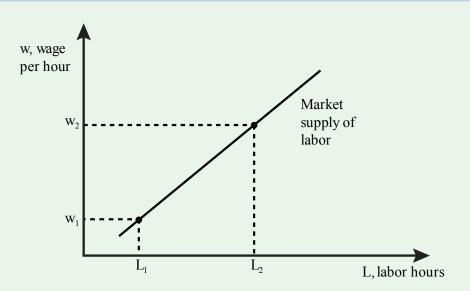


Figure 12.8 The market supply of labor

Labor market equilibrium

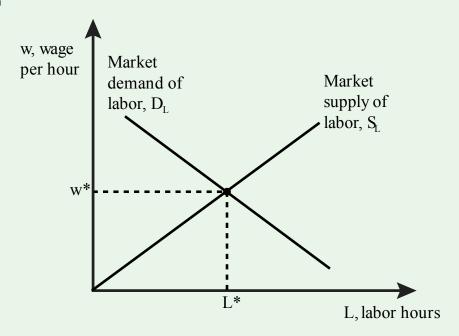


Figure 12.9 Labor market equilibrium

Monopsony and the marginal expenditure curve

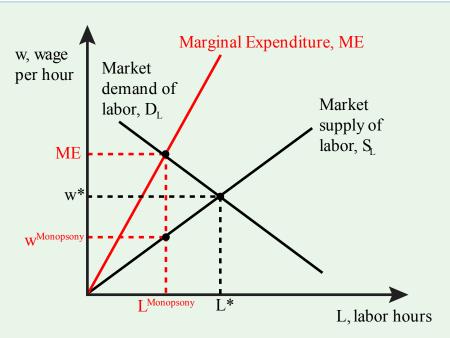


Figure 12.10 Monopsony and the marginal expenditure curve

Minimum wage in a labor market

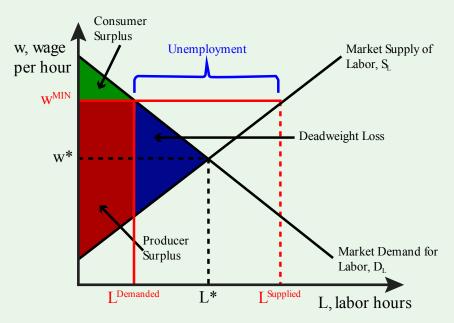


Figure 12.11 Minimum wage in a labor market

Minimum wages with inelastic labor demand and supply

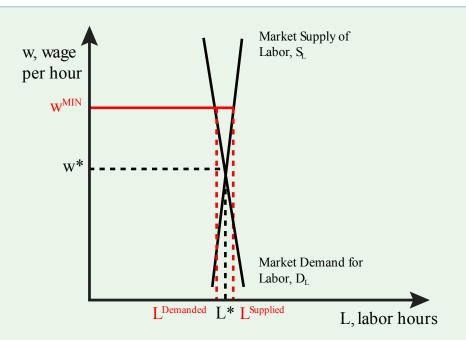


Figure 12.12 Minimum wages with inelastic labor demand and supply

Effect on wages and labor hours due to a ban on self-service gas

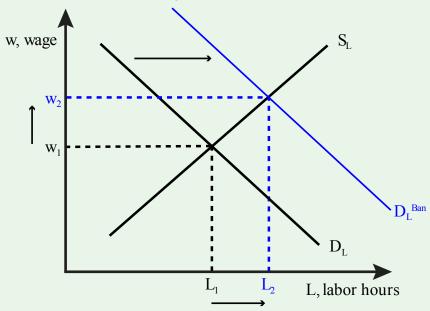


Figure 12.13 Effect on wages and labor hours due to a ban on self-service gas

Effect on retail gas supply due to a ban on self-service gas

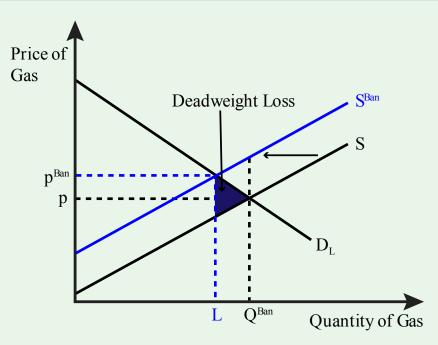


Figure 12.14 Effect on retail gas supply due to a ban on self-service gas

Equation

Marginal revenue product of labor (MRP_L)

$$MRP_L = MR \times MP_L$$

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PERFECT COMPETITION 303

CHAPTER 13

Perfect Competition



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THE POLICY QUESTION

SHOULD THE GOVERNMENT ALLOW OIL COMPANIES TO MERGE RETAIL GAS STATIONS?

In the late 1990s and early 2000s, there were a number of mergers of big oil companies in the United States: Exxon acquired Mobil, BP Amoco acquired ARCO, Chevron acquired Texaco, and Phillips merged with Conoco. This led to massive consolidation in the oil business. In response, US government regulators required the sell-off of some refineries to maintain competitiveness in regional refined gas markets. For the most part, however, the same regulators were unconcerned about the reduction in competition in the retail gas market. In this chapter, we will explore perfectly competitive markets and, in so doing, will be able to better understand why regulators were relatively unconcerned about concentration in the retail gas industry.

EXPLORING THE POLICY QUESTION

- 1. Why were retail gas stations not considered a main concern of regulators?
- 2. Does the merger of major oil companies necessarily lead to higher gas prices? Why or why

not?

LEARNING OBJECTIVES

13.1 Conditions for Perfect Competition

Learning Objective 13.1: Describe the characteristics of a perfectly competitive market.

13.2 Perfect Competition and Efficiency

<u>Learning Objective 13.2</u>: Explain how perfectly competitive markets lead to Pareto-efficient outcomes.

13.3 Policy Example

Should the Government Allow Oil Companies to Merge Retail Gas Stations?

<u>Learning Objective 13.3</u>: Use the perfectly competitive market model to evaluate the decision to allow the consolidation of retail gas stations under fewer brands.

13.1 CONDITIONS FOR PERFECT COMPETITION

Learning Objective 13.1: Describe the characteristics of a perfectly competitive market.

In perfectly competitive markets, firms and consumers are all price takers: their supply and purchasing decisions have no impact on the market price. This means that the market is so big and any one individual seller or buyer is such a small part of the overall market, their individual decisions are inconsequential to the market as a whole. It is worth mentioning here at the start that this is a very strong assumption, and thus this is considered an almost purely theoretical extreme, along with monopolies at the other extreme. We can and will describe markets that come pretty close to the assumptions underlying perfect completion, but most markets will lie somewhere in between purely competitive and monopolistic. It is important to study these extremes to better understand the full range of markets and their outcomes.

Before we describe in detail perfectly competitive markets, let's consider how we categorize market structure, the competitive environments in which firms and consumers interact. There are three main metrics by which we measure a market's structure:

The number of firms.

More firms mean more competition and more places to which consumers can turn to purchase a good.

2. The similarity of goods.

The more similar the goods sold in the market are, the more easily consumers can switch firms, and the more competitive the market is.

3. The barriers to entry.

The more difficult it is to enter a market for a new firm, the less competitive it is.

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The first is relatively straightforward; more firms mean more competition in the sense that it is hard to charge more for a product that consumers can find easily from other sellers. The second is a little subtler because products can be differentiated by something as simple as a brand or more tangible aspects like colors, features, and other characteristics. Finally, the third can be barriers of law like patents or technology, even if not covered by legal patent protection, or more natural barriers like a very high cost of starting up a firm that is not justified by the expected revenue.

We will study four market types in more detail where these metrics will be discussed further, but for now, they are described along the three metrics in **table 13.1**.

Table 13.1 The four basic market structures described

| | The Four Basic Market Structures Described | | | |
|---------------------|--|--------------------------|-----------------------------|-----------|
| Name | Perfect competition | Monopolistic competition | Oligopoly | Monopoly |
| Number of firms | Many | Many | Few | One |
| Similarity of goods | Identical | Differentiated | Identical or differentiated | Unique |
| Barriers to entry | None | None | Some | Many |
| Chapter | <u>13</u> | 20 | <u>19</u> | <u>15</u> |

With this categorization in place, we can turn to the definition of perfect competition. **Perfect competition** is a market with many firms, an identical product, and no barriers to entry. Let's take these three metrics one by one.

Many Firms

Having many firms means that from the perspective of one individual firm, there is no way to raise or lower the market price for a good. This is because the individual firm's output is such a small part of the overall market that it does not make a difference in terms of price. Firms are, therefore, price takers, meaning that their decision is simply how much to sell at the market price. If they try to sell for a higher price, no one will buy from them, and they could sell for a lower price, but if they did so, they would only be hurting themselves because it would not affect their quantity sold. Thus from an individual firm's perspective, they face a horizontal demand curve. We assume they can sell as much as they want but only at the market price. This is an extreme assumption, as mentioned before, but there are some markets that resemble this description. Take the market for corn in the United States. The annual US corn crop is roughly twelve billion bushels, and there are roughly 315,000 corn farms in the country. Thus average output per farm is about thirty-eight thousand bushels annually, or about 0.000003 percent of the total supply of corn in the United States. If one farmer of average corn acreage decided to withhold output, there would not likely be any effect on the market price. It is also true that consumers are price takers as well, meaning no one consumer has a large enough impact to affect prices.

Identical Goods

The existence of identical goods means there is nothing to distinguish one firm's goods from another. To use the corn example, once all the corn is dumped into the grain elevator, there is absolutely no way to tell from which farm a particular kernel of corn came. This means there is no way for one seller to differentiate their output to try to sell it at a different price on the premise that it is different. Contrast this to the automotive market, where the products are heterogeneous. Cars manufactured by Audi are very

different than cars manufactured by Kia. An Audi A6 is very different than a Kia Optima in many substantive ways. Even when there is very little substance that is different, branding can be used to differentiate. Take, for example, polo shirts from Lacoste and Ralph Lauren. The shirt might be almost identical in terms of style, fabric, color, and so on, but by branding them with a logo—a crocodile or polo player—the manufacturers are able to differentiate them in the minds of consumers.

Barriers to Entry

It is very easy for firms to start and stop selling in this market. For example, if a farmer decides to plant corn instead of soybeans, there is nothing preventing them from doing so. Likewise, a farmer who wishes to plant soybeans instead of corn faces no barriers. In general, free entry and exit mean that there are no legal barriers to entry, like needing a special permit only given to a limited number of firms, and no major cost obstacles, like needing to invest millions of dollars in a manufacturing plant, as a new car manufacturer would. This ensures that firms remain price takers even when demand increases. If there is suddenly more demand for corn, perhaps from ethanol producers, farmers can quickly adjust their crops so existing growers do not have an opportunity to raise prices. Free exit is important as well because if firms know they cannot exit easily, they might be reluctant to enter in the first place.

There are two other implicit assumptions worth mentioning here. The first is that we assume that buyers and sellers have full information, meaning that they know the prices charged by every firm. This is important because without it, a firm could possibly charge an uninformed consumer more, and this violates the price-taker condition. The second is that there are negligible transaction costs, meaning it is easy for customers to switch sellers and vice versa. This is also important to ensure price taking, for if transactions costs were high, customers might accept higher prices from existing suppliers to avoid the cost of initiating a new transaction with another supplier at a lower price.

Take a moment and think about the policy example, retail gas, and how well it matches our definition of a perfectly competitive market.

- Are there many sellers?
- Is the product identical?
- Are there barriers to entry?

Your answers to these questions will be the basis of our evaluation of the policy stance the federal government took in assessing the oil company mergers.

In <u>chapter 9</u>, we studied profit maximization for a price-taking firm. We now know in what type of market we find price-taking firms: perfectly competitive markets. In the three other market types we will consider, firms will all have some control over the price of the goods they sell. It is worth taking a moment to review the principles of profit maximization for price-taking firms.

We now know clearly what leads a firm's demand curve to be horizontal and thus the same as the marginal revenue curve: the fact that the firm is in a perfectly competitive market and has no influence on prices.

13.2 PERFECT COMPETITION AND EFFICIENCY

Learning Objective 13.2: Explain how perfectly competitive markets lead to Pareto-efficient outcomes. In <u>chapter 10.4</u>, we studied the concepts of consumer and producer surplus and defined Pareto efficiency. We saw how prices adjust to conditions of excess supply and excess demand until a price that

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equates to supply and demand is reached. What this means is that the market ensures that everyone who values the good more than or equal to the marginal cost of producing it will find a seller willing to sell the good and that all opportunities for consumer and producer surplus will be exploited. This is how we know that total surplus is maximized.

In a perfectly competitive market, neither consumers nor producers have any influence over prices in the market, leaving them free to adjust to supply and demand excesses. Because of this, there is no deadweight loss, total surplus is maximized, and the outcome of the market is Pareto efficient. Prices in competitive markets act as demand and supply signals that are independent of institutional control and ensure that in the end, there are no mutually beneficial trades that do not happen. By mutually beneficial, we mean that buyers and sellers wish to engage in them because they will both be made better off.

It is in this sense that "free" markets are considered efficient. By "free," we mean that prices freely adjust—there are no institutional or competitive controls that prevent prices from adjusting to equilibrate the market until the efficient outcome is achieved. By efficient, we mean Pareto efficient—there is no deadweight loss. With this chapter, we understand the conditions that must hold for a market to achieve the efficient outcome. There must be many buyers and sellers, the good must be homogenous, there must be free entry and exit, and there must be complete information about the good and prices on the part of buyers and no transactions costs. If this sounds like a lot, it is. In later chapters, we will examine the effects of other market structures and when assumptions like complete information fail to hold.

13.3 POLICY EXAMPLE

SHOULD THE GOVERNMENT ALLOW OIL COMPANIES TO MERGE RETAIL GAS STATIONS?

Learning Objective 13.3: Use the perfectly competitive market model to evaluate the decision to allow the consolidation of retail gas stations under fewer brands.

We are now well equipped to address our policy example. What we need to do is evaluate the retail gas market using the description of a perfectly competitive market to try to decide how closely it resembles a perfectly competitive market. We then need to determine if the market looks like a competitive one pre-merger and if that would change significantly after the merger.

Number of Firms

Overall, there are many retail gas stations in the United States—more than 150,000 in 2012. But the United States is too big a geographical area to use for our purposes. For most consumers of retail gas, a reasonable example of a market is the metropolitan area in which they live if they live in urban areas or perhaps a ten-mile radius for rural residents. The number of major branded gas stations was reduced from ten to five with the mergers, but there are also a number of independent or non-name brand gas stations in most retail markets. Post-merger, most communities affected by the merger, those that had stations that represented each of the company brands that merged, still had more than one competing station. But how many competing stations is enough? We will study this question in more detail in chapter 19.

Identical Goods

Retail gas is essentially identical, but major brands do a lot of advertising to try to convince customers that their brand is better. How successful they are at this strategy is beyond our analysis here, but one clue to this is how much more the major branded stations charge over independent stations. However, in this case, the question is how much major brands are able to charge. Casual observation suggests that the answer is not very much. Major branded stations located close to each other almost always charge prices very close to each other, suggesting that though consumers consider their gas higher quality than that of the independent brands, they consider all major branded gas essentially identical.

Free Entry and Exit of Firms

The market for retail gas is fairly open but with some particular aspects. The first is that retail gas requires buried tanks, which often require special permitting. There may also be more zoning restrictions than for other businesses in some areas. But in general, there are few restrictions that prevent new stations to open and existing stations to close.

Retail gas is also one of the most transparent markets in terms of pricing. Most stations prominently display their prices on signs seen easily from the roadway, so the assumption about full information is more apt here than for most retail markets. There are also few transactions costs. There is virtually no cost to purchasing from one station or switching to another. The major gas brands try to create some frictions by establishing loyalty programs or credit card tie-ins that qualify customers for lower prices, but the extent of these programs is clearly limited based on the price matching that most stations do that are located close together.

It appears, then, that the retail gas market is fairly close to a competitive market, if not quite perfect, and that it remains fairly competitive even after the string of mergers. To fully answer the question of whether total surplus is reduced by the merger, we would need to look more closely at real-world price data, but on the face of it, the mergers of retail gas station brands appear relatively benign.

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

13.1 Conditions for Perfect Competition

Learning Objective 13.1: Describe the characteristics of a perfectly competitive market.

13.2 Perfect Competition and Efficiency

Learning Objective 13.2: Explain how perfectly competitive markets lead to Pareto-efficient outcomes.

13.3 Policy Example

Should the Government Allow Oil Companies to Merge Retail Gas Stations?

<u>Learning Objective 13.3</u>: Use the perfectly competitive market model to evaluate the decision to allow the consolidation of retail gas stations under fewer brands.

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LEARN: KEY TOPICS

Terms

Market structure

The competitive environments in which firms and consumers interact.

There are three main metrics by which we measure a market's structure:

1. The **number of firms**.

More firms mean more competition and more places to which consumers can turn to purchase a good.

2. The **similarity of goods**.

The more similar the goods sold in the market are, the more easily consumers can switch firms, and the more competitive the market is.

3. The **barriers to entry**.

The more difficult it is to enter a market for a new firm, the less competitive it is.

Perfect competition

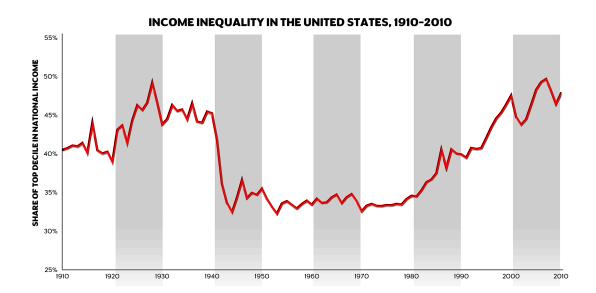
A market with many firms, an identical product, and no barriers to entry.

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CHAPTER 14

General Equilibrium



THE POLICY QUESTION

SHOULD THE GOVERNMENT TRY TO ADDRESS GROWING INEQUALITY THROUGH TAXES AND TRANSFERS?

Rising income inequality in the United States has received a lot of attention in the last few years. As the graph above illustrates, since 1970, there has been a dramatic increase in the concentration of wealth at the top of the income distribution (see <u>chapter 7</u> for a discussion of minimum wages). But a more fundamental policy to address income inequality is a more aggressive tax and transfer policy, where a larger share of the income of the top earners is collected in taxes and then redistributed to low-income earners through tax credits. Critics of this policy worry about the effect such a policy will have on the economy, arguing that it discourages investment and entrepreneurship and is inefficient.

EXPLORING THE POLICY QUESTION

1. Do tax and transfer schemes necessarily lead to inefficiency?

LEARNING OBJECTIVES

14.1 Partial versus General Equilibrium

Learning Objective 14.1: Explain the difference between partial and general equilibrium.

14.2 Trading Economy: Edgeworth Box Analysis

Learning Objective 14.2: Draw an Edgeworth box for a trading economy and show how a competitive equilibrium is Pareto efficient.

14.3 Competitive Equilibrium: Edgeworth Box with Prices

Learning Objective 14.3: Demonstrate how prices adjust to create a competitive equilibrium that is Pareto efficient from any initial allocation of goods.

14.4 Production and General Equilibrium

Learning Objective 14.4: Draw a production possibility frontier and explain how the mix of production is determined in equilibrium and how productive efficiency is guaranteed.

14.5 Policy Example

Should the Government Try to Address Growing Inequality through Taxes and Transfers?

Learning Objective 14.5: Show how any redistribution of resources leads to a Pareto-efficient competitive equilibrium.

14.1 PARTIAL VERSUS GENERAL EQUILIBRIUM

Learning Objective 14.1: Explain the difference between partial and general equilibrium.

In all our previous examinations of markets, we implicitly assumed that changes in other markets do not affect the market we are studying. Though we talked about complements and substitutes and cross-price elasticities, we did not explicitly consider the interaction between markets. What we were doing is called a **partial-equilibrium analysis**: studying the changes in a single market in isolation. This is a useful technique because it allows us to focus on one market and do comparative static analyses without having to try to figure out all the interactions with other markets. The insight gained from this analysis is generally pretty accurate if a market does not have a lot of linkages. For example, the market for biodiesel fuel—a type of diesel fuel produced from waste vegetable oils and animal fat—in the United States is extremely small, and a spike in production costs that increases the price of biodiesel is unlikely to have much of an impact on other markets, even automobiles. Even if a market is likely to have large spillover effects on other markets, those effects could take a while to materialize, so in the short term, partial equilibrium analyses might be reasonably accurate.

However, there are other markets in which the linkages are quite large. Take, for example, the market for crude oil. Crude oil prices affect retail gasoline prices, the market for automobiles, and so on. In order to more accurately analyze these markets, in this chapter, we will relax this assumption and explicitly

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study the interaction among markets. This is called **general-equilibrium analysis**: the study of how equilibrium is obtained in multiple markets at the same time. We will still be working with models—simplified versions of reality—and as such, we will look at several markets simultaneously, but we will not try to model all markets at once. Some economists attempt to model many markets at the same time through the use of computer simulations, but for our purposes, we will concentrate on multimarket analyses where we look only at a few closely related markets.

The linkages between markets are on both the demand side and the supply side. On the demand side, substitutes like cable television and online video streaming services can cause changes in one, like the expansion of videos streaming, to affect the other, like the demand for cable television to fall. Or products can be complements, and an increase in the price of bagels might decrease the demand for cream cheese, for example. On the supply side, markets can have linkages in production choices, like farmers who grow both corn and soybeans. An increase in the price of corn—for example, from the increased production of ethanol—might cause farmers to plant more corn and fewer soybeans, shifting the supply for soy to the left. Or the output of one industry might be an input in another. A reduction in the price of lithium-ion batteries could lead to a reduction in the price of cell phones and electric cars.

Before we move to a full general equilibrium model, let's examine the spillover effects between two related markets: the crude oil market and the market for large sport utility vehicles (SUVs) that are relatively fuel inefficient. When oil prices increase, this leads to higher gasoline prices and reduces the demand for SUVs and vice versa. Let's examine the effect of a significant event in the crude oil market on equilibrium in that market and the market for large SUVs in the United States.

Suppose the oil-producing members of OPEC (Organization of Petroleum Exporting Countries) decided to dramatically cut back on oil production. Such a decision would lead to a large leftward shift of the supply curve, as shown in figure **14.1**, where the supply curve shifts from S_1 to S_2 . This leads to a dramatic price increase from P_1 to P_2 . The price increase in oil leads to a drop in demand for SUVs as automobile consumers switch to smaller, more fuel-efficient cars, as seen in **figure 14.2**, where the demand curve shifts from P_1 to P_2 . The resulting drop in demand lowers the price of SUVs from P_1 to P_2 .

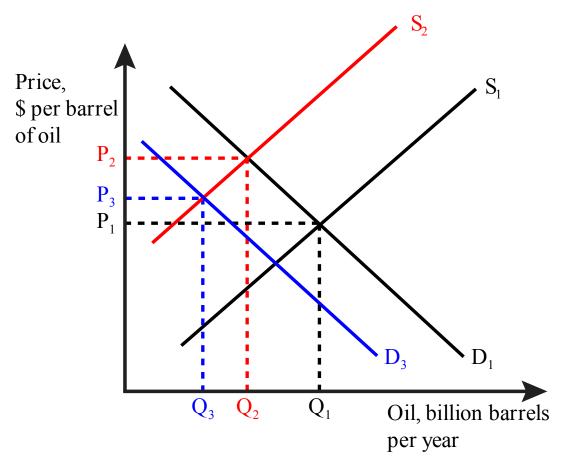


Figure 14.1 General equilibrium in oil markets

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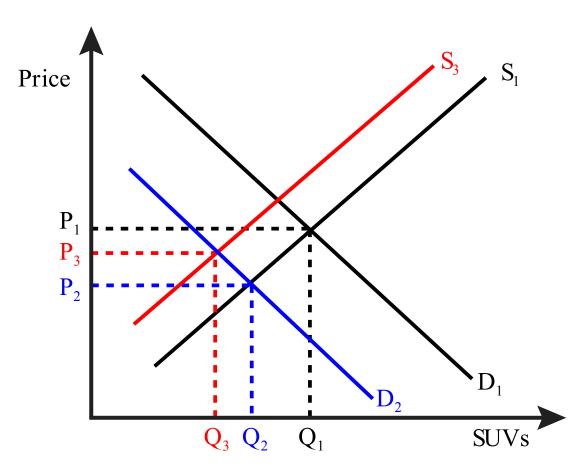


Figure 14.2 General equilibrium in SUV markets

This drop in the price of SUVs will cause automobile manufacturers to shift production away from SUVs and into more fuel-efficient compact cars and electric hybrids. This leads to a shift in SUV supply from S_1 to S_3 in figure **14.2**, and the final price and quantity will be at P_3 and Q_3 . Finally, this shift to more fuel-efficient cars, along with other energy-saving consumption changes, will lower the demand for crude oil, shifting the demand from D_1 to D_3 in panel a and resulting in a final price and quantity that will be at P_3 and Q_3 .

From this example, we can see how markets that are connected influence each other in significant ways. When we ignore these linkages, as we do in partial equilibrium analysis, we can miss significant effects, and our conclusions can be biased.

14.2 TRADING ECONOMY: EDGEWORTH BOX ANALYSIS

Learning Objective 14.2: Draw an Edgeworth box for a trading economy and show how a competitive equilibrium is Pareto efficient.

Though the two-market example introduces the idea of how equilibrium in one market adjusts to changes in another, it is still only a partial analysis. In this section, we will build a simple economy from the most fundamental of starting places—the initial endowment of resources for members of the economy—and we will then show how, through trade in the form of barter, they are able to make themselves better off. In fact, we will show how free trade will lead to a Pareto-efficient outcome: one where it is not possible to make one person better off without hurting another person. In the next section, we will add currency prices and show how prices adjust to achieve equilibrium in the supply and demand of all individuals and show again that the outcome is Pareto efficient.

To construct our trading economy, we need to start with an initial state of the world. To keep matters simple and tractable, our model will assume that there are only two people in this world and two resources. As with all such models in economics, the results are generalizable to many individuals and many goods.

Imagine that two people from the same sea voyage are shipwrecked on two uninhabited tropical islands, separated by a small stretch of water—let's call them Gilligan and Mary Ann. The only things the islands have for them to consume are the bananas and coconuts growing in the trees on both islands. Immediately after the shipwreck, they both take an inventory of the bananas and coconuts available to them. We call this initial allocation of goods their **endowments**. Gilligan finds that he has 60 coconuts and 60 bananas. Mary Ann has 40 coconuts and 90 bananas. The total amount of resources available to both of them is 100 (60+40) coconuts and 150 (60+90) bananas.

As in <u>chapter 1</u>, we can draw a graph for both Gilligan and Mary Ann that shows their initial bundle and their indifference curves through those bundles, as in figure **14.3**.

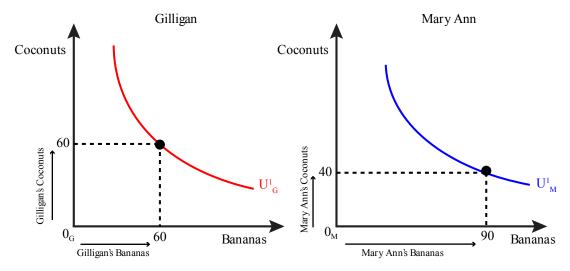


Figure 14.3 Gilligan and Mary Ann's initial endowments and indifference curves

The question for this chapter is, "What happens when Gilligan and Mary Ann discover each other's existence?" More specifically: "Will they trade with each other? Will it improve their well-being?"

To answer these questions, we can begin by implementing a graphical technique called an Edgeworth box (named after the English economist Francis Edgeworth) and shown in **figure 14.4**. The Edgeworth box has dimensions that equal the total resources in the economy. In our case, its height is measured in coconuts, and since there are 100 coconuts total, the height of the box is 100. The width of the box is measured in bananas, and since there are 150 bananas in total, the width is 150. In this way, the dimensions of the Edgeworth box represent the total endowment of the economy. We measure Gilligan's resources from the origin in the southeast corner of the box, labeled \mathcal{O}_G . In contrast, we measure Mary Ann's resources from the northeast corner of the box, labeled \mathcal{O}_M .

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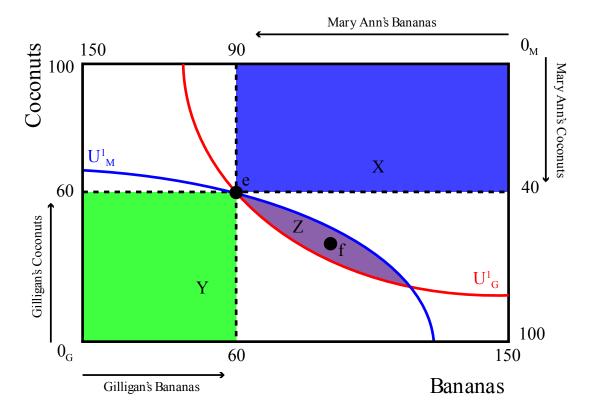


Figure 14.4 The Edgeworth box for Gilligan and Mary Ann's economy

Now each of their initial endowments can be expressed by a single point, marked e. Note that at his point, Gilligan has sixty coconuts. Since there are one hundred coconuts in total, that leaves exactly forty for Mary Ann. This is the distance from Gilligan's sixty to the top of the box. We measure Mary Ann's endowment of coconuts from the top of the box down to her endowment point, e. Her having forty coconuts leaves sixty for Gilligan. The same is true for bananas: we measure Gilligan's from left to right starting at 0_G , and we measure Mary Ann's bananas from right to left starting at 0_M . In fact, any spot in the Edgeworth box represents a full distribution of all the combined resources—this is the clever trick of the Edgeworth box. It also means that nothing is wasted; there are no leftover resources available at any spot in the box.

As in <u>figure 14.3</u>, we can draw indifference curves through the initial endowment point for both people. Gilligan's is identical to the one in <u>figure 14.3</u>. Mary Ann's indifference curve is identical as well in relation to the new origin for her, 0_M .

The trick to understanding the Edgeworth box is to imagine taking Mary Ann's graph from <u>figure 14.1</u> and rotating it 180 degrees and then sliding it over until the endowment points for both are on the same spot. This is illustrated in **figure 14.5**.

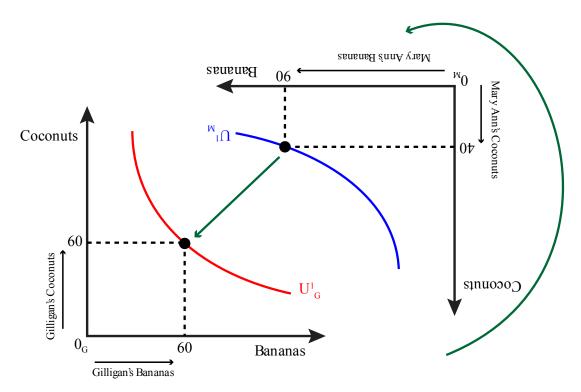


Figure 14.5 Creating the Edgeworth box from two individual initial endowments and indifference curves

In the Edgeworth box in figure 14.4, better consumption bundles for Gilligan are to the northeast of his initial indifference curve, U_G^1 , or in the areas labeled X and Z; this is called the preferred set for Gilligan. Better bundles for Mary Ann are now to the southwest of her initial indifference curve, U_M^1 , in the areas labeled Y and Z; this is the preferred set for Mary Ann. Note that area Z is the one area that is the preferred set for both Gilligan and Mary Ann. This area Z is called the lens.

Now we have to ask the next question: "When Gilligan and Mary Ann become aware of each other and make contact, should they trade?"

Assuming nothing compels them to trade, they will only engage in trade if they can be made better off because otherwise, they will just keep their initial endowment. Assuming that Gilligan and Mary Ann are utility maximizers, as usual, we have already identified a set of alternate distributions of resources that make both better off: the feasible bundles in the lens. They are feasible because they represent a complete distribution of the available resources, as does any spot in the Edgeworth box. They make both people better off because they cause both to achieve a higher indifference curve and therefore a higher utility. The movement from allocation e to allocation f is shown in **figure 14.6**. Note that at f, both Gilligan and Mary Ann are on higher indifference curves: Gilligan moves from U_G^1 to U_G^2 , and Mary Ann moves from U_M^1 to U_M^2 . As long as there is a lens, there is a mutually beneficial trade to be made, so only where the two indifference curves just touch each other or are tangent to each other does the lens disappear. One such point is point f.

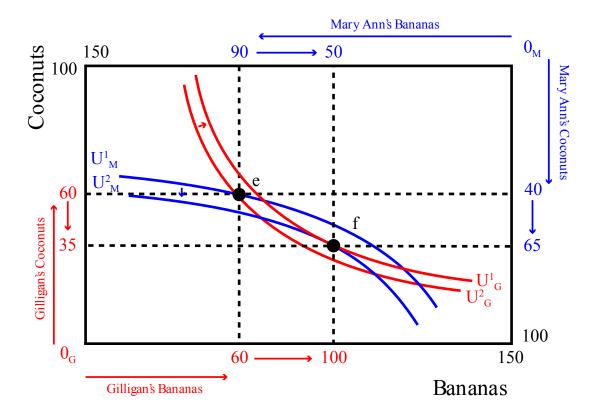


Figure 14.6 Mutually beneficial trade to a Pareto-efficient allocation

Point f isn't just better for both; it is also Pareto efficient: there is no way to reallocate resources from that point without making one of the people worse off (on a lower indifference curve). So what is the trade that gets Gilligan and Mary Ann from e to f? Gilligan trades twenty-five coconuts to Mary Ann in exchange for forty bananas. Gilligan goes from having sixty bananas to having one hundred and from sixty coconuts to thirty-five. Mary Ann goes from having ninety bananas to having fifty and from forty coconuts to sixty-five.

Why is point f both efficient and optimal? We know it is the point at which both Gilligan's and Mary Ann's indifference curves are tangent. This means that the marginal rates of substitution (MRS) of both are equal at f. Recall that the MRS of an agent is the rate at which they would trade one good for the other and be just as well off. When they are equal, there is no more incentive to trade. For example, if both parties are willing to trade one coconut for one banana, neither would be made better off trading.

Note: at the optimal bundle, $MRS_G = MRS_M$.

On the other hand, if Gilligan could trade two coconuts for one banana and be just as well off (his MRS is 2) and Mary Ann could trade one coconut for two bananas and be just as well off (her MRS is ½), then if Gilligan traded one of his coconuts for one banana from Mary Ann, it will make Gilligan better off (he only had to give up one coconut when he could give up two and be as well off) and Mary Ann better off (she only had to give up one banana when she could give up two and be as well off). This is similar to the situation at point e where Gilligan's MRS is greater than Mary Ann's e0, so Gilligan trades coconuts for bananas.

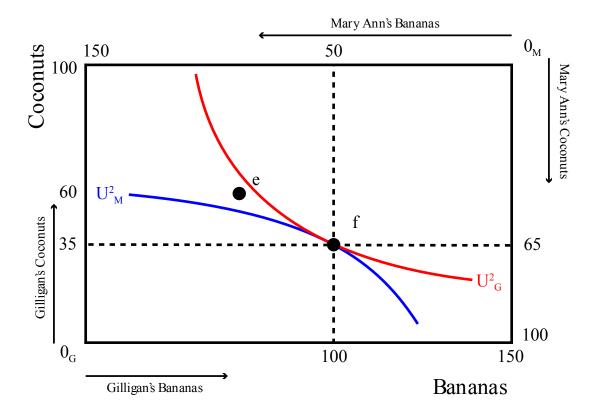


Figure 14.7 Tangent indifference curves, equal [latex]MRS[/latex]s, and the Pareto efficient allocation

But point f is not the only efficient allocation possible. In fact, there are an infinite number of efficient allocations, as the space is filled with an infinite number of indifference curves for both Gilligan and Mary Ann, and therefore, for each indifference curve for one person, there is a point of tangency with an indifference curve of the other. The contract curve is the line that connects all these points of Pareto efficiency. Note that the **contract curve** begins and ends at the corners that represent the complete absence of goods for Gilligan, 0_G , and Mary Ann, 0_M . This is a Pareto-efficient allocation as well because if Gilligan has nothing and Mary Ann has all the coconuts and bananas, it is not possible to give Gilligan some without taking away from Mary Ann and making her worse off. The same logic applies at 0_M .

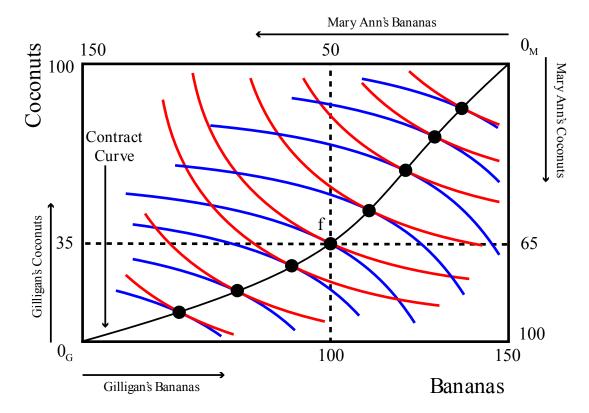


Figure 14.8 The contract curve

We know that there will always be an incentive to trade as long as the marginal rates of substitution are not equal and that from the initial allocation e, they will trade to some point within the lens. We also know that f is a Pareto-efficient allocation within the lens and is one such point. But the contract curve shows us that there are many Pareto-efficient allocations in the lens. The portion of the contract curve that lies within the lens is the ${\bf core}$ and is shown in **figure 14.9**.

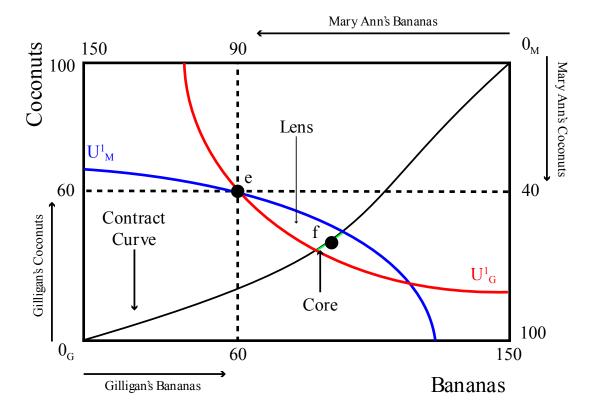


Figure 14.9 The contract curve, the lens, and the core

Mathematical Extension

We have described two conditions that define Pareto-efficient allocations. First, they are feasible. We have ensured feasibility with our graphical technique of the Edgeworth box—all allocations within the box are feasible.

Mathematically, a feasible allocation is one that meets the two following conditions:

$$b^G + B^M = B$$

where B is the total amount of bananas, b^G is Gilligan's share of bananas, and b^M is Mary Ann's share of bananas.

$$c^G + c^M = C$$

where C is the total amount of coconuts, c^G is Gilligan's share of bananas, and c^M is Mary Ann's share of coconuts.

Second, at Pareto-efficient allocations, the marginal rates of substitution are equal.

Mathematically, the marginal rate of substitution [latex](MRS)[/latex] is

So while we cannot predict precisely which allocation Gilligan and Mary Ann will end up on once they discover each other and decide to trade, we know that it will be somewhere on the core.

Note that through barter, the individuals reach a Pareto-efficient outcome, but this outcome depends critically on the initial allocation. The initial allocation determines the lens or the range of possible outcomes given the initial allocation. Our policy example asks about tax and transfer schemes that address inequality. From this analysis, it is clear that an unequal initial allocation will lead to outcomes that are also relatively unequal. So there is nothing within the barter economy that addresses or acts as a corrective for inequality.

The barter economy is a great introduction to general equilibrium and provides critical insight into how voluntary trade makes both parties better off and

leads to Pareto-efficient outcomes. However, in the real world, most transactions happen not by barter but through the use of money. In the next chapter, we will expand our model to a competitive equilibrium setting with the use of money and where there are prices and consumers are price takers.

14.3 COMPETITIVE EQUILIBRIUM: EDGEWORTH BOX WITH PRICES

Learning Objective 14.3: Demonstrate how prices adjust to create a competitive equilibrium that is Pareto efficient from any initial allocation of goods.

Much of the trade in the real world occurs in markets that use some sort of currency as the medium of exchange and where the prices are posted. Take, for example, a supermarket where food and other goods are displayed on shelves with prices listed. There is no bargaining; you either buy or don't buy a good at the price shown. To make our simple model more realistic, we need to add a market and prices. The idea that two people stranded on tropical islands would consider themselves to be price takers might seem a little odd, but we will maintain this assumption to keep the analysis simple. In reality, we are applying this model to situations where there are many buyers and sellers—for example, think of a large farmers' market where there are many different sellers of the same produce and many buyers as well.

So now, instead of exchanging bananas for coconuts, Gilligan and Mary Ann exchange them for dollars. For example, if Mary Ann wants more coconuts, she has to sell some bananas to earn money and then use the money earned to buy coconuts. With only two goods, it is the relative price that matters because it is the relative price that deter-

$$MRS^G = -rac{MUrac{G}{B}}{MUrac{G}{C}} = -rac{rac{\partial U^G}{\partial b^G}}{rac{\partial U^M}{\partial C^M}} ext{ (for Gilligan)}$$
 $MRS^M = -rac{MUrac{M}{B}}{MUrac{M}{C}} = -rac{rac{\partial U^M}{\partial b^M}}{rac{\partial U^M}{\partial c^M}} ext{ (for Mary Ann)}$

Let's consider a specific example. We have the total bananas (150) and coconuts (100) in the economy.

Let
$$U^G - ln(B) + 2ln(c)$$
 and $U^G = ln(B) + 2ln(c)$ and $\frac{\partial U^G}{\partial b^M} = \frac{1}{b^G}$ and $\frac{\partial U^G}{\partial c^G} = \frac{2}{c^G}$, so $\frac{\frac{\partial U^G}{\partial b^G}}{\frac{\partial U^G}{\partial c^G}} = \frac{c^G}{2b^G}$ and $\frac{\partial U^M}{\partial b^M} = \frac{1}{b^M}$ and $\frac{\partial U^M}{\partial C^M} = \frac{2}{c^M}$, so $\frac{\frac{\partial u^M}{\partial b^M}}{\frac{\partial U^M}{\partial c^M}}$

So the condition
$$MRS^G=MRS^M$$
 is equivalent to
$$\frac{\frac{\partial U^G}{\partial b^G}}{\frac{\partial U^G}{\partial c^G}}=\frac{\frac{\partial U^M}{\partial b^M}}{\frac{\partial U^M}{\partial c^M}}.$$
 $MRS^G=MRS^M$ is equivalent to
$$(14.1)\frac{c^G}{2b^G}=\frac{c^M}{2b^M}\ or\ \frac{c^G}{b^G}=\frac{c^M}{b^M}$$
 Now let's return to our feasibility constraints: $b^G+b^M=B$ and $c^G+c^M=C$. Given our resources, these become the following:
$$(14.2)\ b^G+b^M=150$$
 or: $b^M=150-b^G$ or: $c^G+c^M=100$ (14.3) $c^M=100-c^G$

Substituting equations (14.2) and (14.3) into (14.1) yields the following expression of the tangency condition:

$$c^G=rac{2}{3}b^G$$

This is the equation of the contract curve. In this simplified example, the contract curve is just the diagonal of the rectangular Edgeworth box.

mines the rate of exchange. For example, if the price of bananas is \$1 and the price of coconuts is \$2, then the rate of exchange of bananas to coconuts is \$1/\$2, or ½. It takes two bananas to get one coconut. This is true if the price of bananas was \$100 and the price of coconuts was \$200 instead—it would still take two bananas to get one coconut.

To start, let's consider the price of bananas to be \$1 and the price of coconuts to be \$2. At the initial distribution of goods, the bounty of Gilligan's island is worth \$180 (\$1 per banana × 60 bananas + \$2 per coconut × 60 coconuts), and the resources on Mary Ann's island are worth \$170 ($\$1 \times 90 + \2×40).

Now suppose Gilligan would like to trade: he knows, because of the prices, that he can trade at a rate of two bananas for one coconut. He could, for example, sell all his bananas for \$60 and then buy 30 coconuts with the money earned. This would leave him with 0 bananas and 90 coconuts. Alternatively, he can sell 45 coconuts to buy 90 bananas and could then have all 150 bananas on the two islands, which would leave him with 15 coconuts. He could also end up with any other bundle that represents a two-forone trade of bananas and coconuts. This set of available bundles at these prices is illustrated in **figure 14.10** and called the **price line**.

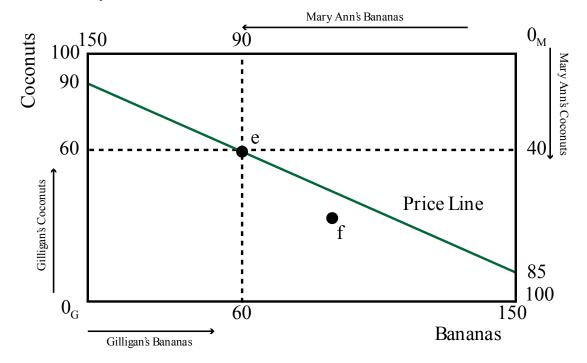


Figure 14.10 The initial endowment and the price line

Mary Ann has equivalent choices; she can sell 90 bananas to earn \$90 and then spend that money on 45 coconuts, leaving her with 0 bananas and 85 coconuts. Or she could sell 30 coconuts and buy 60 bananas, leaving her with all 150 of the bananas on the two islands and 10 coconuts. Therefore, the price line represents all the points in the Edgeworth box at which Gilligan and Mary Ann could end up, given the initial distribution of resources and the prices.

These prices do not allow Gilligan and Mary Ann to get to a Pareto-efficient outcome, however. Each of them maximizing their utility leads to two optimal bundles that are not feasible: together, they want too many bananas (more than the two islands have) and too few coconuts. This situation is shown in **figure 14.11**.

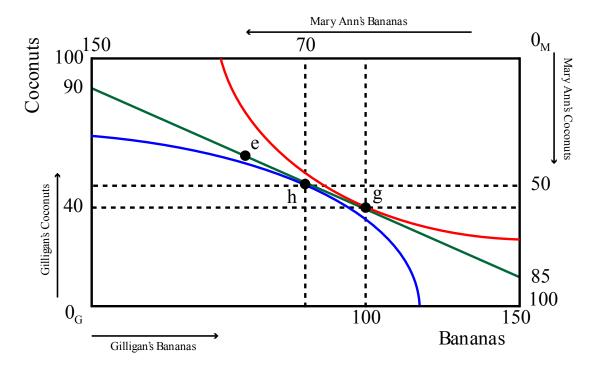


Figure 14.11 No equilibrium in the product markets

As we can see in **figure 14.11**, Gilligan's optimal consumption bundle is at point g, where his indifference curve is tangent to the price line, and Mary Ann's optimal consumption bundle is at point h, where her indifference curve is tangent to the price line. At these bundles, Gilligan would like to consume 100 bananas and 40 coconuts, and Mary Ann would like to consume 70 bananas and 50 coconuts. The total demand for bananas, 170, is greater than the total amount available, 150, and the total demand for coconuts, 90, is less than the total amount available, 100. Thus there is excess demand for bananas and excess supply of coconuts.

We know from previous chapters that excess demand causes prices to rise and excess supply causes the process to fall, so banana prices should rise, coconut prices should fall, and therefore, the relative price of bananas to coconuts should rise.

What is equilibrium in this market? Equilibrium is a set of prices, or a price ratio, where the number of bananas demanded by both Gilligan and Mary Ann exactly equals the total number available *and* the number of coconuts demanded by both Gilligan and Mary Ann exactly equals the total number available.

In our case, the price ratio
$$rac{P_B}{P_C}=rac{1.25}{2}$$
 does exactly that.

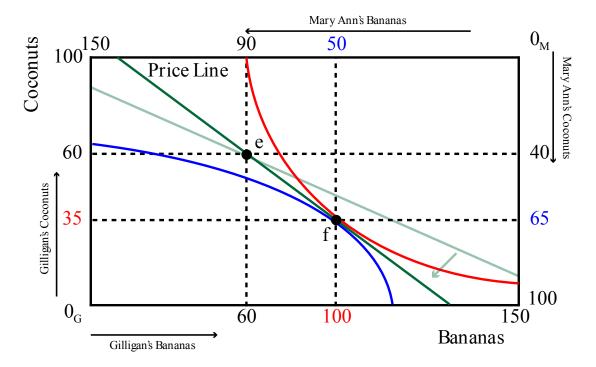


Figure 14.12 Competitive equilibrium in the island economy

As can be seen in **figure 14.12**, at the price ratio of \$1.25/\$2, Gilligan wants to sell twenty-five coconuts at \$2 a coconut, and with the \$50 he earns from that sale, he will buy forty bananas at \$1.25 a banana. At the same time, Mary Ann wants to sell forty bananas at \$1.25 a banana, and with the \$50 she earns, she wants to buy twenty-five coconuts. Equilibrium is achieved because the number of bananas Gilligan wants to buy is exactly equal to the number of bananas Mary Ann wants to sell and the number of coconuts Gilligan wants to buy is exactly equal to the number of coconuts Mary Ann wants to sell. Since this is the case, the condition that characterizes the equilibrium point is

$$MRS_G = -rac{\dot{P_B}}{P_C} = MRS_M.$$

In other words, both indifference curves and the price line all have the same slope at the optimal point, point f. This guarantees that the competitive equilibrium lies on the contract curve, which guarantees that it is Pareto efficient. We call this result the first theorem of welfare economics.

First Theorem of Welfare Economics

Any competitive equilibrium is Pareto efficient

Mathematical Extension

We have described two conditions that define Pareto-efficient allocations in an exchange economy in the previous section: (1) they have to be feasible, and (2) the marginal rates of substitution need to be equal.

With a market economy, we now have to incorporate the price system into our analysis. What we know is that the price line connects the initial allocation

There is a second theorem that is closely related to the first. It concerns the ability of a social planner to select a particular equilibrium point along the contract curve. Is it possible to reallocate resources to achieve equilibrium at a desired point? The answer is yes.

Second Theorem of Welfare

Economics

Any Pareto-efficient competitive equilibrium is achievable through the reallocation of resources

One implication of the second theorem is that society can address inequality through transfers of resources without any efficiency loss. Any efficient allocation on the contract curve can be achieved through a redistribution of the initial endowment. Note that this does not have to be on the contract curve; it is any initial endowment that lies on the equilibrium price line connecting the point on the contract curve.

14.4 PRODUCTION AND GENERAL EQUILIBRIUM

Learning Objective 14.4: Draw a production possibility frontier and explain how the mix of production is determined in equilibrium and how productive efficiency is guaranteed.

In the example of desert-island economies above, we have ignored production—the bananas and coconut were simply there, endowed to the inhabitant of the island. Now we are going to add the final piece of complexity by adding production. Instead of a pile of coconuts and bananas available to the inhabitants, the inhabitants must produce them through the use of their labor to harvest them from trees on the islands. We will assume that both banana trees and coconut trees grow on both islands but that Gilligan and Mary Ann differ in how many coconuts and bananas they can harvest in a day.

Banana trees are not tall, and their fruit is easy to reach without climbing, while coconut trees are very tall and require a lot of climbing to reach their fruit. It turns out that while they are both and the equilibrium point: this means that the equilibrium has to be affordable, and affordability is determined by the initial allocation and the prices themselves.

Let the initial allocation of bananas be given by $b^G+b^M=B'$ where B is the total amount of bananas, b^G is Gilligan's share of bananas, and b^M is Mary Ann's share of bananas. The initial allocation of coconuts is given by $c^G+c^M=C$, where C is the total amount of coconuts, c^G is Gilligan's share of bananas, and c^M is Mary Ann's share of coconuts. In terms of initial wealth, Gilligan has

$$P_b b^G + p_c c^G$$

This is how much Gilligan can earn from selling his endowment. Similarly, MaryAnn has

$$P_b b^M + P_c c^M$$

Any potential equilibrium has to be affordable; these affordability constraints are

$$P_b b^G + P_C c^G {=} p_b reve{b}^G + p_c reve{c}^{G_{ ext{(Gilligan)}}} \ P_b b^M + P_c C^M {=} P_b \hat{b}^M + p_c \hat{c}^{M_{ ext{(Mary Ann)}}}$$

where the hats on top of the $m{b}$ and the $m{c}$ represent equilibrium amounts. These constraints state that the total amount of money spent on the equilibrium allocations has to equal the amount earned from selling the initial allocation.

These constraints, along with the equality of the marginal rates of substitution and the price ratio, characterize the competitive equilibrium:

$$rac{rac{\partial U^G}{\partial b^G}}{rac{\partial U^G}{\partial c^G}} = rac{rac{\partial U^M}{\partial b^M}}{rac{\partial U^M}{\partial c^M}} = rac{Pb}{Pc}$$

Note, however, that the nominal prices don't matter at all; only relative prices matter, since the nominal values do not affect the ability to exchange allocated goods for new goods. So we can set one price p_c , to \$1.

Let's consider the same example from the previous section. We have the total bananas (150)

$$(100)$$
 in the economy. Letting $U^G = ln(B) + 2ln(c)$ and $U^G = ln(B) + 2ln(c)$, we found that

$$MRS^G = MRS^M = P_b$$

is equivalent to

$$rac{c^G}{2b^G}{=}rac{c^M}{2b^M}{=}Pb$$
 or $rac{c^G}{b^G}{=}P_B$

And the contract curve is given as

$$c^G = rac{2}{3} b^G \cdot c^G = rac{2}{3} b^G \cdot \operatorname{or} rac{c^G}{b^G} = rac{2}{3} \cdot rac{2}{3} \cdot$$

Thus

$$\hat{P}b = \frac{2}{3}$$

The demand functions for these Cobb-Douglas preferences are

$$\hat{b}^G = rac{50p_b + 50}{P_b}, and \ \hat{c}^G = rac{rac{1}{2}(50p_b + 50)}{1}.$$

 ${\hat b}^G=125$

Thus the equilibrium quantities and prices are the following:

$$egin{aligned} \hat{c}^G &= 42\ \hat{c}^M &= 25\ \hat{c}^M &= 58\ \hat{p}_b &= rac{2}{3}\ \hat{p}_c &= 1 \end{aligned}$$

more than capable of harvesting both fruits, Gilligan is more adept at finding and harvesting bananas, while Mary Ann is relatively better at climbing trees and harvesting coconuts.

If Gilligan spends his entire day collecting coconuts, he can collect one hundred; if he spends his entire day collecting bananas, he can collect two hundred. He can also split his time between the two activities. If we call etathe fraction of the time he spends on banana harvesting, then 1-eta is the time he spends on coconut harvesting. So in one day, Gilligan will harvest two hundred β bananas plus one hundred (1-eta) coconuts. By varying eta from zero to one, we can find all the points in Gilligan's production possibility frontier (PPF): a line that shows all the possible combinations of bananas and coconuts Gilligan can harvest in a single day. This is shown in **figure 14.13**.

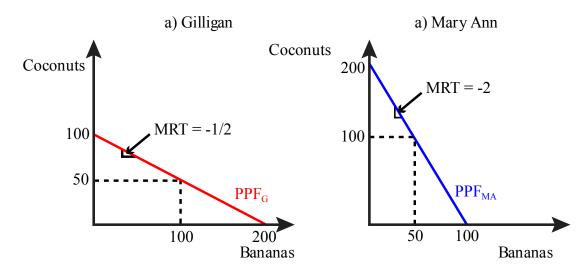


Figure 14.13 Individual production possibility frontiers

Similarly, if Mary Ann spends her entire day collecting coconuts, she can collect two hundred; if she spends her entire day collecting bananas, she can collect one hundred. She can also split her time between the two activities. If we call β the fraction of the time she spends on banana harvesting, then $1-\beta$ is the time she spends on coconut harvesting. So in one day, Mary Ann will harvest one hundred β bananas plus two hundred $(1-\beta)$ coconuts. By varying β from zero to one, we can find all the points in Mary Ann's production possibility frontier. This is shown in figure **14.13**.

Marginal Rate of Transformation

The slope of the PPF is the marginal rate of transformation (MRT): the cost of production of one good in terms of the foregone production of another good. This is the opportunity cost of producing that good. In this case, the MRT is the number of coconuts that can be collected if the collection of bananas is reduced by one banana. For Gilligan, every banana he chooses not to collect leads to enough time to collect $\frac{1}{2}$ more coconuts, or put in another way, for every 2 bananas he gives up, he can collect 1 more coconut. Thus his MRT is $-\frac{1}{2}$, which is the same as the slope of his PPF. Similarly, for Mary Ann, if she reduces her banana collecting by one banana, she can collect 2 coconuts. So her MRT is -2, which is the same as the slope of her PPF.

Comparative Advantage

This leads directly to the concept of **comparative advantage**: a person has a comparative advantage in the production of a good if they have a lower opportunity cost of production than someone else. In our case, Gilligan has a lower opportunity cost of producing (collecting) bananas, as he gives up only ½ coconut per banana. It must be the case in this two-good world that Mary Ann has a comparative advantage in collecting coconuts, as she gives up only ½ a banana to collect a coconut (while Gilligan would have to give up 2). As the name suggests, this is a comparative concept; it is only relative to someone else. And it does not have anything to do with absolute productivity. To see this, suppose that Mary Ann could collect 1,000 bananas and 2,000 coconuts in a day. She would still have the same MRT, -2, and thus the same opportunity cost of bananas.

If they combined their outputs, they would have a joint PPF, as shown in **figure 14.14**.

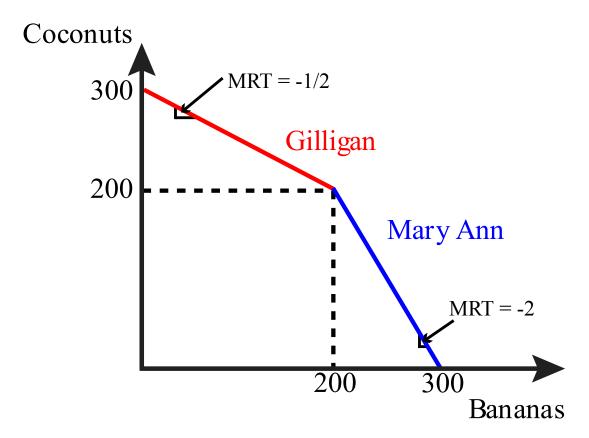


Figure 14.14 Joint production

By producing based on their comparative advantage and trading, both Gilligan and Mary Ann can be made better off. To see this, imagine that both Gilligan and Mary Ann do not trade and spend half their time on each collecting activity. From **figure 14.13**, we can see that Gilligan collects one hundred bananas and fifty coconuts, while Mary Ann collects fifty bananas and one hundred coconuts. Now suppose that each spends all their time collecting the good in which they have a comparative advantage. Gilligan will collect only bananas and harvest two hundred, and Mary Ann will collect only coconuts and harvest two hundred. By sharing half their harvest with each other, they will end up with one hundred of each, or fifty more in total. This is the lesson of trade based on comparative advantage: all parties can benefit.

As we add producers, this adds segments to the PPF. For example, suppose another person, whom we will call Thurston, arrives on the islands, and his ability to collect bananas is 150 per day if he spends all his time collecting bananas and 150 coconuts if he spends his entire day collecting coconuts. Thurston's PPF is shown in **figure 14.15**.

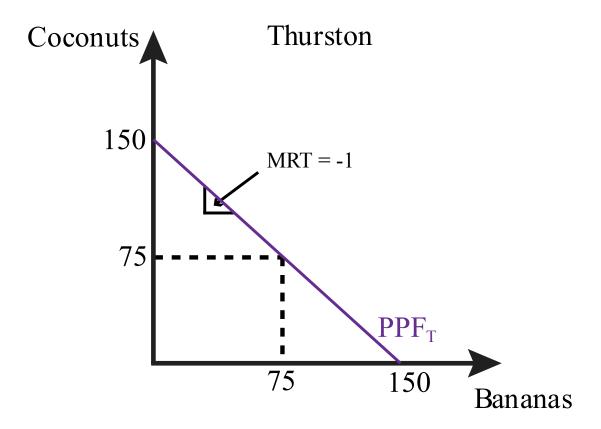


Figure 14.15 Thurston's production possibility frontier

Thurston's MRT is -1, and if he spends half his day collecting bananas and half his day collecting coconuts, he will collect 75 of each.

When we add Thurston's PPF to the group, or the joint production PPF, we have to think about the most effective way for the group to collect both bananas and coconuts. Starting from a position of all three spending their entire time collecting coconuts and thus collecting 450 coconuts and no bananas, we need to ask, "Who is the best person to start collecting bananas if they want to add bananas to their collection?"

The answer, based on having the lowest opportunity cost, is Gilligan. But Gilligan can only collect 200 bananas if he devotes his entire day to the endeavor. What if the group wants to collect even more? The next best person is Thurston, whose opportunity cost of collecting bananas is 1, which is lower than Mary Ann's, which is 2. Thus the second segment in the joint PPF is, therefore, Thurston's PPF, followed by Mary Ann's, as is shown in **figure 14.16**.

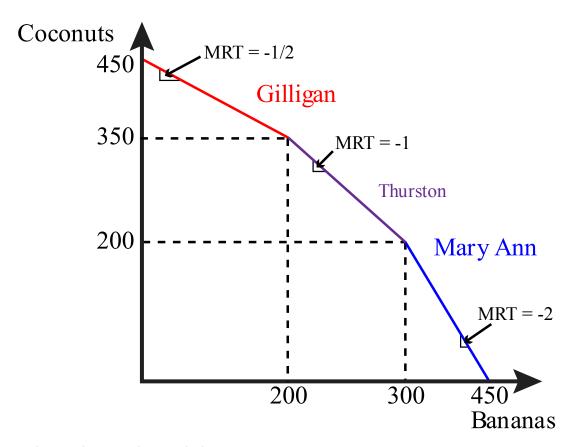


Figure 14.16 The joint [latex]PPF[/latex] with Thurston

As we add more and more producers to this economy, two things will happen. One, we will add their production to the joint PPF, which will shift the PPF out as more goods are being produced overall. Two, we will add more and more segments of the joint PPF, each with its own slope, and the joint PPF will become more and more smooth—the kinks in the curve will become less and less evident until eventually it will appear as a smooth curve, as shown in green in **figure 14.17**.

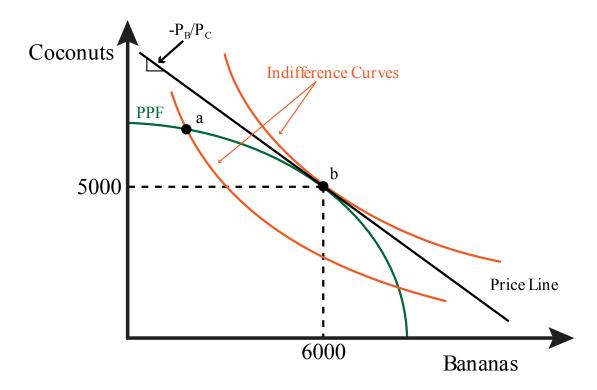


Figure 14.17 The optimal product combination

The concave shape of the PPF leads to an MRT that is constantly changing. The slope becomes increasingly steeper as we move down the PPF, and therefore, the MRT increases in absolute value. The more bananas they produce, the more coconuts they have to give up per banana. The MRT tells us the marginal cost of producing one extra banana in terms of the marginal cost of producing another good; in this case, the MRT is the ratio of the marginal cost of bananas and the marginal cost of coconuts:

(14.4)
$$MRT = -rac{MC_B}{MC_C}$$

Every point on the PPF is efficient; there are no wasted resources—production is at its maximum and feasible. Now we want to know, among all of the possible points, what is the optimal mix of bananas and coconuts?

To answer this, we need to know about the preferences of the consumers of the two goods. To keep things simple, assume that we can represent the preferences of every consumer in this economy with a single indifference curve, perhaps because every consumer has identical preferences. The optimal decision then is the point on the PPF that allows the consumers to achieve the highest indifference curve possible. In **figure 14.17**, point b is on the PPF but leads to an indifference curve that is below the one that includes point a. Point a is the one point that allows the consumers the most utility from the product mix. It is also the one that is just tangent to the PPF at point a. This means that we have a familiar condition that characterizes the optimal mix of goods: MRS = MRT.

We know from chapter 4 that utility maximizing consumers choose a bundle of a good for which their marginal rate of substitution equals the slope of the budget line—the negative of the price ratio. If all consumers face the same price ratio, they will all pick a consumption bundle where they all have the same MRS. This is true even if their preferences differ because prices are common to all consumers, and a condition of the optimal consumption bundle is that MRS equals the negative of relative prices. Because all consumers have the same MRS, no trades will happen; there are no mutually beneficial

trades to be had. This is called **consumption efficiency**: it is not possible to redistribute goods to make one person better off without making another person worse off. This also indicates that the consumption bundle lies on the contract curve.

Suppose that rather than being traded, bananas and coconuts are sold by competitive firms. In a perfectly competitive environment, each firm sells a quantity of each good so that their marginal cost of production equals the price:

$$P_B = MC_B \, and \, P_C = MC_c$$

We divide one equation by the other to get

(14.5)
$$rac{P_B}{P_C}=rac{MC_B}{MC_C}.$$

From <u>14.1</u>, we know that $MRT = -rac{MC_B}{MC_C}$, so

(14.6)
$$MRT=-rac{P_B}{P_C}$$

This has an intuitive explanation. Consider an MRT of -1; what this means is that they can trade off production one for one. They can produce one more banana by producing one less coconut. Now suppose that the price of bananas is \$2 and the price of coconuts is \$1, so the price ratio is -2. Should the firm adjust output? Yes. By producing one more banana, they earn \$2 more; they have to produce one less coconut to do so, but they only forgo \$1 in earnings, so their net gain is \$1. Only where

$$MRT = -rac{P_B}{P_C}$$

do these potential gains disappear. Since we know the optimal consumption bundle is where MRS equals the negative of the price ratio, we know

(14.7)
$$MRS=-rac{P_B}{P_C}=MRT$$

Equation (14.7) is illustrated in <u>figure 14.17</u>—the PPF, the price line, and the indifference curves all have the same slope at point a. Competition ensures that MRT equals MRS, and this means that the economy has achieved **productive efficiency**: there is no other mix of output levels that will increase the firm's earnings.

We can combine the PPF and the Edgeworth box in the same graph by noting that each point on the PPF defines the dimensions of an Edgeworth box. In **figure 14.18**, firms produce 150 bananas and 100 coconuts, point a on the PPF. This is the dimension of the Edgeworth box drawn inside of the PPF.

The prices that consumers pay are the same as the prices producers receive, $-\frac{P_B}{P_C}$, so the price line in the Edgeworth box has the same slope as the price line that touches the PPF.

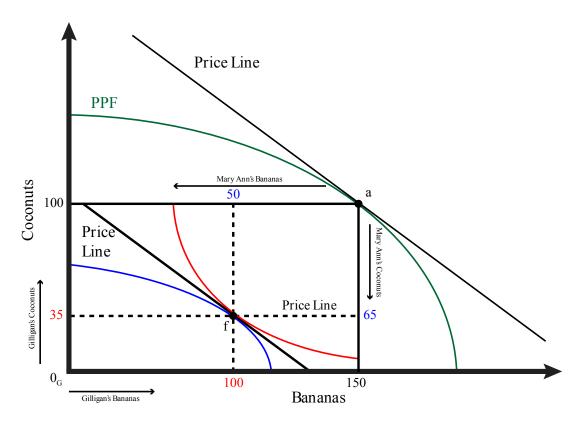


Figure 14.18 Competitive equilibrium

In equilibrium, the price line is tangent to the consumers' indifference curves at point f as well as to the PPF at point a. Thus a competitive equilibrium is reached. Consumers are maximizing their utilities at point f, producers are maximizing their returns at point a, and supply equals demand in both markets: Gilligan consumes 100 bananas and 35 coconuts; Mary Ann consumes 50 bananas and 65 coconuts; and the combined demand for both, 150 bananas and 100 coconuts, exactly equals the supply.

14.5 POLICY EXAMPLE

SHOULD THE GOVERNMENT TRY TO ADDRESS GROWING INEQUALITY THROUGH TAXES AND TRANSFERS?

Learning Objective 14.5: Show how any redistribution of resources leads to a Pareto-efficient competitive equilibrium.

Income inequality is the outcome of markets and society. An unequal distribution of societal resources can be represented in the abstract through the use of Edgeworth box analysis. Though an Edgeworth box represents only two people and two goods, the insight generalizes to many people and many goods. We can represent inequality by an initial distribution of societal resources that gives most of them to only one person, as shown in **figure 14.19**.

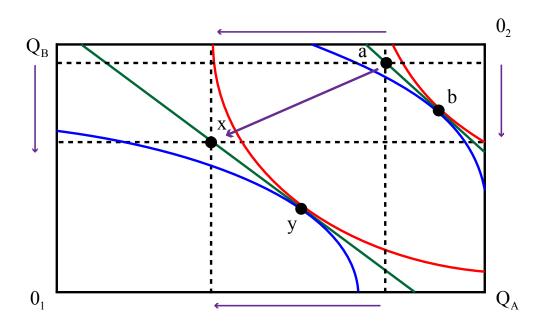


Figure 14.19 A tax and transfer scheme to address initial inequality

Figure 14.19 shows an economy where there are two people, 1 and 2, and two goods, A and B. The initial allocation is at A, where person 1 has most of both goods. The competitive equilibrium that is obtained from this allocation is at B, which is still highly unequal. To address this, a tax and transfer scheme could be implemented by taking away some of the initial allocation of A and B from A and transferring them to A. This is shown in **figure 14.19** as the movement from allocation A to the allocation A. The government that does this is not able to know all the societal preferences and thus is unable to know where the competitive equilibriums are—they do not know the contract curve. So their tax and transfer scheme does not get them directly to a competitive equilibrium. However, the first and second welfare theorems ensure that the competitive equilibrium is Pareto efficient and that A0 Pareto-efficient allocation can be obtained through a redistribution of the initial endowment.

So we can see in the figure that the new allocation x will lead to the Pareto-efficient outcome y. This suggests that there is no efficiency loss from a tax and transfer scheme. Person $\mathbf 1$ is worse off than before the taxes and transfers, and person $\mathbf 2$ is better off. Inequality has been addressed, but whether society is better off because of it is something that would require additional analyses.

What we can say is that there are no wasted societal resources—there is no inefficiency. This assumes, however, that the tax and transfer scheme itself is costless, while we know that in reality, such a program would require a lot of bureaucratic costs. We also have not analyzed what a tax and transfer scheme would do to the incentive to produce. If the rich were not able to enjoy the full benefit of their labor because of an income tax, economic theory suggests that they might not work as hard, and society would produce less. How would this reveal itself? In this case, the PPF would shrink, and so would the size of the Edgeworth box, and since we assume more is better, then the opposite must also be true—less is worse.

So both the bureaucratic costs and the loss from the disincentive to work suggest that there will be a cost to this program. The benefit is a more equal distribution of income. Thus whether it is a good idea

to implement, such a program depends on the relative benefits of a more equal income distribution and the costs of the program.

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

14.1 Partial versus General Equilibrium

Learning Objective 14.1: Explain the difference between partial and general equilibrium.

14.2 Trading Economy: Edgeworth Box Analysis

Learning Objective 14.2: Draw an Edgeworth box for a trading economy and show how a competitive equilibrium is Pareto efficient.

14.3 Competitive Equilibrium: Edgeworth Box with Prices

<u>Learning Objective 14.3</u>: Demonstrate how prices adjust to create a competitive equilibrium that is Pareto efficient from any initial allocation of goods.

14.4 Production and General Equilibrium

Learning Objective 14.4: Draw a production possibility frontier and explain how the mix of production is determined in equilibrium and how productive efficiency is guaranteed.

14.5 Policy Example

Should the Government Try to Address Growing Inequality through Taxes and Transfers?

Learning Objective 14.5: Show how any redistribution of resources leads to a Pareto-efficient competitive equilibrium.

LEARN: KEY TOPICS

Terms

Partial-equilibrium analysis

Studying the changes in a single market in isolation.

General-equilibrium analysis

The study of how equilibrium is obtained in multiple markets at the same time.

Endowments

The initial resources/goods available to a firm or an individual, i.e., when first shipwrecked, the endowment available to both Gilligan and Marianne are 100 coconuts and 150 bananas; Gilligan has a personal endowment of 60 coconuts and 60 bananas, and Mary Ann has a personal endowment of 40 coconuts and 90 bananas.

Contract curve

The line that connects all points of Pareto efficiency. See Figures 14.8 and 14.9.

Price line

A line on a graph that illustrates the set of available bundles at any given price. See Figure 14.10.

First theorem of welfare economics

Any competitive equilibrium is Pareto efficient.

Second theorem of welfare economics

Any Pareto-efficient competitive equilibrium is achievable through the reallocation of resources.

Production possibility frontier (PPF)

A line that shows all the possible combinations of outputs a firm/individual can produce in a day. See PPF Series in Graphs section below.

Marginal rate of transformation (MRT)

The cost of production of one good in terms of the foregone production of another good.

Comparative advantage

A person has a comparative advantage in the production of a good if they have a lower opportunity cost of production than someone else.

Consumption efficiency

The point at which it is not possible to redistribute goods to make one person better off without making another person worse off.

Productive efficiency

The point at which there exists no other mix of output levels that will increase the firm's earnings.

Graphs

General equilibrium in oil and SUV markets

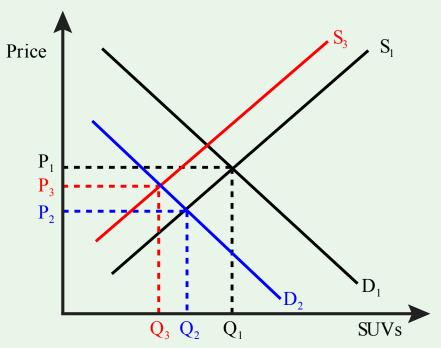


Figure 14.2 General equilibrium in SUV markets

Gilligan and Mary Ann's initial endowments and indifference curves

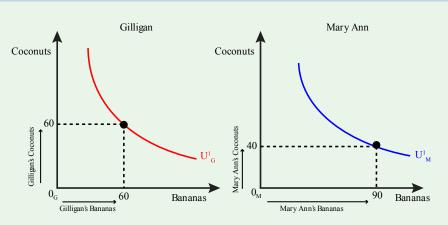


Figure 14.3 Gilligan and Mary Ann's initial endowments and indifference curves

The Edgeworth box for Gilligan and Mary Ann's economy

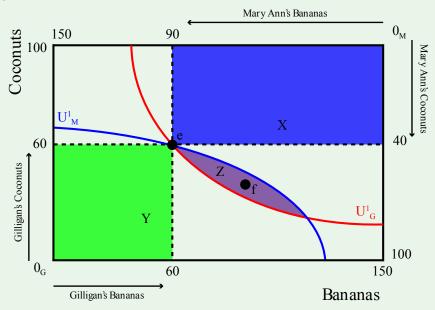


Figure 14.4 The Edgeworth box for Gilligan and Mary Ann's economy

Creating the Edgeworth box from two individual initial endowments and indifference curves

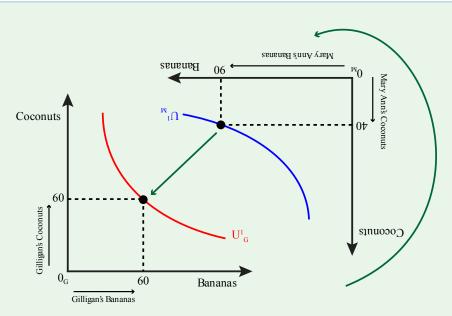


Figure 14.5 Creating the Edgeworth box from two individual initial endowments and indifference curves

Mutually beneficial trade to a Pareto-efficient allocation

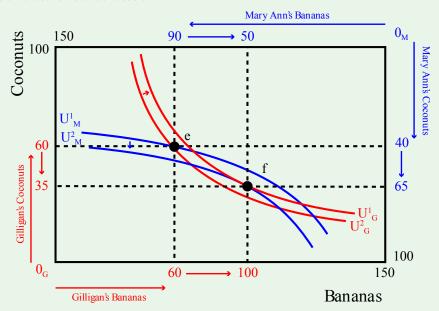


Figure 14.6 Mutually beneficial trade to a Pareto-efficient allocation

At the optimal point, the indifference curves are tangent, the MRSs are equal, and the allocation is Pareto efficient.

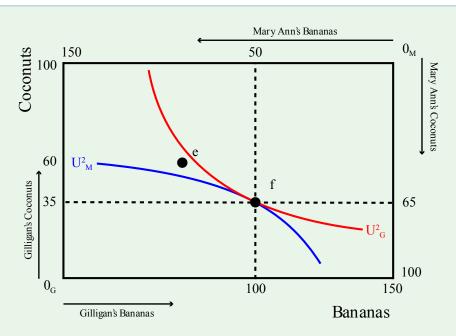


Figure 14.7 Tangent indifference curves, equal [latex]MRS[/latex]s, and the Pareto efficient allocation

The contract curve

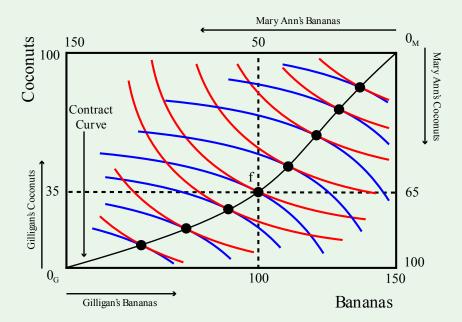


Figure 14.8 The contract curve

The contract curve, the lens, and the core

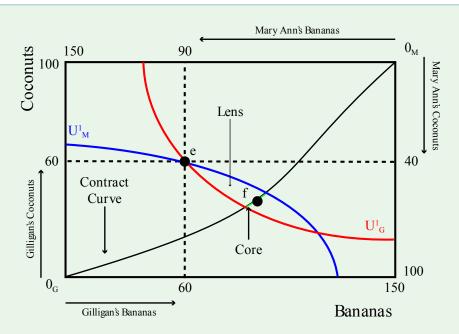


Figure 14.9 The contract curve, the lens, and the core

The initial endowment and the price line

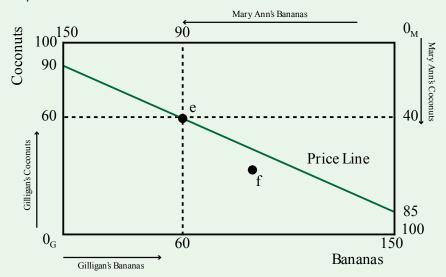


Figure 14.10 The initial endowment and the price line

No equilibrium in the product markets

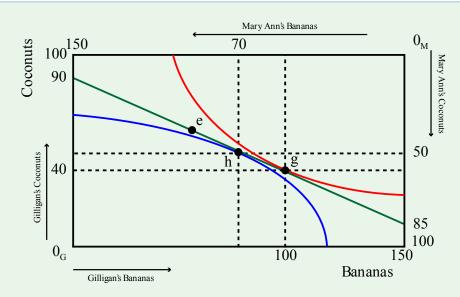


Figure 14.11 No equilibrium in the product markets

Competitive equilibrium in the island economy

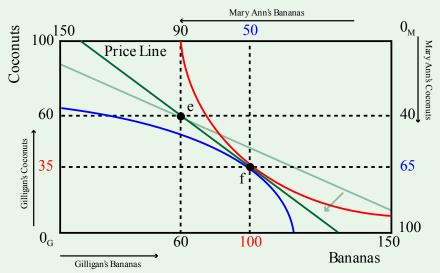


Figure 14.12 Competitive equilibrium in the island economy

Figures 14.13-14.17, Personal production possibility fronteirs

Individual production possibility frontiers

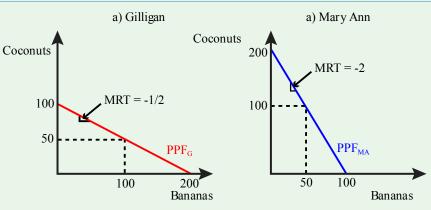


Figure 14.13 Individual production possibility frontiers

Joint production

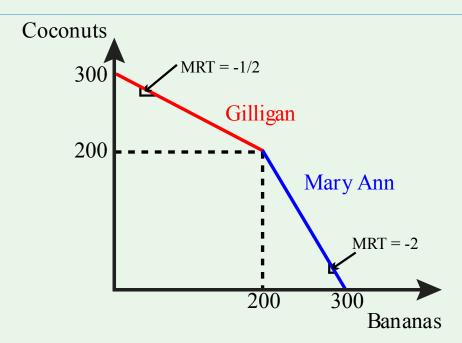


Figure 14.14 Joint production

Thurston's production possibility frontier

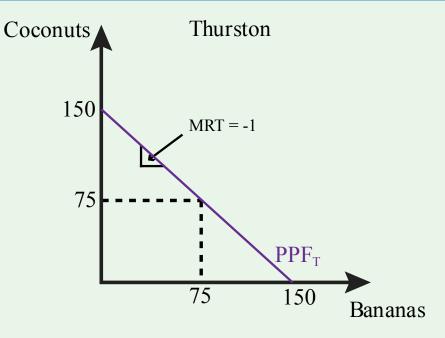


Figure 14.15 Thurston's production possibility frontier

The joint PPF with Thurston

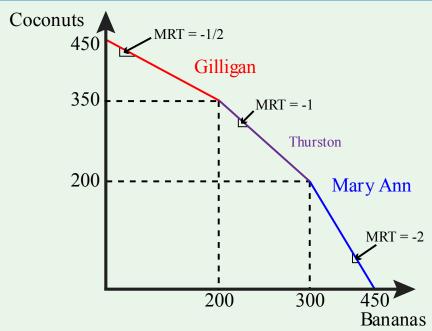


Figure 14.16 The joint [latex]PPF[/latex] with Thurston

The optimal product combination

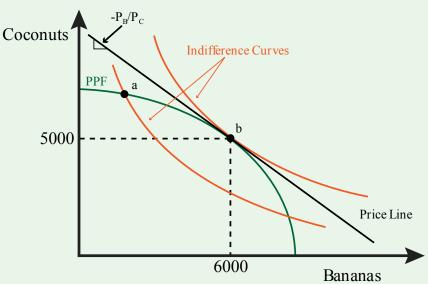


Figure 14.17 The optimal product combination

Competitive equilibrium

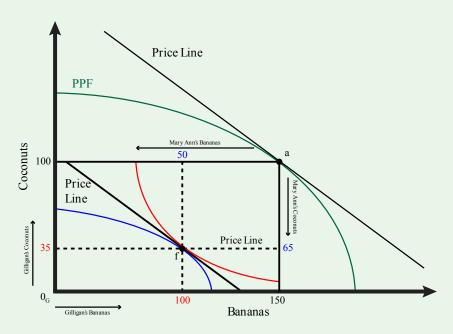


Figure 14.18 Competitive equilibrium

A tax and transfer scheme to address initial inequality

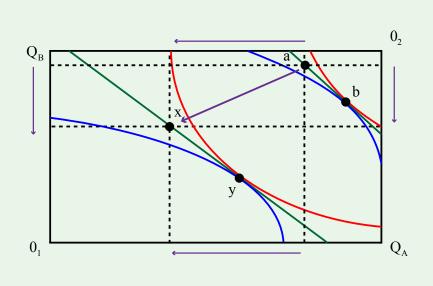


Figure 14.19 A tax and transfer scheme to address initial inequality

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CHAPTER 15

Monopoly



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THE POLICY QUESTION

SHOULD THE GOVERNMENT GIVE PATENT PROTECTION TO COMPANIES THAT MAKE LIFE-SAVING DRUGS?

In 1993, Shionogi, a Japanese pharmaceutical company, received a patent for the anti-statin medication rosuvastatin calcium, better known by its brand name, Crestor. Crestor is used to treat high cholesterol and related heart and cardiovascular diseases. Crestor has become one of the best-selling drugs of all time. In 2016, the patent protection will expire, and AstraZeneca, the manufacturer of Crestor, will cease to be a monopolist, and generic versions of the drug will flood the market. The patent created a twenty-three-year monopoly in the Crestor market, for which AstraZeneca has enjoyed enormous profits; the company recorded \$5 billion in Crestor sales in 2015 alone.

Providing a company the exclusive rights to sell a popular and medically important drug creates the potential for enormous profits, which gives pharmaceutical companies a very strong incentive to invest in the research and development of new drugs. But it also creates a situation in which medically necessary drugs are very expensive for consumers.

EXPLORING THE POLICY QUESTION

- 1. Does the societal benefit from the advent of new drugs outweigh the cost to society from the creation of monopolies?
- 2. What other way could society promote the development of new medicines?

LEARNING OBJECTIVES

15.1 Conditions for Monopoly

<u>Learning Objective 15.1</u>: Explain the conditions that lead to monopolies.

15.2 Profit Maximization for Monopolists

Learning Objective 15.2: Explain how monopolists maximize profits and solve for the optimal monopolist's solution from a demand curve and a marginal cost curve.

15.3 Market Power and the Demand Curve

Learning Objective 15.3: Describe the relationship between demand elasticity and a monopolist's ability to price above marginal cost.

15.4 Monopoly and Welfare

Learning Objective 15.4: Describe how monopolists create deadweight loss and explain how deadweight loss affects societal welfare.

15.5 Policy Example

Should the Government Give Patent Protection to Companies That Make Life-Saving Drugs?

<u>Learning Objective 15.5</u>: Explain the effect of patent protection on drug markets and the trade-off society makes to promote the development of new drugs.

15.1 CONDITIONS FOR MONOPOLY

Learning Objective 15.1: Explain the conditions that lead to monopolies.

A **monopoly** is the sole supplier of a good for which there does not exist a close substitute. In the policy example above, a firm that makes the only drug with which to treat or cure a disease is a monopolist if there is no other drug available to treat or cure the disease or if the only other drugs are not nearly as effective. Many drug makers continue to hold on to their trademarked drug names even after the patents

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run out and generic drugs enter the market, but the presence of the generics means that the original companies are no longer monopolists in the market for that particular drug.

As we learned in <u>chapter 13</u>, the characteristics of monopoly markets are a single firm, a unique product, and barriers to entry. But what are those barriers to entry, and where do they come from? There are two main sources of these barriers: (1) cost conditions that make it cheaper for one firm to produce and (2) government regulations that create legal barriers to entry that prevent other firms from competing in the same market.

Cost advantages can come from a number of sources. A firm might control an essential input; for example, one company might control the only source of a rare earth element used in high-performance batteries for automobiles. A firm might have better technology for or a better method of producing a good or service that gives it a cost advantage. Of course, this advantage only lasts as long as the firm is the only one with the technology or method. For this reason, many firms keep their production processes a closely guarded secret.

Another source of a monopoly is large fixed costs associated with production. If the fixed costs of production are large enough relative to the demand for a product, it may be true that only one firm can make non-negative economic profits. This is referred to as a **natural monopoly**—when one firm can supply the market more cheaply than two or more firms. For example, suppose an entrepreneur wants to start a concrete-pumping service in her isolated small town to provide concrete for difficult-to-reach places that normal concrete trucks are unable to access. Concrete-pumping trucks are very large and very expensive. The town might have enough demand to justify the cost of one such truck, and so the entrepreneur will attract enough business to cover the cost of the truck itself and the other accounting and opportunity costs of the business. But there might not be enough demand to justify the purchase of a second concrete-pumping truck if another business decided to start up. Thus the monopoly that results is a natural result of the large fixed cost relative to the limited demand.

We can express the concrete-pumping example more formally with a simple model. Suppose the marginal cost of supplying pumped concrete is fixed at c and the cost of the truck itself, the fixed cost, is F. The truck is a fixed cost because it costs F to acquire the truck, and this does not depend on the amount of concrete sold, or Q. The firm's total cost function is therefore TC=cQ+F. Average cost is AC=c+F/Q. This is the same for any firm that enters the market. Let's say that the cost of the truck, F, is \$500,000 per year, and the marginal cost is \$1 per cubic foot of concrete, Q. Now suppose that the demand is such that at MC=\$1, 100,000 cubic feet of concrete is sold per year. If there is one firm, the average cost of pumped concrete is AC=\$1+\$500,000/100,000, or AC=\$6. If there were two firms, the average cost of the industry would be $AC_IND=c+2F/Q$. Note that at a constant MC, the cost of a single cubic foot of concrete is always c, no matter which company provides it; however, with two firms, there are two fixed costs because each one has to pay for a truck. So AC=\$1+\$1,000,000/100,000/100,000, or AC=\$11. If the maximum willingness to pay for concrete at 100,000 cubic feet a year in this town is \$8, the town can only support one firm. One firm would make \$2 in economic profit in this business, while two firms would each lose \$3 in economic profit.

Another important source of monopoly power is government. The government itself owns and manages monopolies; for example, the federal government runs the US Postal Service, and local governments are often the sole provider of utilities such as water and sewer services. The government also provides protection from competition for individual firms, guaranteeing their monopoly status. The most common protection the government offers is patent protection, but the government can also require licenses to operate businesses—for example, a local hospital—and issue only one per market. The gov-

ernment can also grant a firm the right to operate as a monopoly; for example, a municipality might grant one company the right to collect residential trash.

A **patent** is an exclusive right to an invention that excludes others from making, using, selling, or importing it into the country for a limited time. In other words, the inventor is granted protection from any direct competition for a period of time, generally twenty years from the time an application is filed, and in exchange, the invention becomes public knowledge when the patent is granted. Why does the government offer patent protection? As we will see in the next section, being a monopolist often allows companies to collect positive economic profits—a better-than-normal return on investment. So patents give companies a reward for investing in new technologies, new drugs, and new methods that are valuable to society as an incentive.

15.2 PROFIT MAXIMIZATION FOR MONOPOLISTS

Learning Objective 15.2: Explain how monopolists maximize profits and solve for the optimal monopolist's solution from a demand curve and a marginal cost curve.

All profit maximizing firms, regardless of the structure of the markets in which they sell, maximize profits by setting the output so that marginal revenue equals marginal cost, as we learned in chapter 8 demonstrated how to find a marginal cost curve from the firm's total cost curve. What is different in the case of a monopoly is the marginal revenue curve. Perfectly competitive firms take prices as given; their output decisions do not change market prices, and so the marginal revenue for a perfectly competitive firm is simply the market price. Monopolists, on the other hand, are "price makers" in the sense that they can set their prices by picking a point on the demand curve. Note that they are not free of constraint; the demand curve dictates the maximum price they can charge for every quantity level. The task for the profit maximizing monopolist is to determine which point on the demand curve maximizes their profits. A downward-sloping demand curve will mean that the firm faces a trade-off: they can sell more but must lower their price to do so. This means that the marginal revenue of a monopolist will depend on their output decision.

The total revenue for a firm is the number of goods they sell, Q, multiplied by the price at which they sell the goods, p. Note that Q is both the firm's output and the market output, as there is only one firm supplying the market.

$$TR = pQ$$

The firm's marginal revenue is the change in total revenue from the sale of one more unit of its output. Thus in a firm that earns ΔTR extra revenue from the sale of ΔQ , more units have a marginal revenue of

$$MR = \frac{\Delta TR}{\Delta Q}.$$

Therefore, if the firm sells one more unit, $\Delta Q=1$ and $MR=\Delta TR$.

Calculus

Marginal revenue can be found from total revenue by taking the derivative:

Because of the price-quantity trade-off from the demand curve, the marginal revenue of a monopolist will depend on its output. Unlike a perfectly competitive firm whose product sells for a constant price and therefore has a constant price for its marginal revenue, a monopolist who wants to sell one more unit must lower its price to do so. Thus a monopolist's marginal revenue is a constantly declining function. It also declines at a rate greater than the demand curve because to sell more,

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the monopolist must lower the price of all its goods. **Figure 15.1** demonstrates the marginal revenue trade-off.

$$MR = \frac{dTR}{dQ}$$

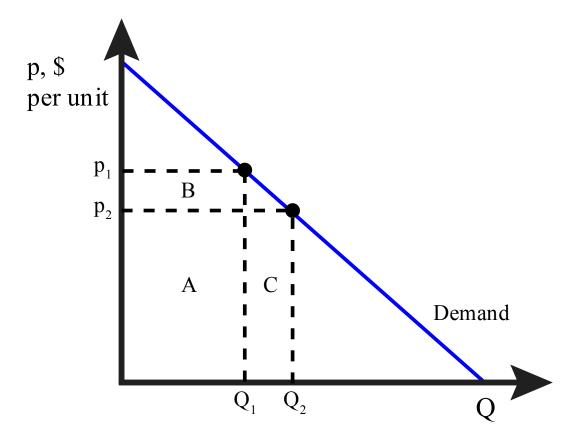


Figure 15.1 Monopoly, revenue, and marginal review

At price p_1 , the total revenue is p_1Q_1 , which is represented by the areas A+B. At price p_2 , the total revenue is p_2Q_2 , which is represented by the areas A+C. Area A is the same for both, so the marginal revenue is the difference between B and C, or C-B.

Note that area C is the price, p_2 , times the change in quantity, Q_2-Q_1 , or $p\Delta Q$, and area B is the quantity, Q_1 , times the change in price, p_2-p_1 , or ΔpQ . Since p_2-p_1 is negative, the change in total revenue is C-B, or

$$\Delta TR = p\Delta Q + \Delta pQ$$
.

Dividing both sides by ΔQ gives us an expression for marginal revenue:

(15.1)
$$MR=rac{\Delta TR}{\Delta Q}=p+Qrac{\Delta p}{\Delta Q}$$

This expression has an intuitive interpretation. The first part, p, is the extra revenue the firm gets from selling an extra unit of the good. The second part, $Q\frac{\Delta p}{\Delta Q}$, which is negative, is the decrease in revenue from the fact that increasing output marginally lowers the price the firm receives for all of its output.

Since the second part is negative, we know that the MR curve is below the demand curve for every Q, since the demand curve relates price and quantity.

Figure **15.2** shows the relationship between a linear demand curve and the marginal revenue curve in the top panel and the total revenue in the bottom panel.

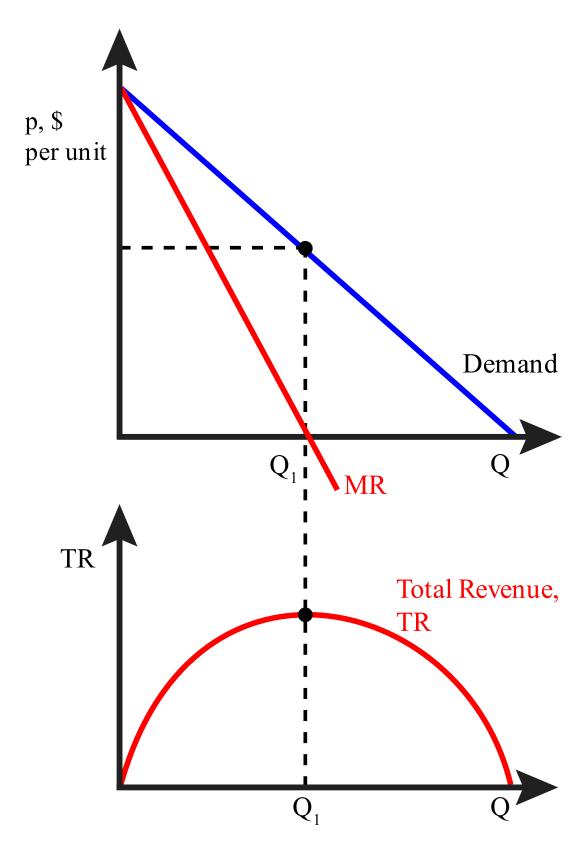


Figure 15.2 Demand, marginal revenue, and total revenue

Since marginal revenue is the rate of change in total revenue for a marginal increase in quantity, when marginal revenue is positive, the total revenue curve has a positive slope, and when marginal revenue is

negative, the total revenue curve has a negative slope. Note that this means the total revenue is maximized at the point where marginal revenue is zero.

A profit maximizing firm chooses an output so that the marginal cost of producing that output exactly matches the marginal revenue it gets from selling that output. Now that we have the marginal revenue, all that remains is to add the marginal cost. **Figure 15.3** shows that the optimal output for the monopolist is where marginal revenue and marginal cost intersect.

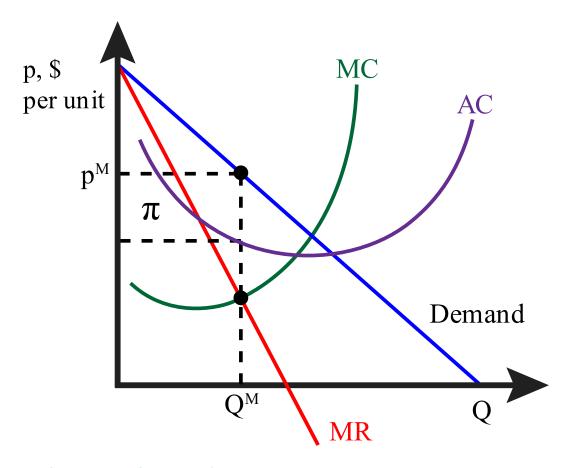


Figure 15.3 Profit maximization for a monopolist

The intersection of the marginal revenue and marginal cost curves occurs at point Q^M , and the highest price at which the monopolist can sell exactly Q^M is p^M . At Q^M , the total revenue is simply $(p^M) \times (Q^M)$, and total cost is $(AC) \times (Q^M)$, since AC is just TC/Q. Therefore, the shaded area is the difference between total revenue and total cost or profit.

Mathematically, profit maximization for a monopolist is the same as for any firm: find the output level for which marginal revenue equals marginal cost. Let's start with a general example. Suppose the demand for a good produced by a monopolist is p=A=BQ. Note that this is an **inverse demand curve**, a demand curve written with price as a function of quantity. We could easily solve it for Q to get it back in normal form: Q=A/B—p/B. We can find the marginal revenue curve by first noting that $TR=p\times Q$. Thus $TR=(A-BQ)\times Q$, or $TR=AQ-BQ^2$.

The marginal revenue from a linear demand curve is a curve with the same vertical intercept as the demand curve (in this case, A) and a slope twice as steep (in this case, -2B). In other words, for an inverse demand curve, p=A-BQ, and the marginal revenue curve is MR=A-2BQ.

Let's consider a specific example: suppose that Tesla is a monopolist in the manufacture of luxury electric cars. For its electric Model S cars, let's say it faces an annual demand curve of Q=200-2p (in thousands). Its marginal cost of producing a Model S is MC=Q (also in thousands).

Calculus ${}^{\rm If}TR=AQ{-\!\!\!\!\!--}BQ^2,$ then $MR=\partial TR\partial Q=A-2BQ$

First, we will solve for the monopolist's profit maximizing level of output and the profit maximizing price. Second, we will graph the solution.

To solve the problem, we need to proceed in four steps: (1) find the inverse demand curve; (2) find the marginal revenue curve; (3) set marginal revenue equal to marginal cost and solve for Q^M , the monopolist's profit maximizing output level; (4) find p^M , the monopolist's profit maximizing price.

1. Find the inverse demand curve by solving for demand curve for p:

$$Q = 200 - 2p \ 2p = 200 - Q \ p = 100 - rac{1}{2}Q$$

2. Find the marginal revenue curve by doubling the slope coefficient (B):

$$MR=100-(2) imes(rac{1}{2})Q$$
 $MR=100-Q$

3. Set MR equal to MC and solve for Q:

$$egin{aligned} MR &= MC \ 100 - Q &= Q \ 100 &= 2Q \ Q^M &= 50 ext{ or } \ Q^M &= 50,000 \end{aligned}$$

4. Find p^M from the inverse demand curve:

$$egin{aligned} p &= 100 - rac{1}{2}Q \ p &= 100 - frac12(50) \ p &= 100 - 25 \ p^M &= \$75 ext{ or } \ p^M &= \$75,000 \end{aligned}$$

So the optimal output of Model S cars for Tesla is fifty thousand cars, and the optimal price is \$75,000 per car.

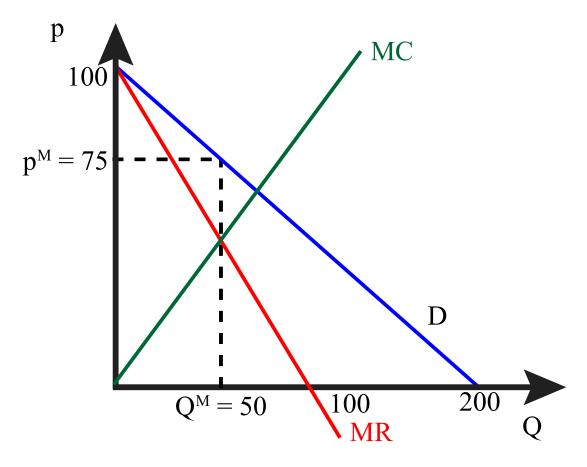


Figure 15.4 Solution to Tesla's profit maximization problem

In order to determine Tesla's profit, we need the total cost function. Suppose total cost is $TC=\frac{1}{2}Q^2$. In this case, with $Q^M=50$ and $p^M=\$75$, the total revenue is $TR=\$75\times50=\$3,750$, or \$3.75 million. Total cost is $TC=\frac{1}{2}(50)^2=\$1,250$, or \$1.25 million. So profit, which is TR-TC, equals \$2,500, or \$2.5 million.

15.3 MARKET POWER AND THE DEMAND CURVE

Learning Objective 15.3: Describe the relationship between demand elasticity and a monopolist's ability to price above marginal cost.

A firm that faces a downward-sloping demand curve has **market power**: the ability to choose a price above marginal cost. Monopolists face downward-sloping demand curves because they are the only supplier of a particular good or service, and the market demand curve is therefore the monopolist's demand curve. How much market power a firm has is a function of the shape of the demand curve. A market in which customers are price sensitive is one with a highly elastic demand curve, or one that is relatively flat. A market in which customers are very price insensitive is one with a highly inelastic demand curve, or one that is relatively steep. What makes customers more or less price sensitive? This could be caused by a number of factors, but the most important one is the availability of good substitutes. A drug company

that has a patent for a drug that is the only cure for a serious disease is likely to face an inelastic demand curve, as those who have the disease will be likely to buy at any price they can afford, since there is no other choice. However, a smartphone company that has a patent for its unique technologies would probably face a highly elastic demand curve because customers are likely to switch to a different smartphone with slightly different capabilities if the price is too high.

Consider Tesla, the example from 15.2: Tesla arguably has a monopoly on luxury all-electric cars. But there are many other non-luxury all-electric cars and luxury hybrid cars with both gas and electric motors. Tesla's demand curve is probably somewhere in between the two examples above. There are substitutes, but they are quite a bit different from the Tesla, and so customers of Tesla are probably fairly price insensitive.

The relationship between the elasticity of the demand curve that a monopolist faces and the monopolist's ability to price above its marginal cost can be derived by using the marginal revenue equation (15.1):

$$MR = p + Q rac{\Delta p}{\Delta Q}$$

Profit maximization implies that MR=MC, so

$$p+Qrac{\Delta p}{\Delta Q}=MC.$$

If we multiply $Qrac{\Delta p}{\Delta Q}$ by $rac{p}{p}$, we don't change the value, since $rac{p}{p}=1$, but we can rearrange to get

$$(rac{\Delta p}{\Delta Q}xrac{Q}{p})xp$$
, or

$$p+(rac{\Delta p}{\Delta q}xrac{Q}{p})xp=MC.$$

Notice that the term in the parentheses is the inverse of the elasticity, $\frac{1}{\varepsilon}$, from <u>chapter 5</u>, so

$$p+(rac{1}{arepsilon}) imes p=MC$$

Rearranging terms yields

(15.2)
$$\dfrac{p-MC}{p}=-\dfrac{1}{arepsilon}$$

We call the left-hand side of this equation the **markup**: the percentage of the price is above marginal cost. The right-hand side of the equation says that the markup is inversely related to the elasticity of the demand. As consumers are more price sensitive, the absolute value of the elasticity increases, causing the right-hand side of the equation to decrease, meaning the markup decreases—monopolists are not able to charge as high a price as if they faced price-insensitive customers. Equation (15.2) has a special name, the **Lerner index**, and it measures the firm's optimal markup. This is also a measure of market power, as firms with more market power are more able to charge prices above marginal cost. Notice that when the demand curve is perfectly elastic, or horizontal, the monopolist is in the same situation that a perfectly competitive firm is. Perfect elasticity implies that $\varepsilon = \infty$, or that the right-hand side of the Lerner index is essentially zero, meaning the monopolist sets price equal to marginal cost, just as if they were a perfectly competitive firm. On the other extreme, a perfectly inelastic demand curve has an elasticity close to zero. In this case, the markup is infinitely high.

We know from figure 15.2 that a monopolist firm will never want to operate on the inelastic part of the demand curve, and the Lerner index confirms that if |e|<1, the index is greater than one, and this implies that p-MC>p, which can only be true if marginal cost is negative, and marginal cost can never be negative.

The relationship between markup and demand elasticity can be seen graphically, as in figure 15.5.

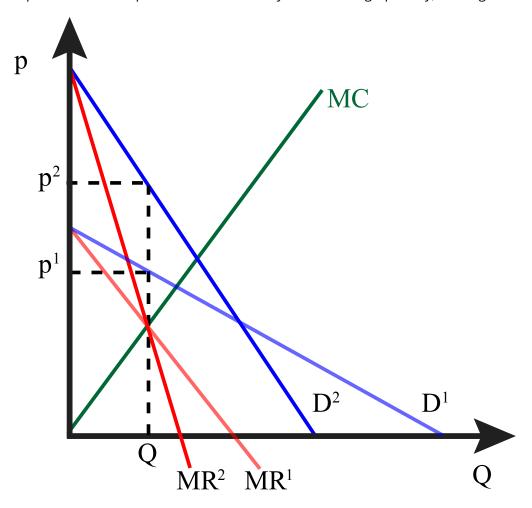


Figure 15.5 The markup and shape of the demand curve

In the figure above, D^1 is the demand curve, which is much more elastic than D^2 . This means that if the monopolist tries to charge higher prices, it loses more sales than if it faced D^2 . This constrains the monopolist, and therefore p^1 is significantly lower than p^2 . As an example, using the Lerner index, suppose that at Q, the elasticity from D^1 is -4 and the elasticity from D^2 is -2. The Lerner index for p^1 is 1/2, .25, or a 25 percent markup. The Lerner index for 1/20 is 1/22, .5, or a 50 percent markup.

15.4 MONOPOLY AND WELFARE

Learning Objective 15.4: Describe how monopolists create deadweight loss and explain how deadweight loss affects societal welfare.

In <u>chapter 10</u>, we learned that welfare is defined as the sum of consumer and producer surplus. Perfectly competitive markets that meet a set of criteria maximize welfare and achieve efficiency. Monopoly markets do not. To understand why not, think about the marginal revenue's relationship to the demand

curve, as explained in <u>section 15.2</u>. The monopolist's incentive is to limit output in order to keep prices high for all its goods.

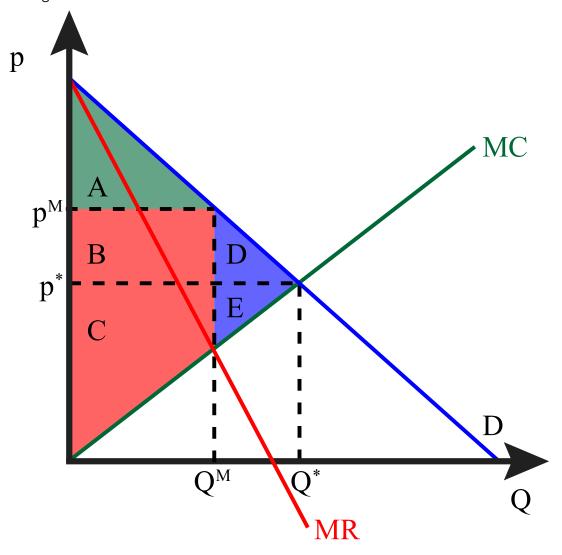


Figure 15.6 Monopoly and deadweight loss

In **figure 15.6**, the monopolist output, Q^M , and the monopolist's price, p^M , create an area of consumer surplus of A. The producer surplus is area B+C, and the total surplus is A+B+C. We can compare this outcome to the perfectly competitive outcome, which is shown as p^* and Q^* , or where price equals marginal cost, which is what we know is the perfectly competitive firm's outcome. In this case, the consumer surplus is A+B+D, and the producer surplus is C+E, for a total surplus of A+B+C+D+E. The difference in total surplus between the perfectly competitive outcome and the monopoly outcome is D+E. This is the deadweight loss that results from the presence of a monopoly in this market. Again, the deadweight loss is the potential surplus not realized due to the lower level of output.

As an example, suppose that a drug company has a patent for a drug that makes it a monopolist on the market for that drug. The demand for that drug is described by the inverse demand curve p=30-Q, and the firm's marginal cost is MC=Q, where Q is in thousands. The monopolist's profit maximizing

level of output is where MR equals MC and marginal revenue is a line with the same vertical intercept, 30, and twice the slope, 2: MR=30-2Q.

So
$$MR=MC$$
 yields $30-2Q=Q$, or $30=3Q$, or $Q^M=10million$, and therefore, since $p=30-Q$, $p^M=\$20$.

That is the monopolist's profit maximizing solution. What is the perfectly competitive market solution? It is where p equals MC:

$$p=30-Q=Q=MC$$
, or $2Q=30$, or $Q^st=15million$

and

$$p^* = \$15$$
.

Graphically, this looks like **figure 15.7**.

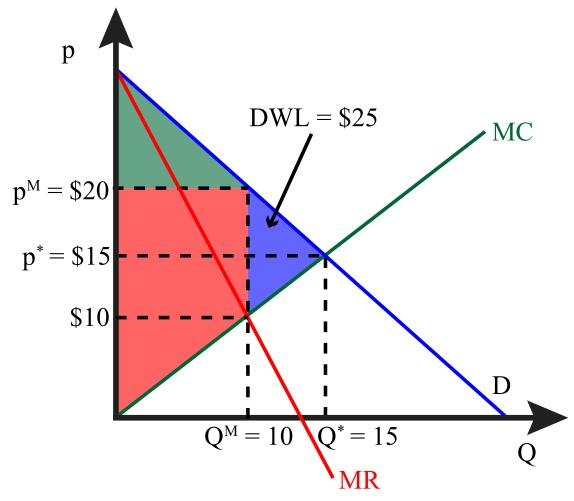


Figure 15.7 Deadweight Loss from Monopoly

We can see from figure **15.7** that the deadweight loss is a triangle with a base of 10, because at $Q^M=10$, MC=\$10 and $p^M=\$20$; therefore, the distance between the two is \$10 with a height of 5, the difference between Q^M and Q^* . Using the formula for the area of a triangle of ½ base times height, we get $\frac{1}{2}(\$10)(5)=\25 .

SHOULD THE GOVERNMENT GIVE PATENT PROTECTION TO COMPANIES THAT MAKE LIFE-SAVING DRUGS?

Learning Objective 15.5: Explain the effect of patent protection on drug markets and the trade-off society makes to promote the development of new drugs.

Providing companies like AstraZeneca patent protection for drugs like Crestor gives them a profit incentive to invest in the research and development of new, medically important drugs. However, from section 15.4, we also know that monopoly power creates deadweight loss. **Figure 15.8** shows the deadweight loss that results from monopoly power, but it is important to understand what the deadweight loss represents: this is the loss to society that results from the reduction in output of these medically important drugs. By restricting output, monopolies keep prices high and, in so doing, exclude a segment of consumers who would purchase the drugs if the price were at marginal cost, as would be the case in a perfectly competitive market.

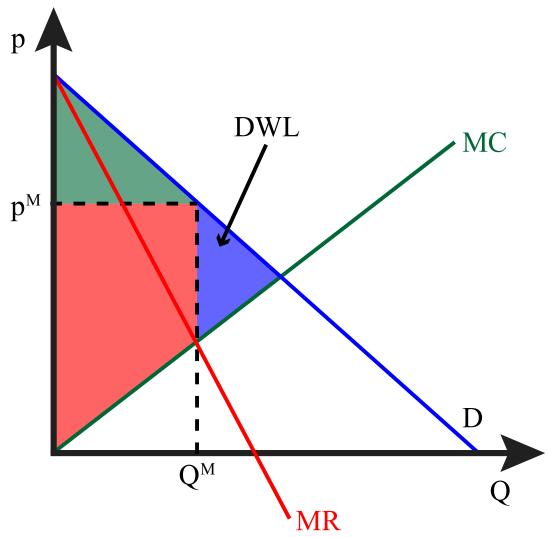


Figure 15.8 Deadweight loss from monopoly power

However, there would be an even larger deadweight loss if the drug was never discovered and the market never created. The total surplus, the combination of the red- and green-shaded areas in **figure 15.8**, would be lost.

The most basic policy question is therefore whether the benefit to society is greater than the dead-weight loss. Given the diagram in **figure 15.8**, the answer is almost certainly yes. Another policy question is whether there is an alternate policy that could achieve the same objective of developing new medicines at a lower societal cost—the most obvious is to fund the research of new medicines directly by the government and then allow new discoveries to be produced by many firms. This would lead to more production and lower costs of new drugs but might not be as efficient at promoting new discoveries. A final question is whether the patent protections promote the discovery of only the most profitable drugs, such as those often associated with aging in high-income countries. Malaria, a disease that remains one of the most lethal in the world, has not generated a lot of funding for the creation of a new drug to combat it, and many critics believe this is because it is a disease most commonly found in low-income countries and thus the potential profits are low because the market could not support high prices. Supporters of the current system like the fact that it is private enterprise, not the government, that decides in which areas to invest resources, thus ensuring that the drugs with the highest expected benefits are invested in most heavily.

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

15.1 Conditions for Monopoly

<u>Learning Objective 15.1</u>: Explain the conditions that lead to monopolies.

15.2 Profit Maximization for Monopolists

Learning Objective 15.2: Explain how monopolists maximize profits and solve for the optimal monopolist's solution from a demand curve and a marginal cost curve.

15.3 Market Power and the Demand Curve

Learning Objective 15.3: Describe the relationship between demand elasticity and a monopolist's ability to price above marginal cost.

15.4 Monopoly and Welfare

Learning Objective 15.4: Describe how monopolists create deadweight loss and explain how deadweight loss affects societal welfare.

15.5 Policy Example

Should the Government Give Patent Protection to Companies That Make Life-Saving Drugs?

<u>Learning Objective 15.5</u>: Explain the effect of patent protection on drug markets and the trade-off society makes to promote the development of new drugs.

LEARN: KEY TOPICS

Terms

Monopoly

The sole supplier of a good for which there does not exist a close substitute.

Natural monopoly

When one firm can supply the market more cheaply than two or more firms.

Patent

An exclusive right to an invention that excludes others from making, using, selling, or importing it into the country for a limited time.

Inverse demand curve

A demand curve written with price as a function of quantity. See figure 15.3.

Markup

The percentage of the price above marginal cost.

Market power

The ability to choose a price above marginal cost.

The Lerner index

Measures the firm's optimal markup. This is also a measure of market power, as firms with more market power are more able to charge prices above marginal cost.

$$\frac{p-MC}{p}=-\frac{1}{\varepsilon}$$

Graphs

Monopoly, revenue, and marginal revenue

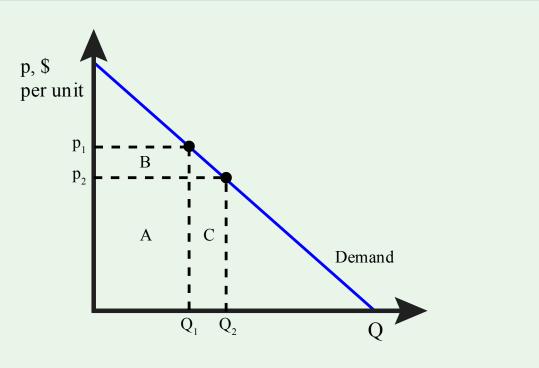
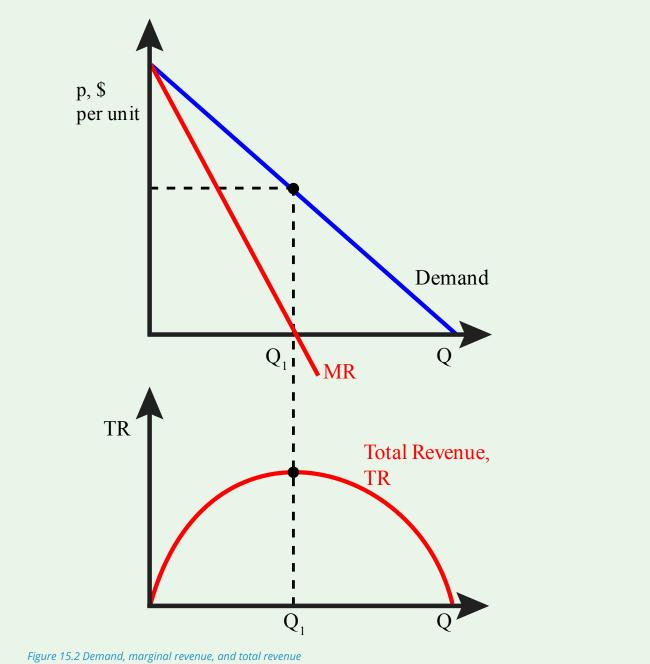


Figure 15.1 Monopoly, revenue, and marginal review

Demand, marginal revenue, and total revenue



Profit maximization for a monopolist

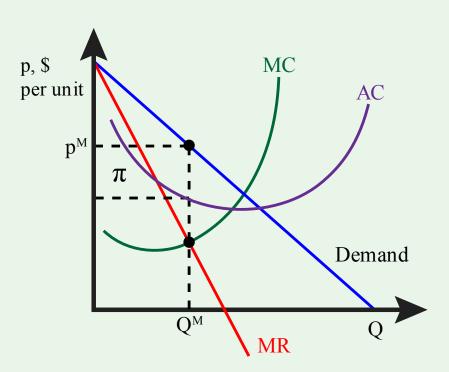


Figure 15.3 Profit maximization for a monopolist

Solution to Tesla's profit maximization problem

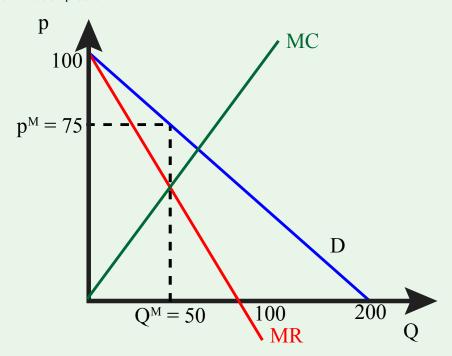
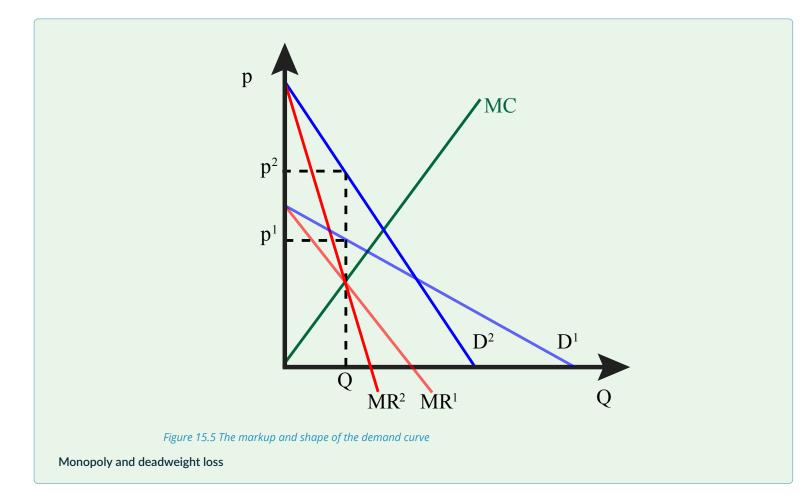
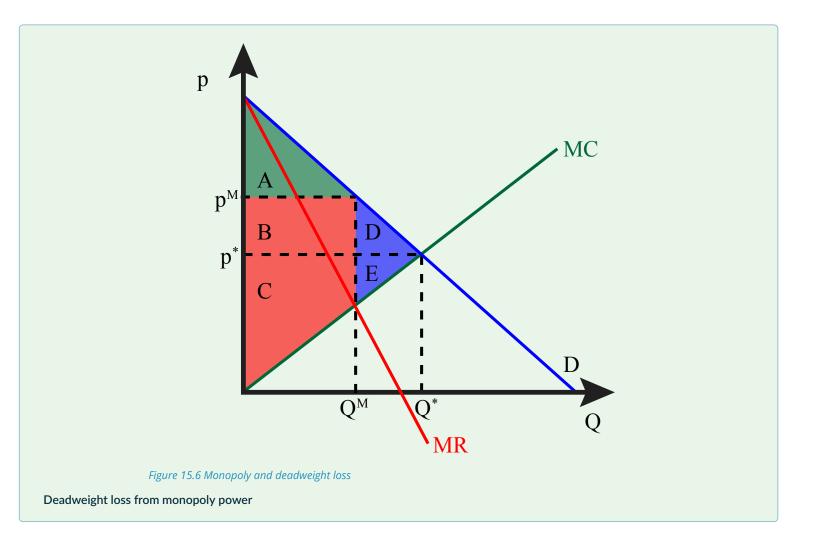


Figure 15.4 Solution to Tesla's profit maximization problem

The markup and shape of the demand curve





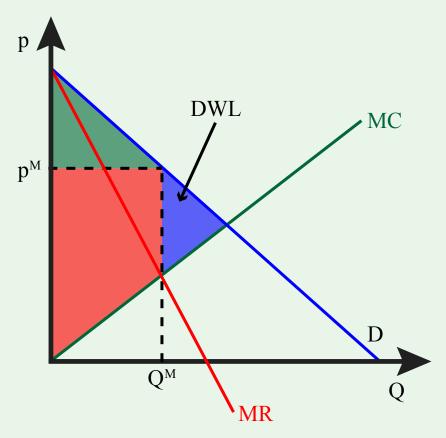


Figure 15.8 Deadweight loss from monopoly power

Equations

Marginal revenue

$$MR = rac{\Delta TR}{\Delta Q} = p + Qrac{\Delta p}{\Delta Q}$$

The Lerner index

Measures the firm's optimal markup. Also measures market power, as firms with more market power are more able to charge prices above marginal cost.

$$\frac{p-MC}{p}=-\frac{1}{\varepsilon}$$

Marginal revenue curve produced by an inverse demand curve

The marginal revenue from a linear demand curve is a curve with the same vertical intercept as the demand curve and a slope twice as steep. The demand for a particular good is (or the inverse demand curve, or the demand curve solved as a function of price):

$$p = A - BQ$$

The marginal revenue curve is found by first noting that:

$$TR = p \times Q$$

Total revenue equals profit times output, and therefore,

$$TR=(A-\!\!\!\!-BQ) imes Q$$
 or $TR=AQ-\!\!\!\!-BQ^2$ and if $TR=AQ-\!\!\!\!-BQ^2$, then

$$MR = \partial TR\partial Q = A - 2BQ$$

In other words, for an inverse demand curve of

$$p = A - BQ$$

the marginal revenue curve is

$$MR = A - 2BQ$$

The Tesla example

Optimizing a monopolist's output and profit is a two-part process. The first part is solving for the monopolist's profit maximizing level and the second is solving for their profit maximizing price. The results are usually graphed afterwards.

Solving for the monopolist's profit maximizing level of output

A four step process.

I. Find the inverse demand curve

Find the inverse demand curve by solving for the demand curve for ${oldsymbol p}$

$$Q = 200 - 2p \ 2p = 200 - Q \ p = 100 - rac{1}{2}Q$$

II. Find the marginal revenue curve

Find the marginal revenue curve by doubling the slope coefficient (B)

$$MR=100-(2) imes(rac{1}{2})Q$$
 $MR=100-Q$

III. Solve for Q

Set marginal revenue (MR) equal to (MC) and solve for Q

$$MR=MC \ 100-Q=Q \ 100=2Q \ Q^M=50 \ {
m or} \ Q^M=50,000$$

IV. Find p^M

Find p^M from the inverse demand curve

$$p = 100 - rac{1}{2}Q$$
 $p = 100 - frac12(50)$ $p = 100 - 25$ $p^M = \$75$ or $p^M = \$75,000$

Solving for Tesla's profit maximizing price

Requires the total cost function. A theoretical total cost equation for Tesla:

$$TC=rac{1}{2}Q^2$$

Previously defined variables p^M (\$75) and Q^M (\$50) are now substituted into Tesla's total cost function and the total revenue equation:

$$TR = \$75 \times 50 = \$3,750$$
 $TC = \frac{1}{2}(50)^2 = \$1,250$

This defines the variables of total cost (TC) and total revenue (TR) as \$1,250 and \$3,750, respectively. Substituting into the profit equation:

$$p = TR - TC$$

gives us p=3750-1250, or 2,500; in this case, we have sliced zeroes off for ease of calculation, so the exact total is \$2.5 million.

The graphed solution to the Tesla example

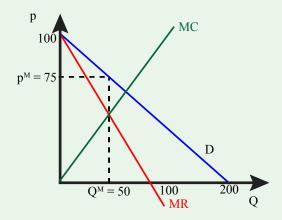


Figure 15.4 Solution to Tesla's profit maximization problem

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CHAPTER 16

Pricing Strategies

THE POLICY QUESTION

SHOULD PUBLIC UNIVERSITIES CHARGE EVERYONE THE SAME PRICE?

Modern public universities, like their private counterparts, publish a tuition price each year that few students actually pay. Most students receive internal grants and awards that reduce their costs well below the list price. The amount of this reduction in price varies dramatically and is closely related to the income of the student's family.

Unlike their private counterparts, public universities in the United States receive public funding and are expected, in return, to provide an affordable college education for residents of the states they serve. Are their pricing policies antithetical to their mission? Are they fair? Do they support the mission of the institution? These are questions we will seek to answer by studying the practice of price discrimination.

EXPLORING THE POLICY QUESTION

- 1. Does charging tuition based on family income support or undermine the mission of public universities?
- 2. Is charging tuition based on family income fair?

LEARNING OBJECTIVES

16.1 Market Power and Price Discrimination

Learning Objective 16.1: Explain differentiated pricing and describe the three types of price discrimination.

16.2 Perfect or First-Degree Price Discrimination

Learning Objective 16.2: Describe first-degree price discrimination and the challenges that make it hard.

16.3 Group Price or Third-Degree Price Discrimination

Learning Objective 16.3: Describe third-degree price discrimination and its effect on profits.

16.4 Quantity Discounts, or Second-Degree Price Discrimination

Learning Objective 16.4: Describe second-degree price discrimination and how it overcomes the identification problem.

16.5 Two-Part Tariffs and Tie-In Sales

Learning Objective 16.5: Define two-part tariffs and tie-in sales and how they work as price discrimination mechanisms.

16.6 Bundling, Versioning, and Hurdles

Learning Objective 16.6: Define bundling, versioning, and hurdles and how each works to increase firm profits.

16.7 Policy Example

Should Public Universities Charge Everyone the Same Price?

<u>Learning Objective 16.7</u>: Explain how the use of price discrimination can be seen as a way for public universities to accomplish their mission.

16.1 MARKET POWER AND PRICE DISCRIMINATION

Learning Objective 16.1: Explain differentiated pricing and describe the three types of price discrimination

Firms that have market power face demand curves that are downward sloping. We call such firms price makers, since the shape of the demand curve gives them choices about the prices they charge. Monopolists of the type examined in chapter 15 are simple monopolists: monopolists that are limited to a single price at which all the output they produce is sold. This limitation leads simple monopolists to limit output so that they can maintain a higher price for all their goods or services. This limitation in output creates deadweight loss, the lost surplus from transactions that don't happen but that for which positive total surplus is possible. What we will see in this chapter is that firms with market power that are able to differentiate their consumers based on their demands or willingness to pay for the goods and services may be able to charge different prices for their goods and services. This practice is called **differentiated** pricing: selling the same good or service for different prices to different consumers. Differentiated pricing can come in many forms, from a car dealership that negotiates prices with consumers, selling the same model car for different prices to different customers; to a movie theater that offers a student price and an adult price; to volume discounts where consumers who buy multiple units qualify for lower perunit prices, such as a sale on socks that are either \$4 a pair or \$10 for three pairs. Differentiated pricing can also come in the form of bundling, selling a set of goods for a single price, and product differentiation, selling different versions of a product for different prices that do not reflect production cost differences.

These more sophisticated pricing strategies are the topic of this chapter, and economists call the practice of charging different prices for the same good to different consumers **price discrimination**. Price discrimination often leads to higher profits for firms and to higher output, as the incentive to constrain output to maintain a higher price for all units is no longer there. Price discrimination allows discriminating firms to capture more or all of the consumer surplus and the deadweight loss that results from a single price and is therefore a strategy that increases profits. As we will see in this chapter, price discrimination

ination can be hard because it requires firms to know information about consumers' demands and to be able to prevent the resale of goods by a consumer who was charged a low price to a consumer who is being charged a high price.

Price discrimination is characterized by three main categories in economics: perfect price discrimination, group price discrimination, and quantity discounts. **Perfect price discrimination**, or **first-degree price discrimination**, is a type of pricing strategy that charges every consumer a price equal to their willingness to pay. Firms that can do this can extract the entire consumer surplus and all the deadweight loss for themselves and can extract all potential profit from a market. This type of price discrimination is rare because it requires that firms deduce each consumer's willingness to pay and change the price to equal it. Though it might be a hypothetical extreme, many firms try to charge customers a price that is based on their willingness to pay, even if they can't reach their exact willingness to pay. Car dealers that set final prices through negotiations or haggling are an example of this.

When firms are unable to ascertain individual willingness to pay but know something about the average demands among different distinguishable groups, they can **practice group price discrimination**, or **third-degree price discrimination**: charging different prices for the same good or service to different groups or different types of people. Movie theater pricing is a good example of this type of price discrimination: they often have different prices for kids, students, adults, and seniors. This type of price discrimination requires only that firms are able to ascertain group membership and prevent resale from one group to the other.

When firms are unable to determine individuals' willingness to pay or categorize individuals into groups based on average demand, they can often employ pricing strategies that get consumers to self-select different prices based on their demands through the use of quantity discounts. **Quantity discounts**, or **second-degree price discrimination**, are when firms charge a lower price per unit to consumers who purchase larger amounts of the good.

It is important to understand that any firm with pricing power can potentially price discriminate, but in this chapter, we are focusing on monopolists and how these pricing strategies are potentially profit enhancing. It is also important to note that not all price differentials are evidence of price discrimination, such as when price differentials simply reflect the actual cost differential. For example, a store might offer a single pair of socks for \$4 or three pairs for \$10, which could be clever price discrimination; however, a mail-order retailer might make the same offer knowing that it costs \$1 to prepare the shipment regardless of how many pairs of socks are ordered. So the socks are being sold for \$3 plus the preparation charge, and the price difference is simply a reflection of this fixed cost divided by the number of pairs of socks.

16.2 PERFECT OR FIRST-DEGREE PRICE DISCRIMINATION

Learning Objective 16.2: Describe first-degree price discrimination and the challenges that make it hard. Imagine a firm with market power that can prevent the resale of its goods and is able to ascertain each of its customers' reservation price or maximum willingness to pay. If they are able to sell their goods at individual prices, the very best they can do in each transaction is to charge each customer exactly their reservation price. This ensures maximum revenue from each transaction as well as that the entire available surplus is captured by the firm as producer surplus.

Consider the example of a firm that makes gold-plated designer smartphones that has only five potential customers, each of whom would purchase exactly one unit if the price is at or below their reservation price.

| Table 16 1 | Customers and | thair racanyati | on nrices |
|------------|---------------|-----------------|-----------|
| | | | |

| Consumer | Reservation price (\$) |
|----------|------------------------|
| 1 | \$10,000 |
| 2 | \$8,000 |
| 3 | \$6,000 |
| 4 | \$4,000 |
| 5 | \$2,000 |

In the case of a simple monopolist, the firm does not know the reservation prices of its consumers; in this case, the firm does know the reservation prices of individual consumers. Suppose in addition that the marginal cost of producing a unit of this good is \$3,000. In **figure 16.1**, we see that at a price of \$10,000, the firm would sell exactly one unit because there is only one consumer who has a reservation price that high.

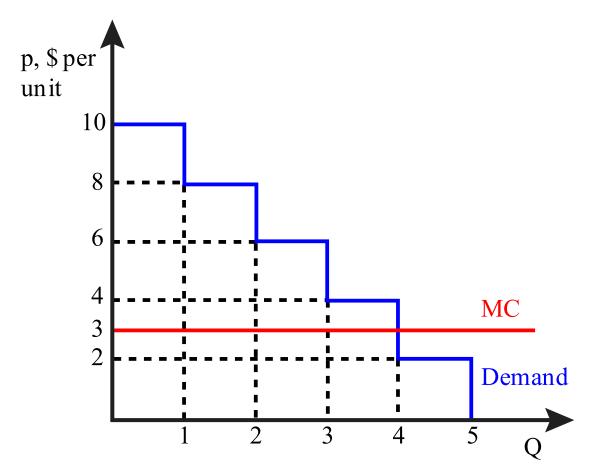


Figure 16.1 First-degree price discrimination

If the firm can practice perfect or first-degree price discrimination, it means that they know each consumer's reservation price and can prevent resale, so the firm can charge consumer 1 \$10, consumer 2 \$8, consumer 3 \$6, consumer 4 \$4, and even consumer 5 \$2. However, since consumer 5's reservation price is below the marginal cost of production, the firm will choose not to sell to consumer 5. The marginal revenue is \$10 for the first unit, \$8 for the second unit, \$6 for the third unit, and \$4 for the fourth unit. The surplus created by the sale of the first unit is the difference between the reservation price and the marginal cost: \$10 - \$3 = \$7. This surplus is captured entirely by the firm, making it all producer

surplus. The producer surplus is \$5 from the sale of the second good, \$3 from the sale of the third good, and \$1 from the sale of the fourth. Total producer surplus is the sum of these and equals \$16, which is the area above the MC curve and below the demand curve. Notice that the marginal revenue curve is the same as the demand curve, which means this perfect price-discriminating monopolist is producing at the point where marginal revenue equals marginal cost, four units.

Interestingly, the amount of output the firm produces is equal to the amount a perfectly competitive firm would produce, and there is no deadweight loss. All of the surplus that is possible to create in this market is created. The difference is, of course, that the firm captures the entire surplus for itself. So consumer surplus actually falls relative to a simple monopolist, but total surplus and producer surplus increase.

This is an ideal situation for a firm with market power, but does it actually happen in the real world? It is rare to see it in its purest, most perfect form, but some examples come close. Bargaining over price is one example. Sellers might not be able to tell the exact willingness to pay but can become skilled in making educated guesses. Consider the case of new car sales. When a customer walks into an auto showroom and is greeted by a salesperson, that salesperson is already making inferences about the customer's reservation price. Casual conversations about where the customer lives, where they work, and what their family is like are all potential clues. The haggling itself is another signal, as low-reservationprice individuals will likely haggle quite strenuously and high-reservation-price individuals might not haggle much at all. In the end, each customer walks out of the dealership paying a different price, where that price difference is related to the reservation price.

Another good example of first-degree price discrimination is higher education. Colleges and universities are some of the best price discriminators around. It is estimated that less than one-third of all US college students pay full tuition. Most students routinely fill out a form to apply for student financial aid, which reveals a lot about their family's financial situation

Calculus

To understand the firm's optimal output decision, we can start with the knowledge that a perfect price discriminator charges each customer their reservation price, or p=D(Q), where D(Q) is the inverse demand curve and Q is the firm's output. Since the firm is charging each customer their reservation price, their total revenue is the area under the demand curve up to the point of total output, or

$$rac{d\pi}{dQ}$$
= $D(Q)$ - $rac{dTC(Q)}{dQ}$ = 0
 $D(Q)$ = $MC(Q)$
 $TR(Q)$ = $\int_{0}^{Q}D(z)dz$

Profit is total revenue minus the total cost of producing Q units of output, so the firm's objective function is to maximize profit by choosing Q:

$$egin{aligned} & rac{d\pi}{dQ} = D(Q) - rac{dTC(Q)}{dQ} = ^0 \ & D(Q) = MC(Q) \ & rac{max \ \pi(Q)}{Q} = \int_0^Q D(z) dz \end{aligned}$$

The first-order condition that characterizes a maximum is

$$\frac{d\pi}{dQ}{=}D(Q){-}\frac{dTC(Q)}{dQ}{=}0$$
 or

$$D(Q) = MC(Q)$$

So the firm will choose the $m{Q}$, where the demand curve and the marginal cost curve intersect, which is the same as a perfectly competitive firm.

and therefore their reservation price or ability to pay. Through the use of grants, scholarships, and subsidized loans, each student is given a price of attending a college or university that is tailored to them.

16.3 GROUP PRICE OR THIRD-DEGREE PRICE DISCRIMINATION

Learning Objective 16.3: Describe third-degree price discrimination and its effect on profits.

In general, most firms with market power are unable to determine individual consumers' reservation prices and charge them individual prices. However, firms might know something about the average reservation prices of identifiable groups. For example, it is generally true that, on average, retired individuals have less income than prime working-age adults and are likely to have lower reservation prices across a number of goods, like admission to movie theaters. If purchases are in person, group membership can be determined through identification, such as a driver's license. This solves the identification problem, but the arbitrage problem remains. To maintain price differentials, firms must be able to prevent resale from members of the low-price group to members of the high-priced group. Often such resale is prevented naturally by transactions costs, the economic costs of buying and selling a good or service beyond the price itself. For instance, in the car dealership example, it would take time and effort to find a buyer for a car that was just purchased, there would be bureaucratic costs associated with switching the registration of the car, and in many states, sales tax would have to be paid for both transactions. Since this is a cumbersome and costly process, there is unlikely to be much arbitrage in the new car market, and differential pricing will be able to be sustained. In the case of movie theaters, however, it is not hard to imagine a group of enterprising kids who purchase youth tickets and then wait outside the theater and sell them to adults at a premium over the youth price but at a discount over the adult price. This is why most movie theaters have ticket sellers and ticket takers who inspect tickets as patrons enter the theater to be sure adults have adult tickets.

Calculus

To understand the multimarket monopolist's optimal output decisions in each market, consider the monopolist's optimization problem. If the firm's costs are common across markets, then we can write the total cost function as a function of the sum of the output for both markets, TC(Q1+Q2). Thus the profit maximization problem looks like this:

$$rac{max\pi(Q1,Q2)}{Q1,Q2} = \ TR_1(Q_1) + TR_2(Q_2) - TC(Q_1+Q_2)$$

The first-order conditions that characterize the optimal solution are the following:

$$\begin{split} \frac{\partial \pi}{\partial Q1} &= \frac{dTR_1}{dQ1} - \frac{dTRC}{dQ} \frac{\partial Q}{\partial Q1} = 0 \\ \frac{\partial \pi}{\partial Q_2} &= \frac{dTR_2}{dQ_2} - \frac{dTRC}{dQ} \frac{\partial Q}{\partial Q_2} = 0 \end{split}$$

Rearranging terms and noticing that the first term is the marginal revenue and the second term is marginal cost, we get

$$MR1=MC$$

To understand how group price discrimination works, consider the following example of book prices in the United States versus the United Kingdom. The book Steve Jobs was released in 2011 in both the United States and the United Kingdom. In the United States, the cover price of the book was \$30; in the United Kingdom, the cover price was £25, which at the time equaled \$40. The reason for the price differential was likely due to the demand for the book in the United States being quite different than the demand in the United Kingdom. To see this, suppose that the marginal cost of production was \$5 in both countries; the demand for the book in the United Kingdom was $Q^{UK}=75-p^{UK}$; and the demand for the book in the United States was $Q^{US}=110-2p^{US}$, where quantities are expressed in the thou-

sands. Publishing companies are monopolists in the publication of a specific copyrighted book and therefore have market power in the market for that book. They are also quite sophisticated, and we can

$$MR2=MC$$

or the simple monopolists solution in both markets.

safely assume they estimated the demand in both markets. They see that demand differs, and since the two markets are geographically distinct, it makes it possible to charge different prices to the two groups by charging different prices in the two markets. Arbitrage is possible, but the transaction costs associated with buying books in one market and shipping them to the other means that any attempts at arbitrage will probably be insignificant.

In each individual market or to each group, the firm acts as a simple monopolist: charging a single price to all consumers in the market or group. So to figure out the profit maximizing price and quantity for the two markets, we simply have to solve the monopolist's profit maximization problem. We start by solving for the inverse demand functions:

| Table 16.2a Inverse demand curve equations | | |
|--|------------------------------|--|
| UK market | US market | |
| $Q^{UK}=75-p^{UK}$ | $Q^{US}=110-2p^{US}$ | |
| $p^{UK}=75-Q^{UK}$ | $2p^{US}=110-Q^{US}$ | |
| | $p^{US}=55-rac{1}{2}Q^{US}$ | |

Because these are both linear demand curves, we know that the marginal revenue curves have the same vertical intercept as the inverse demand curves but have twice the slope. Thus the marginal revenue functions are the following:

| Table 16.2b Solving for marginal revenue | | |
|--|------------------------------|--|
| UK market | US market | |
| $p^{UK}=75-Q^{UK}$ | $p^{US}=55-rac{1}{2}Q^{US}$ | |
| $MR^{UK}=75-2Q^{UK}$ | $MR^{US}=55-Q^{US}$ | |

To find the profit maximizing price and quantity in each market, we have to apply the profit maximization rule, which says that the profit maximizing output level is reached when MR=MC:

| Table 16.2c Applying the profit maximization rule | | |
|---|-------------------|--|
| UK market | US market | |
| $MR^{UK}=MC^{UK}$ | $MR^{US}=MC^{US}$ | |
| $75-2Q^{UK}=5$ | $55-Q^{US}=5$ | |
| $70=2Q^{UK}$ | $50=Q^{US}$ | |
| $Q^{UK}=35$ | $Q^{US}=50$ | |

To find the price, we simply plug these quantities into the inverse demand functions:

| Table 16.2d Finding the profit maximizing price | | |
|---|----------------------------|--|
| UK market | US market | |
| $p^{UK}=75-Q^{UK}$ | $p^US=55-rac{1}{2}Q^{US}$ | |
| $p^{UK}=75-35$ | $p^{US}=55-rac{1}{2}50$ | |
| $p^{UK}=\$40$ | $p^{US}=55-25$ | |
| | $p^{US}=\$30$ | |

The profit maximizing price for the publisher is \$40 in the UK market and \$30 in the US market. Graphically, the solution is shown in figure **16.2**.

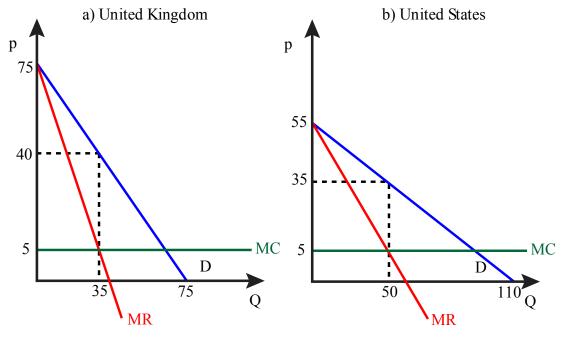


Figure 16.2 Group of third-degree price discrimination in book publishing

The firm's producer surplus is the difference between the price of the book and the marginal cost of producing the book multiplied by the number of books sold. The producer surplus in the United Kingdom is $PS^{UK}=(40-5)\times 35,000=\$1,225,000$, and the producer surplus in the United States is $PS^{US}=(30-5)\times 50,000=\$1,250,000$. Total producer surplus from the sales of the book in the two markets is \$2,475,000.

How much more producer surplus did the firm earn from practicing group price discrimination? We can answer this question by comparing this outcome to the outcome for a simple monopolist that charged the same price for the book in both markets. To figure out the profit maximizing price for the combined market, we have to sum the two demands together. Note that for prices above \$55, only UK consumers will purchase the book. So let's begin by assuming that the final price will be below \$55, and then we can check this assumption at the end.

Adding two demands together for prices below \$55 begins with adding the quantities together:

$$egin{aligned} Q^{UK} &= 75 - p^{UK} \ + Q^{US} &= 110 - 2p^{US} \ Q^{TOTAL} &= 185 - 3p \end{aligned}$$

Putting this into inverse demand format yields

$$p=61rac{2}{3}-rac{1}{3}Q^{TOTAL}$$
 ,

giving us a marginal revenue curve of

$$MR=61rac{2}{3}-rac{2}{3}Q^{TOTAL}.$$

Setting MR=MC yields

$$61rac{2}{3} - rac{2}{3}Q^{TOTAL} = 5$$

or

$$56rac{2}{3}=rac{2}{3}Q^{TOTAL}.$$

Solving this gives us

$$Q^{TOTAL}=85$$
 and $p=\$33.33$.

We see here that our assumption that the price would be less than \$55 is confirmed, so consumers in both markets will purchase the book.

The producer surplus in this combined market is thus

$$PS^{TOTAL} = (33.33 - 5) \times 85,000 = \$2,408,050$$

which is almost \$67,000 less than the price-discriminating monopolist. From this example, we can clearly see how offering different prices to the two sets of consumers can improve the outcomes for firms with market power.

16.4 QUANTITY DISCOUNTS, OR SECOND-DEGREE PRICE DISCRIMINATION

Learning Objective 16.4: Describe second-degree price discrimination and how it overcomes the identification problem.

A firm might know that their customers have different demands, but they are unable to tell anything about individual demands and are unable to divide them into identifiable groups. However, they might still be able to price discriminate by offering quantity discounts. The key to this type of price discriminate

nation is to offer pricing schemes so that the different types of consumers sort themselves by choosing different deals. Done well, firms can improve profits through the use of such a scheme, and the prevalence of volume discounts in markets suggests that this is a very effective profit increasing tool for firms with market power.

The effect of volume discounts is to entice high-demand consumers to purchase more of the good. This increases overall sales for the producer, which improves their profit. High demanders are better off as well since the opportunity to purchase the output at the normal price is available to them, but they choose the volume discount. This type of pricing has another name in economics, **non-linear pricing**, and is very common in consumer products. To understand the name, consider a linear relationship in the pricing of soft drinks. If a 10 oz. soda sells for \$1, a 15 oz. soda sells for \$1.50, and a 20 oz. soda sells for \$2, there is a linear relationship between the amount of the good and the price. In each case, the price per ounce is \$0.10. Typically, however, we see soda prices that are non-linear. A 10 oz. soda might be priced at \$1, but then a 15 oz. soda might be \$1.25 and a 20 oz. soda might be \$1.45, so the price per ounce declines as the volume increases.

Consider the example of a college convenience store that sells soft drinks from a soda fountain and has a monopoly on soft drink sales on campus. Suppose it knows that there are two types of consumers for its soft drinks: high and low. Low demanders are less thirsty and have an inverse demand curve of $p^L=.25-\frac{qL}{100}$, where q is measured in ounces of soda. High demanders are more thirsty and have

an inverse demand curve of $p^H=.35-rac{q^H}{100}.$ Though the manager of the store knows that these

two types of consumers exist, the store has no way of knowing which type a consumer is when they come into the store. The manager also knows that $\frac{1}{5}$ of the consumers on campus are of the high type.

The manager also knows that each ounce of soft drink costs \$0.05 to provide, or the marginal cost of an ounce of soft drink is \$0.05, and there are no fixed costs.

Let's begin the analysis by asking what the manager would do if she was able to both tell the two types apart and charge them different prices—in other words, act as a simple monopolist for both types. Because these are linear demands, the marginal revenue of both has the same vertical intercept but twice the slope, thus

$$MR^L=.25-rac{q^L}{50}$$
 and $MR^H=.35-rac{q^H}{50}\cdot$

Equating the MR to the MC yields the following set of results:

| Table 16.3 Comparison of maximum profit using non-linear pricing | | |
|--|---|--|
| Low demanders | High demanders | |
| $MR^L = .25 - rac{q^L}{50} = .05 = MC$ | $MR^{H} = .35 - rac{q^{H}}{50} = .05 = MC$ | |
| $Q^{ML}=10$ | $Q^{MH}=15$ | |
| $p^{ML}=\$0.15$ | $p^{MH}=\$0.20$ | |

In other words, the store would sell a 10 oz. soft drink to low demanders for \$1.50 and a 15 oz. soft drink to high demanders for \$3. The profit per customer is \$1.00 for the low demanders and \$2.25 for the high demanders. This is found by noticing that the per-ounce profit is the difference between the price and the marginal cost and then multiplying this by the amount of each type of purchase. Since $\frac{4}{5}$ of the cus-

tomers are low types and $\frac{1}{5}$ are high types, the average profit per customer is

$$(rac{4}{5}) imes (\$1.00) + (rac{1}{5}) imes (\$2.25) = \$1.35$$

If the stores are unable to tell the two types apart, they could charge the single monopolist price for the low demanders, since the high demanders will purchase at that price but the low demanders will not purchase at the high demanders' monopolist price. This would yield an average per-customer profit of \$1.00, as all customers would buy a 10 oz. soft drink for \$1.50. Alternatively, if they only offered the large drink, only high demanders would buy, and though they would make \$2.25 in profit on those sales, only $\frac{1}{5}$ of the customers will buy, so the average profit per customer would be \$0.45. It is also immediately clear that if the store offered both deals, no one would buy a 15 oz. soda at \$3, as for the same price, they could buy two 10 oz. soft drinks or a 20 oz. soft drink.

But if the store offered a volume discount on the soft drink, could they get the high demanders to voluntarily switch to a larger drink and make more money in the process? Consider the following deal: anyone can buy a 10 oz. soft drink for \$1.50 or a 20 oz. soda for \$2.40. This second offer is a volume discount, as the price per ounce has dropped from \$0.15 in the 10 oz. case to \$0.12 in the 20 oz. case. But would this work? Well, low types would only buy the 20 oz. if the price per ounce is \$0.05, so they would choose the 10 oz. soft drink. What would high types do? Well, a 10 oz. soft drink at a price of \$1.50 leaves the high type with \$1.50 of consumer surplus, as can be seen in figure 16.3 with the green area above the price and below the demand curve. A 20 oz. bottle of soft drink for \$2.40 leaves high demanders with \$2.60 in consumer surplus, or the green area plus the areas A and C. In other words, the large soft drink returns more value to the high-demand customers, so they will voluntarily choose the larger soft drink, while the low demanders will voluntarily choose the smaller soft drink.

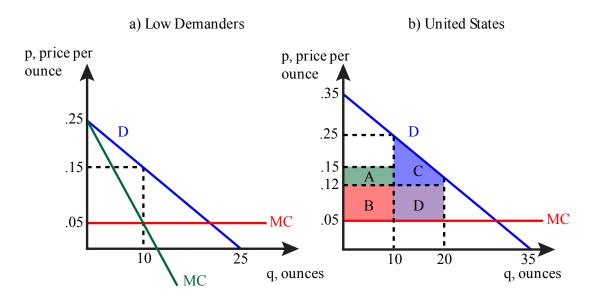


Figure 16.3 Volume discounts with two types of consumers

All that remains to be checked is whether it is better for the store to offer the two prices. If they only offered one, we have seen that it is best to offer the 10 oz. soft drink for \$1.50 and make \$1.00 in profit per consumer. With this pricing scheme, low demanders will buy the 10 oz. soda and high demanders will buy the large drink. The per-customer profit on the large drink is \$1.40, as can be seen in figure 16.3 with the areas B and D. So getting the 20 percent of consumers to voluntarily choose the large drink increases average profit by \$0.08. Graphically, this is represented in **panel b** of **figure 16.3**, where the store gains area D in profits and gives up area A. Since D is bigger than A, this represents an increase in profits for the store.

This example illustrates how firms with market power who serve customers with different demands can extract more surplus from the market by offering volume discounts, which the high-demand customers will choose voluntarily.

16.5 TWO-PART TARIFFS AND TIE-IN SALES

Learning Objective 16.5: Define two-part tariffs and tie-in sales and how they work as price discrimination mechanisms.

There are other ways that a firm with market power can practice second-degree price discrimination other than quantity discounts. One way is through the use of two-part pricing, and the other is through tie-in sales. In both cases, the key characteristic is the inability of the producer to identify consumers' willingness to pay either as individuals or in groups. Both pricing schemes rely on consumers voluntarily choosing a price based on their demands.

A **two-part tariff** is a pricing scheme where a consumer pays a lump-sum fee for the right to purchase an unlimited number of goods at a unit price. One example of a two-part tariff is a nightclub that charges a cover fee to enter the establishment, and once inside, patrons are able to purchase drinks at set prices. Another example is membership retailers like Costco and Sam's Club, which require patrons to purchase annual memberships to shop at the stores. Two-part tariffs are particularly relevant in the case of multiple purchases, as consumers who only purchase one unit are essentially paying a single price, but those that purchase more units are lowering their per-unit price as the one-time fee is divided across more units.

To understand how a two-part tariff works, we begin by assuming identical consumers. After examining the identical-consumer case, we turn to the case of two types of consumers, high demand and low demand, to understand how two-part tariffs can work as second-degree price discrimination mechanisms.

Two-Part Tariff with Identical Consumers

Suppose a monopolist knows the demand curve of each of its consumers and that its consumers all have identical demands. For example, suppose the only fitness club in a town knows that every single customer has exactly the same monthly inverse demand curve for visits to the club of $p=10-\frac{1}{2}q$

, where q is the individual's quantity of visits. This fitness club is considering using a two-part pricing scheme where it charges a monthly membership fee and a price per use. Furthermore, the club estimates its marginal cost each time a client uses the club at \$4. This includes the wear and tear on machines, cleaning, cost of towels and water in the locker room, and so on. Since the monopolist knows the demand curves of its customers, they can use the per-visit price to maximize consumer surplus and then use the monthly fee to extract the entire consumer surplus.

The fitness club's pricing strategy is illustrated in **figure 16.4**. By setting the per-use price equal to the marginal cost of \$4, consumers will choose to visit the fitness club sixteen times per month. The total consumer surplus generated from being able to visit the fitness club sixteen times in a month at a price of \$4 is \$48. So if the club charges a monthly membership fee of \$48 on top of a per-use price of \$4, consumers will be willing to pay it, as they get the benefit of paying \$48 to use the club at \$4 a time. The club is able to maximize and extract the entire surplus in the market, identical to a first-degree price discriminator.

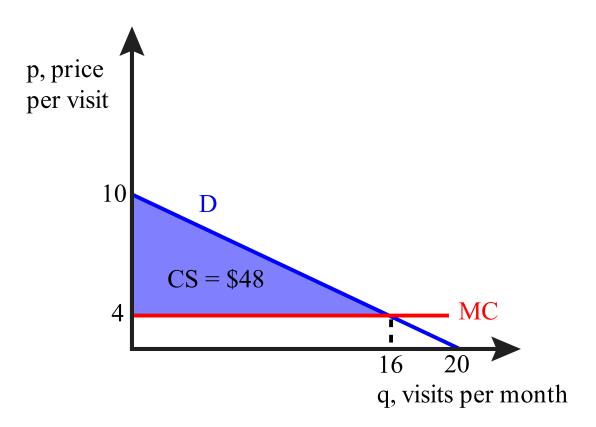


Figure 16.4 Two-part tariff with identical consumers

Note that this outcome extracts the maximum surplus possible from the market, and the quantity is the same as the perfectly competitive outcome. There is no possible way for a firm to do better than this. It is also a quite simple pricing mechanism but a very effective one.

Two-Part Pricing with Two Types of Customers

Now let's explore how a firm that knows it has different types of consumers but can't tell them apart can use two-part tariffs to price discriminate and improve profits. Let's return to our fitness club, but now let's assume that there are two types of customers: fitness nuts and casual exercisers. Fitness nuts have an inverse demand curve of $p^H=24-q^H$, while casual exercisers have an inverse demand curve that

is the same as the previous example: $p^L=10-rac{1}{2}q^L.$ How can the fitness club use a two-part tar-

iff to practice second-degree price discrimination? It can offer the same prices as in the previous example but with one further restriction; a monthly membership costs \$48, but this membership entitles the purchaser up to sixteen visits in a month for \$4 each. We know that the casual exercisers will choose to purchase this, as they would choose exactly sixteen visits and gain exactly \$48 in consumer surplus from consuming sixteen visits at \$4 each.

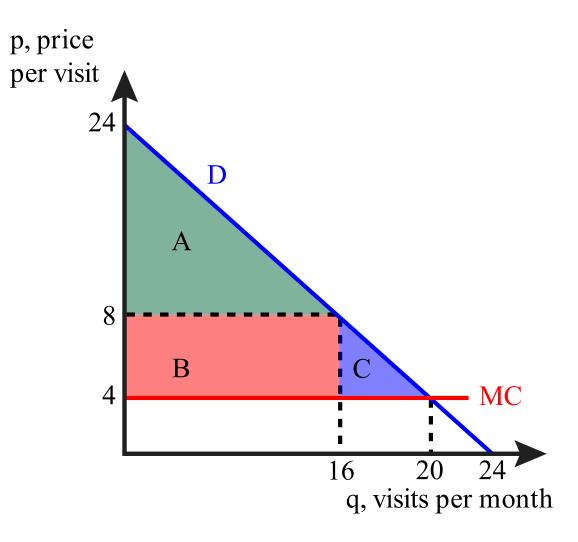


Figure 16.5 Two-part tariff for high demanders

But what about the fitness nuts whose demand curve is shown in **figure 16.5**? This deal, let's call it the silver membership—sixteen visits at \$4 each—would yield a total of \$192 in consumer surplus (areas A+B), \$48 of which would be paid as the monthly membership, netting \$144 in leftover consumer surplus that the fitness nuts enjoy. However, note that the fitness nuts would like to visit the club more than sixteen times in a month at the price of \$4; they would like to visit twenty times. If they were allowed to visit twenty times, they would get a total of \$200 in surplus (areas A+B+C). So the club could offer a gold membership, a package for more frequent visitors, in addition to the silver membership. If they offered a package that included twenty visits a month, how much could they charge for this enhanced membership? In order to get the fitness nuts to voluntarily choose the gold membership over the silver membership, they need to leave them with as much consumer surplus as the silver membership leaves: \$144. So \$200 - \$144 = \$56. If the club charged \$56 for the gold membership, the fitness nuts would voluntarily choose this package. What about casual exercisers? They would not visit more than sixteen times in a month, even if they had the right to, and they would not generate more than \$48 in consumer surplus, so a membership of \$56 is too expensive, and they would not choose it.

This pricing scheme is successful in getting the different types of consumers to self-select into different pricing schemes, but is it better for the club? The answer is yes. The club breaks even at every visit, since the price of each visit, \$4, is exactly equal to the marginal cost of the visit. So by offering gold member-

ships, they collect \$56 from types from whom they would otherwise have earned \$48. This \$8 difference is the improvement in profits for the club. Note that in this case, the gold membership represents a volume discount, as the average cost per visit for the silver members is \$7, while the average cost per visit for the gold members is \$6.80.

Now that we have seen how two-part tariffs can be used to increase firm profits and act as a type of price discrimination, let's consider the practice of tie-in sales.

Tie-In Sales

Tie-in sales refer to situations where the purchase of one item commits the consumer to buy another product as well. A very common example is ink-jet computer printers. The printers themselves are sold in quite competitive markets, but the printer requires that only the manufacturer's ink can be used in the printer, creating a situation where the firm has market power in the ink market. In many ways, such programs are very similar to two-part tariffs, where the price of the printer is like the fixed fee and the ink is the per-use price. However, in tie-in sales, it is the printer that is priced competitively and the ink for which a monopoly price is charged.

Other examples include razors and blades, automobiles and "genuine" parts required to keep the warranty valid, and so on.

16.6 BUNDLING, VERSIONING, AND HURDLES

Learning Objective 16.6: Define bundling, versioning, and hurdles and how each works to increase firm profits.

Selling more than one good together for a single price is called **bundling**. Firms use bundling as another pricing strategy to increase profit. **Pure bundling** is when the goods are only sold together at a single price, and **mixed bundling** is when goods are available separately at individual prices and together at a single price that is typically lower than the sum of the two individual prices. Bundling is an alternative pricing strategy that is similar to quantity discounts but is generally used in markets for goods where consumers don't generally purchase more than one unit of each at a single time, and therefore quantity discounts are not effective. Bundling does require that resale is preventable or impractical.

A good example of bundling is cable and satellite television. Most companies sell television channels in packages of channels, so, for example, if you are a sports fan that wants ESPN, you might be forced to choose a package of channels that includes the Home and Garden Network (HGN), which you might not value very highly. On the other hand, you might be very interested in home improvement and value the HGN channel very highly and have a low value for ESPN. By selling them together as a bundle, the cable or satellite television provider can improve its profits relative to selling them separately.

To see this, consider the following simple example of an economy in which there are two types of television watchers: the sports fans and the home improvers. We will assume that there are equal numbers of both in the economy and that there is a single cable company that provides the channels but that the cable provider cannot tell the two types of customers apart prior to a sale. We also assume that the cable company's marginal cost of an extra subscriber for each channel is zero.

Sports fans like to watch sports and are not very interested in home improvement. Home improvers like to watch home improvement shows and are not very interested in sports. Their reservation prices for a month of access to ESPN and HGN are given in **table 16.4**:

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Table 16.4 Reservation prices for television channels per month

| Consumer types | | | |
|----------------------------------|------|------|--|
| Channel Sports fan Home improver | | | |
| ESPN | \$30 | \$12 | |
| HGN | \$14 | \$36 | |
| Both | \$44 | \$48 | |

Given this information, what is the best pricing strategy for the cable monopolist? One strategy is to sell the channels separately à la carte style. If they did so, they could charge the monopoly price for each channel. In the case above, the profit maximizing price for ESPN is \$30. Since marginal cost is zero, the profit maximizing price is the same as the price that maximizes revenue. If the company charges \$30, the sports fan will purchase it, but the home improver will not, so total revenue is \$30 per customer pair. If instead the company charged \$12, both consumers would purchase the channel, so total revenue would be \$24. So \$30 is the profit maximizing price for ESPN. Similarly, if the cable company charged \$36 for HGN, only home improvers would buy, and the revenue per consumer pair would be \$36. If they charged \$14, both consumers would buy the channel, and they would generate \$28 per pair. In total, the maximum profit per consumer pair from selling the channels separately is \$30 + \$36, or \$66.

Now if they sold the two channels only as a bundle, what is the profit maximizing price for the bundle? If the cable company charged \$48 for the bundle, home improvers would buy, sports fans would not, and revenue per consumer pair would be \$48. If the cable company charged \$44 for the bundle, both types would buy, and revenues would be $\$44 \times 2$, or \$88. So clearly the profit maximizing price for the bundle is \$44.

Comparing the bundle revenues to the single-channel revenues, it is clear that bundling is a better choice for the company, as they earn \$88 per consumer pair when they bundle versus \$66 when they sell the channels separately. Why is this? By selling them separately, their incentive is to charge prices for individual channels and exclude the channels the consumer doesn't prefer. By bundling, the company both forces the consumer to purchase the other, less preferred channel and offers a substantial discount for the second channel. This gets consumers to buy twice as many channels as they would otherwise, which is good for the firm because, at a marginal cost of zero, any extra sales that bring in additional marginal revenue are profit enhancing.

But bundling does not always result in higher profits. Consider the same example with different reservation prices.

Table 16.5: Reservation prices for television channels per month

| Consumer Types | | | | |
|----------------------------------|------|------|--|--|
| Channel Sports fan Home improver | | | | |
| ESPN | \$30 | \$14 | | |
| HGN | \$16 | \$10 | | |
| Both | \$46 | \$24 | | |

In this example, the sports fan still has a higher reservation price for ESPN, and the home improver still has a higher reservation price for HGN, but now the sports fan has relatively high reservation prices for both, while the home improver has low reservation prices for both. Now, if they charge for the channels separately, the profit maximizing prices are \$30 for ESPN, which yields \$30 in revenue per pair because only the sports fan would purchase it, and \$10 for HGN, which yields \$20 in revenue per pair, for a total

of \$50 in revenue. The profit maximizing bundle price is \$24, which both consumers would pay, and they generate a total of \$48, or \$2 less than selling them separately.

What has changed in these two examples? In the former, the reservation prices are negatively correlated across the two types of customers: the sports fan has a higher reservation price for ESPN and a lower reservation price for HGN, and the opposite is true for the home improver. In the latter example, the reservation prices are positively correlated: the sports fan has higher reservation prices for both channels.

Another form of price discrimination is **versioning**: the selling of a slightly different version of a product for a different price that does not reflect cost differences. A common example of this is the sales of luxury versions of family sedans by major car companies. The Honda Accord, the Toyota Camry, and the Ford Fusion are all mid-sized family sedans. All three come in base models, with a standard set of features, and luxury versions, with additional features such as more luxurious interior materials, such as leather seats; more technological components, such as adaptive cruise control systems; and the like. If the price differential simply reflected the extra cost to the firm of these extra features, there would be no price discrimination. However, this is not the case; car companies charge a premium over additional costs. For this to be a profit maximizing strategy, it must be the case that customers with low-price elasticities self-select into the luxury versions because preference for luxury amenities and low-price elasticity are correlated. They pay a higher price than do customers with higher-price elasticities. As we saw in section 16.3, being able to charge the low-elasticity customers a higher price than high-elasticity customers is often a profit improving strategy.

Another price discrimination mechanism is through the use of **hurdles**: a non-monetary cost a consumer has to pay in order to qualify for a lower price. The most classic hurdle is the redeemable coupon. Consider a grocery store that prints a sheet of coupons and puts them in a flyer in the local newspaper or sends them in the mail. All customers of the store have a chance to use them, but many don't. Those that do pay a price to use them: the time and effort of cutting them, searching for the specific good for each coupon, and redeeming them at checkout. The price-discrimination mechanism is that high-elasticity customers are more likely to pay the cost of dealing with coupons, and at the same time, these are the very customers to whom the stores would like to offer a lower price.

Other examples of hurdles are early-bird dinner deals, mail-in rebates, matinee movie tickets, paper-back versions of popular books, and rush tickets for theater performances only available the night of the performance. In all cases, there is some cost to purchasing the product—having to arrive early to a restaurant or movie, not being able to be guaranteed a seat at a theater, having to wait to buy a book, having to fill out a rebate card and wait six to eight weeks for a check—that entitles to the person paying the cost to a lower price. This cost causes consumers to self-select into two groups, those that pay the cost to get a lower price and those that pay the higher price and avoid the cost.

16.7 POLICY EXAMPLE

SHOULD PUBLIC UNIVERSITIES CHARGE EVERYONE THE SAME PRICE?

Learning Objective 16.7: Explain how the use of price discrimination can be seen as a way for public universities to accomplish their mission.

US public universities, like the University of California at Berkeley, have a common foundational purpose: to provide a quality education for the students of the state in which they reside. Providing a quality education comes at a considerable cost, as universities are complex institutions that house, feed, and educate students. But is price discrimination antithetical to their mission? As non-profit entities, what

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motivates universities to charge different prices if profit is the motivation for most companies' price discrimination?

To understand the rationale behind the use of price discrimination, let's begin by thinking of a demand curve for a local public state university. There are a limited number of places the university can offer each year and a selection process, so let's think of the demand curve for accepted students, those that have been offered a spot. The demand curve for these admitted students is likely downward sloping, as there are probably only a few families that could potentially afford a high tuition, but as tuition declines more and more, families are able to and would choose to purchase a college education at the institution. There is also a competitive effect, as there are other colleges and universities competing for the same students, but let's deliberately ignore that to focus on the questions at hand. We will also assume the marginal cost of each student is constant. The key to understanding the university's situation is to think about what the excess revenues above marginal cost represent. As a not-for-profit institution, we can think of this as going toward paying the fixed costs of the school, much of which is represented by the tenured faculty and the research and teaching infrastructure, which we could loosely call the quality component. More or better professors, better labs, better classrooms, and so on both cost more and contribute to the quality of the education.

A university has a number of options when thinking about the price to charge for tuition. Because they can both charge a price to each individual and, by collecting detailed information on family finances, tailor that price to their ability to pay, they can overcome the two challenges to price discrimination—preventing arbitrage and acquiring information. So universities can engage in very sophisticated pricing strategies. But should they? One option is to charge a single price that allows them to break even by exactly covering their total costs. This solution is seen in **figure 16.6**. The tuition price, $P^{\rm TUITION}$, is such that at the quantity demanded at the price Q^{OP} , the total revenue equals the total cost. In this scenario, Q^{OP} students attend the school and all pay exactly the same price.

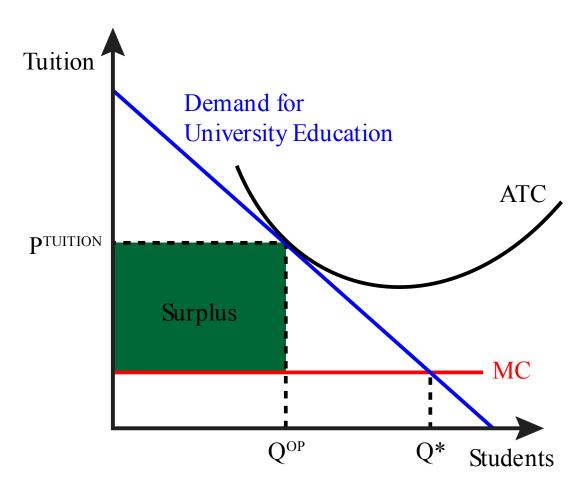


Figure 16.6 Universities charging a single price

If instead the university practices price discrimination, they can charge each student exactly their reservation price. This situation is illustrated in **figure 16.7**.

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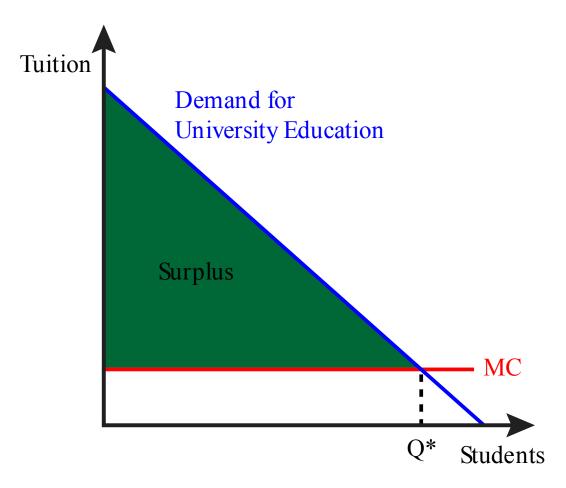


Figure 16.7 Universities practicing first-degree price discrimination

Because the university can charge individual prices, they will continue to offer tuition prices to all students whose reservation price is at least equal to marginal cost. This means that they will end up serving Q^* students. This is substantially more students than the single-price strategy and is also the socially optimal number of students. In this case, the university captures the entire area beneath the demand curve and above the marginal cost as producer surplus. This is also substantially more than the producer surplus in the one-price scenario and is money that the university can invest in improving the quality of the school.

By practicing very sophisticated price discrimination, the university comes close to the first-degree price discriminator's outcome, where the number of students is the socially optimal Q^* , but the school captures all the surplus for itself to cover fixed costs and invest in quality. So from an institutional level, we could argue that this is a good thing. What about for individual students? The answer depends on where on the demand curve the individual students lie. For wealthier students or those that otherwise had a very high reservation price, they are playing quite a bit more than they would with a single price. But for low-income or otherwise low-reservation-price students, with price discrimination, they can attend the university where otherwise they would have been shut out with a single price, and they pay a lower tuition than the single price.

EXPLORING THE POLICY QUESTION

1. Explain how high-income students might feel very differently about the price discrimina-

tion by state universities than low-income students.

- 2. Do you think that price discrimination is consistent with the mission of your school?
- 3. How do you feel about the price you pay for college? Is it fair?

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

16.1 Market Power and Price Discrimination

Learning Objective 16.1: Explain differentiated pricing and describe the three types of price discrimination.

16.2 Perfect or First-Degree Price Discrimination

Learning Objective 16.2: Describe first-degree price discrimination and the challenges that make it hard.

16.3 Group Price or Third-Degree Price Discrimination

Learning Objective 16.3: Describe third-degree price discrimination and its effect on profits.

16.4 Quantity Discounts, or Second-Degree Price Discrimination

Learning Objective 16.4: Describe second-degree price discrimination and how it overcomes the identification problem.

16.5 Two-Part Tariffs and Tie-In Sales

Learning Objective 16.5: Define two-part tariffs and tie-in sales and how they work as price discrimination mechanisms.

16.6 Bundling, Versioning, and Hurdles

Learning Objective 16.6: Define bundling, versioning, and hurdles and how each works to increase firm profits.

16.7 Policy Example

Should Public Universities Charge Everyone the Same Price?

<u>Learning Objective 16.7</u>: Explain how the use of price discrimination can be seen as a way for public universities to accomplish their mission.

LEARN: KEY TOPICS

Terms

Simple monopolists

Monopolists that are limited to a single price at which all the output they produce is sold.

Differentiated pricing

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Selling the same good or service for different prices to different consumers.

Price discrimination

The practice of charging different prices for the same good to different consumers.

Perfect price discrimination

A type of pricing strategy that charges every consumer a price equal to their willingness to pay, i.e., car dealerships, even though ultimately the final prices in this scenario are negoatiated.

First-degree price discrimination

See perfect price discrimination.

Group price discrimination

When firms charge different prices for the same good or service to different groups or different types of people, i.e., membership rates at a movie theatre.

Third-degree price discrimination

See group price discrimination.

Quantity discounts

When firms charge a lower price per unit to consumers who purchase larger amounts of the good, i.e., a grocery store sets a group of products as buy 10 spend a \$1, in which the consumer must select 10 products to ultimately pay \$10.

Second-degree price discrimination

See quantity discount.

Transactions costs

The economic costs of buying and selling a good or service beyond the price itself.

Non-linear pricing

In which a product is discounted based on its individual volume, i.e., soft drinks:

If a 10 oz. soda sells for \$1, a 15 oz. soda sells for \$1.50, and a 20 oz. soda sells for \$2, there is a linear relationship between the amount of the good and the price. In each case, the price per ounce is \$0.10. Typically, however, we see soda prices that are non-linear. A 10 oz. soda might be priced at \$1, but then a 15 oz. soda might be \$1.25 and a 20 oz. soda might be \$1.45, so the price per ounce declines as the volume increases.

Two-part tariff

A pricing scheme where a consumer pays a lump-sum fee for the right to purchase an unlimited number of goods at a unit price, i.e., retailers like Sam's Club and CostCo, which require an annual membership to shop at their store.

Tie-in sales

A situation where the purchase of one item commits the consumer to buy another product as well, i.e., razors and blades; printers and toner; a gaming system and games.

Bundling

Selling more than one good together for a single price, i.e., Buy One Get One Free; Dollar Shave Club.

Pure bundling

When the goods are only sold together at a single price: gift baskets; sample-size beauty products; salad kits (the specific portion of dressing, lettuce, etc. is only available bundled in that product).

Mixed bundling

When goods are available separately at individual prices and together at a single price that is typically lower than the sum of the two individual prices, i.e., cable channels. Different versions of channel bundles exist depending on preferences and willingness to pay, but channels can also be purchased a la carte.

Versioning

The selling of a slightly different version of a product for a different price that does not reflect cost differences, i.e., the "luxury" version of a car; collector's editions of video games/figures/etc.

Graphs

First-degree price discrimination

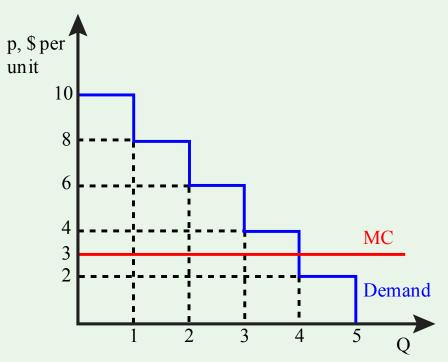


Figure 16.1 First-degree price discrimination

Group or third-degree price discrimination in book publishing

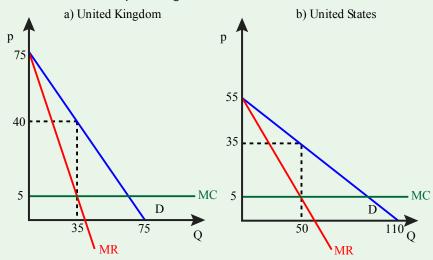


Figure 16.2 Group of third-degree price discrimination in book publishing

Volume discounts with two types of consumers

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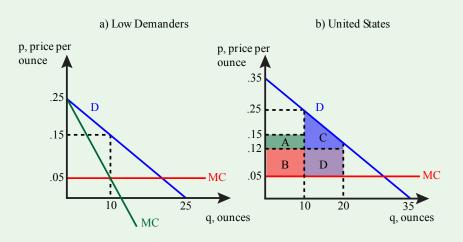


Figure 16.3 Volume discounts with two types of consumers

Two-part tariff with identical consumers

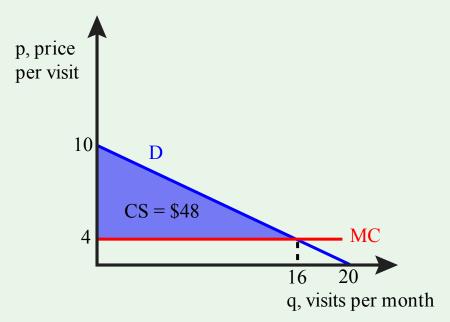


Figure 16.4 Two-part tariff with identical consumers

Two-part tariff for high demanders

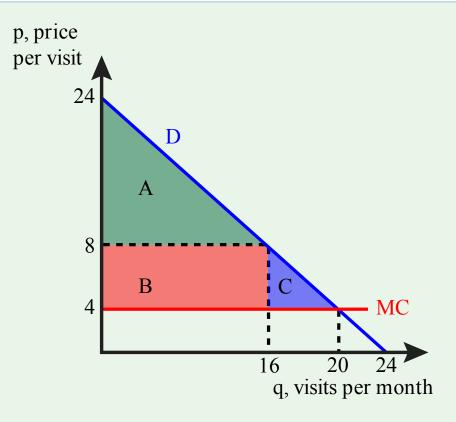


Figure 16.5 Two-part tariff for high demanders

Tables

Reservation prices for television channels per month: comparison

Table 16.4 Reservation prices for television channels per month; bundling as a good choice

| Consumer types | | | |
|----------------------------------|------|------|--|
| Channel Sports fan Home improver | | | |
| ESPN | \$30 | \$12 | |
| HGN | \$14 | \$36 | |
| Both | \$44 | \$48 | |

Table 16.5: Reservation prices for television channels per month; bundling as a bad choice

| Consumer Types | | | |
|----------------------------------|------|------|--|
| Channel Sports fan Home improver | | | |
| ESPN | \$30 | \$14 | |
| HGN | \$16 | \$10 | |
| Both | \$46 | \$24 | |

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CHAPTER 17

Game Theory

THE POLICY QUESTION

DO WE NEED TO REGULATE BANKS TO SAVE THEM FROM THEMSELVES?

In the real estate and banking crisis that caused the United States to fall into the worst recession since the Great Depression, banks were seen to have engaged in reckless and risky behavior that was seemingly against their self-interest. Part of the risky behavior was attributed to the relaxation of banking regulations, particularly those that separated commercial banks from investment banks. But the question of why banks would engage in self-destructive behavior in the first place is one that puzzles many observers who have a background in economics and knows that free markets often direct individual self-interested action toward the good of society.

One possible explanation for this disconnect is the possibility that the banking industry is much more strategic than policy makers understood. The strategic incentives to take risks could be a lot more powerful than generally appreciated. The nature of this strategic environment and the incentives it provides are essential to understand to be able to make appropriate and effective policies.

EXPLORING THE POLICY QUESTION

- 1. What are the strategic incentives for banks to take risks?
- 2. What policy solutions present themselves from this analysis?

LEARNING OBJECTIVES

17.1 What Is Game Theory?

<u>Learning Objective 17.1</u>: Describe game theory and the types of situations it describes.

17.2 Single Play Games

Learning Objective 17.2: Describe normal form games, and identify optimal strategies and equilibrium outcomes in such games.

17.3 Sequential Games

Learning Objective 17.3: Describe sequential move games, and explain how they are solved.

17.4 Repeated Games

<u>Learning Objective 17.4</u>: Describe repeated games and the difference between finitely repeated games and infinitely repeated games and their equilibrium.

17.5 Policy Example

Do We Need to Regulate Banks to Save Them from Themselves?

Learning Objective 17.5: Explain how game theory can be used to understand the banking collapse of 2008.

17.1 WHAT IS GAME THEORY?

Learning Objective 17.1: Describe game theory and the types of situations it describes.

Until this chapter, we have studied economic decision-making in situations where an agent's payoff is based on their actions alone. In other words, the payoff to an agent's actions is known, and the trick is to figure out how to get the highest payoff. But there are many situations in which the payoffs to an agent's actions are determined in part by the actions of other agents. Consider this simple example: On Saturday, you know there are a number of parties happening in and around your school. How much you will enjoy attending any one party is in large part determined by how many of your friends will be there. In other words, your payoff is a function of not only your decision about which party to attend but also the decisions of your friends. We call these types of interactions **strategic interactions**, where agents must anticipate the actions of others when making decisions, and we use game theory to model them so that we can think about the outcomes of these interactions just like we think about outcomes in markets without strategic interaction, like the price and quantity outcome in a product market. **Game theory** is the study of strategic interactions among economic agents.

Game theory is extremely useful because it allows us to anticipate the behavior of economic agents within a game and the outcomes of strategic games. Game theory gets its name from actual games. Checkers and chess are strategic games where two players interact, and the outcome of the game is determined by the actions of both players. In economics, game theory is particularly useful in understanding imperfectly competitive markets like oligopoly—the subject of the next chapter—because the price and output decisions of one firm affect the demand and therefore profit function of the other firms. But before we can study oligopoly markets, we must first understand games and how to analyze them. In this chapter, we will consider only **non-cooperative games**, games where the players are not able to negotiate and make binding agreements within the game. An example of a cooperative game might be one where two poker players agree to share winnings no matter who actually wins; as a result, their strategies are based on how best to maximize the joint expected payoff, not individual payoffs.

All games have three basic elements: players, strategies, and payoffs. The **players** of the game are the agents actively participating in the game and who will experience outcomes based on the play of all players. The **strategies** are all the possible strategic choices available to each player; they can be the same for all players or different for each player. The **payoffs** are the outcomes associated with every possible strategic combination for each player. Any complete description of a game must include these three elements. In the games that we will study in this chapter, we will assume that each player's goal is to maximize their individual payoff, which is consistent with the rational utility maximizing agent that is the foundation of modern economic theory.

We begin by separating games into two basic types: simultaneous games and sequential games. **Simultaneous games** are games in which players take strategic actions at the same time without knowing what move the other has chosen. A good example of this type of game is the matching coins game where two players each have a coin and choose which side to face up. They then reveal their choices simultaneously, and if they match, one player gets to keep both coins, and if they don't match, the other player keeps both coins. **Sequential games** are games where players take turns and move consecutively. Checkers, chess, and go are all good examples of sequential games. One player observes the move of the other player and then makes their play and so on.

Games can also be single shot or repeated. **Single-shot** games are played once, and then the game is over. **Repeated games** are simultaneous move games played repeatedly by the same players. A single-shot game might be a game of rock, paper, scissors played once to determine who gets to sit in the front seat of a car. A repeated game might be repeated plays of rock, paper, scissors, with the first player to win five times getting the right to sit in the front seat of a car.

Games can become very complicated when all players do not know all the information about the game. For the purposes of this chapter, we will assume **common knowledge**. Common knowledge is when the players know all about the game—the players, the strategies, and the payoffs—and know that the other players know, that the other players know, and so on ad infinitum. In simpler terms, all participants know everything.

17.2 SINGLE PLAY GAMES

Learning Objective 17.2: Describe normal form games, and identify optimal strategies and equilibrium outcomes in such games.

The most basic of games is the simultaneous, single play game. We can represent such a game with a **payoff matrix**: a table that lists the players of the game, their strategies, and the payoffs associated with every possible strategy combination. We call games that can be represented with a payoff matrix **normal form games**.

Let's start with an example of a game between two friends, Lena and Sven, who are competing to be the top student in a class. They have a final exam approaching, and they are deciding whether they should be cooperative and share notes or be uncooperative and keep their notes to themselves. They won't see each other at the end of the day, so they each have to decide whether to leave notes for each other without knowing what the other one has done. If they both share notes, they both will get perfect scores. Their teacher gives a ten-point bonus to the top exam score, but only if there is one exam better than the rest, so if they both get top score, there is no bonus, and they both get 100 on their exams. If they both don't share, they won't do as well, and they will both receive a 95 on their exams. However, if one shares and the other doesn't, the one who shares will not benefit from the other's notes and will only get a 90, and the one who doesn't share will benefit from the other's notes and get the top score and the bonus for a score of 110.

All of these facts are expressed in the payoff matrix in **table 17.1**. Since this is a single-shot, simultaneous game, it is a normal form game, and we can use a payoff matrix to describe it. There are two players: Lena and Sven. There are two strategies available to each player. We will assume common knowledge—they both know all this information about the game, and they know that the other knows it, and they know that the other knows that they know it, and so on.

Table 17.1 The valedictorian game

| Note Strategy | Sven's Payoff | Lena's Payoff |
|---------------|---------------|---------------|
| Sven shares | 90 | 110 |
| Lena shares | 110 | 90 |
| Neither share | 95 | 95 |
| Both share | 100 | 100 |

The payoff matrix offers a complete description of the game because it lists the three elements: players, strategies, and payoffs.

It is now time to think about individual strategy choices. We will start by examining the difference between dominant and dominated strategies. A **dominant strategy** is a strategy for which the payoffs are always greater than any other strategy no matter what the opponent does. A **dominated strategy** is a strategy for which the payoffs are always lower than any other strategy no matter what the opponent does. Predicting behavior in games is achieved by understanding each rational player's optimal strategy, the one that leads to the highest payoff. Sometimes the optimal strategy depends on the opponent's strategy choice, but in the case of a dominant strategy, it does not, and so it follows that a rational player will always play a dominant strategy if one is available to them. It also follows that a rational player will never play a dominated strategy. So we now have our first two principles that can, in certain games, lead to a prediction about the outcome.

Let's look at the valedictorian game in **table 17.1**. Notice that for Lena, she gets a higher payoff if she doesn't share her notes no matter what Sven does. If Sven shares his notes, she gets 110 if she doesn't share rather than 100 if she does. If Sven doesn't share his notes, she gets 95 if she doesn't share and 90 if she does. It makes sense then that she will never share her notes. Don't share is a dominant strategy, so she will play it. Share is a dominated strategy, so she will not play it. The same is true for Sven, as the payoffs in this game happen to be completely symmetrical, though they need not be in games. We can predict that both players will choose to play their dominant strategies and that the outcome of the game will be don't share, don't share—Lena chooses don't share, and Sven chooses don't share—and they both get 95.

This outcome is known as a **dominant strategy equilibrium** (DSE), an equilibrium where each player plays their dominant strategy. This is a very intuitive equilibrium concept and is the one used in situations where all players have a dominant strategy. Unfortunately, many, or even most, games do not have the feature that every player has a dominant strategy. Let's examine the DSE in this game. The most striking feature of this outcome is that there is another outcome that both players would voluntarily switch to: share, share. This outcome delivers 100 to each player and is therefore more efficient in the Pareto sense—there is another outcome where you could make one person better off without hurting anyone else. Games with this feature are known as prisoner's dilemma games—the name comes from a classic game of cops and robbers, but the general usage is for games that have this Pareto-suboptimal feature.

Why do we get this suboptimal result? It comes from the fact that each agent is purely self-interested; all they care about is maximizing their own payoffs, and if they think the other player is going to play share, their best play is to not share. What is particularly interesting about this result is that it overturns the first welfare theorem of economics that says that a competitive equilibrium is Pareto efficient. The difference is the strategic nature of the interactions in the game. Here we have much of the same conditions of a competitive market, but because of the strategic nature of the game, one player's actions affect the other players' payoffs.

What if a game lacked dominant strategies? Let's go back to the example of the last section where you are thinking about which party to attend because you want to meet up with friends. Let's simplify the example by saying that there are two friends, Malia and Caitlin, who both have been invited to two parties, one sponsored by the college international club and another sponsored by the college debate club. Neither of them has a particular preference about which party they want to go to, but they definitely want to see each other and so want to end up at the same party. They talked earlier in the week, so they know that each is considering the two parties and how much each of them likes the two parties, so there is common knowledge. The problem is that Caitlin's mobile phone battery has run out of charge, and they can't communicate. When asked how much they would enjoy the parties, Caitlin and Malia gave similar answers, and we will represent them as payoffs in the payoff matrix in **table 17.2**.

Table 17.2 The party game, version 1

| | Table 17.2 The par | Malia | | |
|----------|-------------------------|-------------------------|------------------|--|
| | | International Club (IC) | Debate Club (DC) | |
| Caitlin | International Club (IC) | C: 10; M: 10; | C: 2; M: 2 | |
| Caltilli | Debate Club (DC) | C: 2; M: 2 | C: 10; M: 10; | |

This matrix shows Caitlin's strategies on the left in a column and Malia's strategies in a row on top. Each of them has exactly two strategies: international club and debate club. For each, their payoffs are shown in the boxes that correspond to each strategy pair. For example, in the boxes for international club, the payoffs are 10 and 10. The first payoff corresponds to Caitlin, and the second corresponds to Malia.

We now have to determine each player's **best response function**: one player's optimal strategy choice for every possible strategy choice of the other player. For Caitlin, her best response function is the following:

Play IC if Malia plays IC.

Play **DC** if Malia plays **DC**.

For Malia, her best response function looks similar:

Play IC if Caitlin plays IC.

Play **DC** if Caitlin plays **DC**.

Since the best response changes for both players depending on the strategy choice of the other player, we know immediately that neither one has a dominant strategy. What then? How do we think about the outcome of the game? The solution concept most commonly used in game theory is the Nash equilibrium concept. A **Nash equilibrium** is an outcome where, given the strategy choices of the other players, no individual player can obtain a higher payoff by altering their strategy choice. An equivalent way to think about Nash equilibrium is that it is an outcome of a game where all players are simultaneously playing a best response to the others' strategy choices. The equilibrium is intuitive if, when placed in a certain outcome, no player wishes to unilaterally deviate from it, which means equilibrium is achieved—there are no forces within the game that would cause the outcome to change.

In the party game above, there are two outcomes where the best responses correspond: both players choosing IC and both players choosing DC. If Caitlin shows up at the international club party and finds Malia there, she will not want to leave Malia there and go to the debate club party. Similarly, if Malia shows up at the international club party and finds Caitlin there, she will not want to leave Caitlin there and go to the debate club party. So the outcome (IC, IC)—which describes Caitlin's choice and Malia's choice—is a Nash equilibrium. The outcome (DC, DC) is also a Nash equilibrium for the same reason.

This example illustrates the strengths and weaknesses of the Nash equilibrium concept. Intuitively, if they show up at the same party, both women would be content, and neither one would want to leave to the other party if the other is staying. However, there is nothing in the Nash equilibrium concept that gives us guidance as to predicting at which party the women will end up. In general, a normal form game can have zero, one, or multiple Nash equilibriums.

Consider this different version of the party game, where Caitlin really doesn't want to go to the international club party, so much so that she prefers attending the debate club party without Malia to attending the international club party with Malia.

Table 17.3 The party game, version 2

| | | Malia | | |
|---------|-------------------------|-------------------------|------------------|--|
| | | International Club (IC) | Debate Club (DC) | |
| Caitlin | International Club (IC) | C: 1; M: 10; | C: 1; M: 2 | |
| Caltiin | Debate Club (DC) | C: 5; M: 2 | C: 15; M: 10; | |

Now DC is a dominant strategy for Caitlin. Malia knows Caitlin does not like the international club party and will correctly surmise that she will attend the debate club party no matter what. So both Caitlin and Malia will go to the debate club party, and (DC, DC) is the only Nash equilibrium. In this case, the Nash equilibrium concept is satisfying: it gives a clear prediction of the unique outcome of the game and intuitively makes sense.

Another possibility is a game that has no Nash equilibrium. Consider the game matching pennies. In this game, two players, Ahmed and Naveen, each have a penny. They decide which side of the penny to have facing up and cover the penny until they are both revealed simultaneously. By agreement, if the pennies match, Ahmed gets to keep both, and if the two pennies don't match, Naveen keeps both. The players, strategies, and payoffs are given in the payoff matrix in **table 17.4**.

Table 17.4 The matching coin game

| Round | Ahmed's Play | Naveen's Play | Results |
|---------|--------------|---------------|-------------------------|
| Round 1 | Heads | Tails | Ahmed: -1 Naveen: +1 |
| Round 2 | Heads | Heads | Ahmed: +1 Naveen: -1 |
| Round 3 | Tails | Tails | Ahmed: +1 Naveen: -1 |
| Round 4 | Tails | Heads | Ahmed: -1 Naveen: +1 |

Ahmed's best response function is to play heads if Naveen plays heads and to play tails if Naveen plays tails. Naveen's best response is to play tails if Ahmed plays heads and to play heads if Ahmed plays tails. As you can clearly see, there is no correspondence of best response functions, no outcome of the game in which a player would want to unilaterally deviate, and thus no Nash equilibrium. The outcome of this game is unpredictable, and no outcome creates contentment for both players.

Finding the Nash equilibrium in normal form games is made relatively easy by following a simple technique that identifies the best response functions on the payoff matrix itself. To do so, simply underline the maximum payoff for a given opponent's strategy. Consider the example below.

Table 17.5 The location game, version 1

| | | Pat | | |
|-------|--------|--------------|--------------|--------------|
| | | Left | Center | Right |
| | Up | C: 65, P: 44 | C: 29, P: 38 | C: 44, P: 29 |
| Chris | Middle | C: 53; P: 41 | C: 35, P: 31 | C: 19, P: 56 |
| | Down | C: 30, P: 57 | C: 41, P: 63 | C: 72, P: 27 |

For Chris, if Pat plays left, the maximum payoff is 65, which comes from playing up, so let's underline 65. If Pat plays left, Chris should play up. Moving along the columns, we find that Chris should play down if Pat plays center, and Chris should play down again if Pat plays right. Switching perspective, if Chris plays up, Pat gets a maximum payoff from playing left, so we underline Pat's payoff, 44, in that box. Continuing on, if Chris plays middle, Pat should play right, and if Chris plays down, Pat should play center.

So now that we have identified each player's best response functions, all that remains is to look for outcomes where the best response functions correspond. Such outcomes are those where both payoffs are underlined. In this game, the two Nash equilibriums are (up, left) and (down, center).

If we change the payoffs in the game to what is shown below, notice that each player has a dominant strategy, as seen by the three underlines all in the row "Down" for Chris and three underlines all in the column "Center" for Pat. Down is always the best strategy choice for Chris no matter what Pat chooses, and center is always the right strategic choice for Pat no matter what Chris chooses.

Table 17.6 The location game, version 2

| | | Pat | | |
|-------|--------|--------------|--------------|--------------|
| | | Left | Center | Right |
| | Up | C: 30, P: 41 | C: 29, P: 44 | C: 44, P: 24 |
| Chris | Middle | C: 53; P: 33 | C: 35, P: 56 | C: 19, P: 39 |
| | Down | C: 65, P: 57 | C: 41, P: 63 | C: 72, P: 27 |

Note also that the dominant strategy equilibrium (down, center) also fulfills the requirements of a Nash equilibrium. This will always be true of dominant strategy equilibriums: all dominant strategy equilibriums are Nash equilibriums. From the example above, however, we know the reverse is not true: not all Nash equilibriums are dominant strategy equilibriums. So dominant strategy equilibriums are a subset of Nash equilibriums, or to put it in another way, the Nash equilibrium is a more general concept than the dominant strategy equilibrium.

Mixed Strategies

So far we have concentrated on **pure strategies** where a player chooses a particular strategy with complete certainty. We now turn our attention to **mixed strategies**, where a player randomizes across strategies according to a set of probabilities they choose. For an example of a **mixed strategy**, let's return to the matching pennies game in **table 17.4**.

As was noted before and as we can see by using the underline strategy to illustrate best responses, there is no Nash equilibrium of this game in pure strategies. What about mixed strategies? A mixed strategy is a strategy itself; for example, Ahmed might decide that he will play heads 75 percent of the time and tails 25 percent of the time. What is Naveen's best response to this strategy? Well if Naveen plays tails with certainty, he will win 75 percent of the time. Ahmed's best response to Naveen playing tails is to play tails with certainty, so Ahmed's mixed strategy is not a Nash equilibrium strategy. How about

Ahmed choosing a mixed strategy of playing heads and tails, each with a 50 percent chance—simply flipping the coin—can this be a Nash equilibrium strategy? The answer is yes, which is evident when we think of Naveen's best response to this mixed strategy. Naveen can play either heads or tails with certainty or the same mixed strategy with equal results—he can expect to win half the time. We know that the pure strategies have the best responses as given in the matrix above, so only the mixed strategy is a Nash equilibrium. If Ahmed decides to flip his coin, Naveen's best response is to flip his too. And if Naveen is flipping his coin, Ahmed's best response is to do the same.

So this game, which did not have a Nash equilibrium in pure strategies, does have a Nash equilibrium in mixed strategies. Both players randomize over their two strategy choices with probabilities .5 and .5.

17.3 SEQUENTIAL GAMES

Learning Objective 17.3: Describe sequential move games, and explain how they are solved.

There are many situations where players of a game move sequentially. Checkers is such a game: one player moves, the other player observes the move and then responds with their own move, and so on. **Sequential move games** are games where players take turns making their strategic choices: one player observes their opponent's choice prior to making their own strategic choice. We describe these games by drawing a **game tree**, a diagram that describes the players, their turns, their choices at every turn, and the payoffs for every possible set of strategy choices. We have another name for this description of sequential games: **extensive form games**.

Consider a game where two Indian food carts located next to each other are competing for many of the same customers for their tikka masala. The first cart, called Ashok's, opens first and sets its price; the second cart, called Tridip's, opens second and sets its price after observing the price set by Ashok's. To keep it simple, let's suppose there are three prices possible for both carts: high, medium, low.

The extensive form, or game tree, representation of this game is given in **figure 17.1**. The game tree describes all the principal elements of the game: the players, the strategies, and the payoffs. The players are described at each decision node of the game, each place where a player might potentially have to choose a strategy. From each node, branches extend, representing the strategy choices of a player. At the end of the final set of branches are the payoffs for every possible outcome of the game. This is the complete description of the game. There are also subgames within the full game. Subgames are all the subsequent strategy decisions that follow from one particular node.

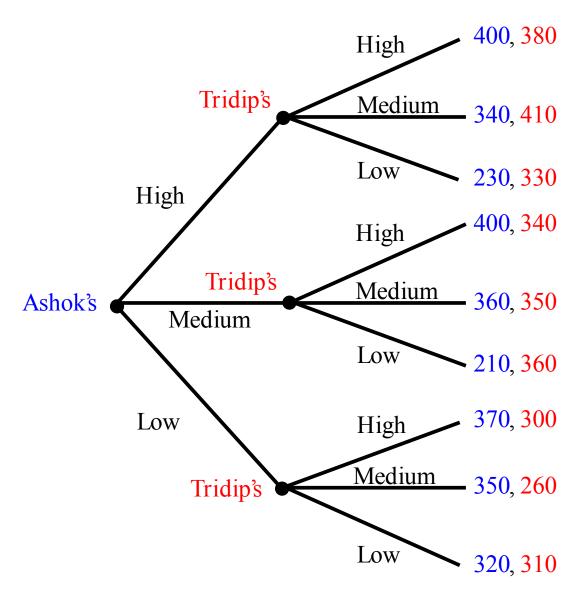


Figure 17.1 The curry pricing game

In this game, Ashok's is at the first decision node, so they get to move first. Tridip's is at the second set of decision nodes, so they move second. How will the game resolve itself? To determine the outcome, it is necessary to use backward induction: to start at the last play of the game and determine what the player with the last turn of the game will do in each situation and then, given this deduction, determine what the payer with the second-to-last turn will do at that turn and continue this way until the first turn is reached. Using backward induction leads to the subgame perfect Nash equilibrium of the game. The **subgame perfect Nash equilibrium** (SPNE) is the solution in which every player, at every turn of the game, is playing an individually optimal strategy.

For the curry pricing game illustrated in figure 17.1, the SPNE is found by first determining what Tridip's will do for each possible play by Ashok's. Tridip's is only concerned with his payoffs in red and will play medium if Ashok's plays high and thus will get 410, will play low if Ashok's plays medium and will get 360, and will play low if Ashok's plays low and will get 310. Because of common knowledge, Ashok's knows this as well and so has only three possible outcomes. Ashok's knows that if they play high, Tridip's will play medium, and Ashok's will get 340; if they play medium, Tridip's will play low, and Ashok's will get

210; and if they play low, Tridip's will play low, and Ashok's will get 320. Since 340 is the best of the possible outcomes, Ashok's will pick high. Since Ashok's picks high, Tridip's will pick medium, and the game ends.

Backward induction will always lead to the SPNE of a sequential game.

Credible and Non-credible Threats

Let's consider a famous game where there is an established "incumbent" firm in a market and another entrepreneur who is thinking of entering the market and competing with the incumbent, who we will call the "potential entrant." Suppose, for example, that there is just one pizza restaurant in a commercial district just off a university campus that sells pizza slices to the students of the university, let's call it Gino's. Since they face no direct competition, they can sell a slice of pizza for \$3, and they make \$400 a day in revenue. But there is a pizza maker named Vito who is considering entering the market by setting up a pizza shop in an empty storefront just down the street from Gino's. When facing the potential arrival of Vito's pizza restaurant, Gino has two choices: accommodate Vito by keeping prices higher (say, \$2) or fighting Vito by selling his slices below cost in the hope of preventing Vito from opening. The game and the payoffs are given below in the normal form game in **Table 17.7**.

In **Table 17.8**, we see that if we follow the underlining strategy to identify the best responses, this game has two Nash equilibriums: (accommodate, enter) and (fight, don't enter). Note that for Gino, both accommodate and fight result in the same payoff if Vito chooses don't enter, so we underline both—either one is equally a best response.

Table 17.7 The market entry game

| | | Vito's (Potential Entrant) | |
|-------------|-------------|----------------------------|---------------|
| | | Enter | Don't Enter |
| Gino's | Accommodate | G: 200; V: 300; | G: 400; V: 0 |
| (Incumbent) | Fight | G: 100; M: 200 | G: 400; M: 0; |

Table 17.8 Nash equilibrium in the market entry game

| | | Vito's (Potential Entrant) | |
|-------------|-------------|----------------------------|-----------------------|
| | | Enter | Don't Enter |
| Gino's | Accommodate | G: 200; V: <u>300</u> ; | G: <u>400</u> ; V: 0 |
| (Incumbent) | Fight | G: 100; M: 200 | G: <u>400</u> ; M: 0; |

But there is something unsatisfying about the second Nash equilibrium—since this is a simultaneous game, both players are picking their strategies simultaneously. Thus Gino is picking fight if Vito does not enter, and so Vito's best choice is not to enter. But would Vito really believe that Gino would fight if he entered? Probably not. We call this a non-credible threat: a strategic choice to dissuade a rival that is against the best interest of the player and therefore not rational.

A better description of this game is therefore a sequential one, where Vito first chooses to open a pizza restaurant and Gino has to decide how to respond.

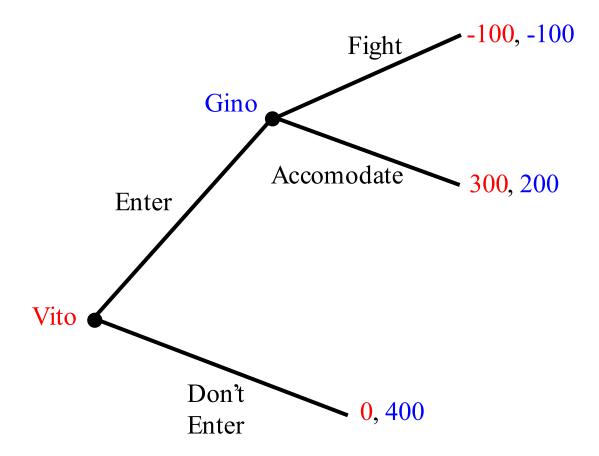


Figure 17.2 The sequential market entry game

In this version of the game, if Vito decides not to enter, the game ends, and the payoffs are \$0 for Vito and \$400 for Gino. If Vito decides to enter, then Gino can either fight and get \$–100 or accommodate and get \$200. Clearly, the only individually rational thing for Gino to do if Vito enters is to accommodate, and since Vito knows this, he will enter.

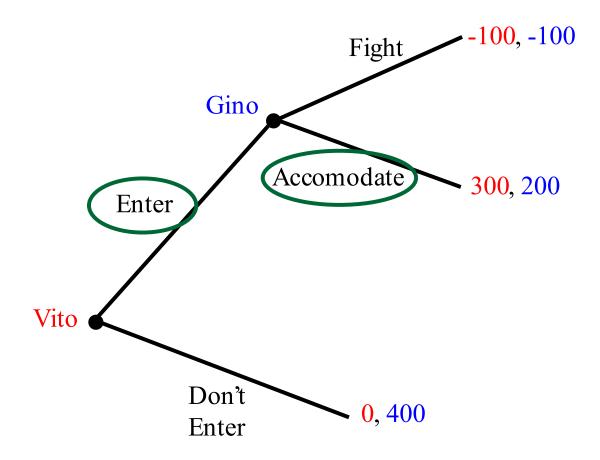


Figure 17.3 The squential market entry game [latex]SPNE[/latex]

The SPNE of this game is (enter, accommodate). What this version of the game does is eliminate the equilibrium based on a non-credible threat. Vito knows that if he decides to open up a pizza shop, it is irrational for Gino to fight because Gino will make himself worse off. Since Vito knows that Gino will accommodate, the best decision for Vito is to open his restaurant.

17.4 REPEATED GAMES

Learning Objective 17.4: Describe repeated games and the difference between finitely repeated games and infinitely repeated games and their equilibrium.

Any game can be played more than once to create a larger game. For example, the game rock, paper, scissors, where two players simultaneously use their hands to form the shape of a rock, a piece of paper, or scissors can be played just once or can be repeated multiple times—for example, playing "best of three," where the winner is the first player to win two rounds of the game. This is a normal form game in each round but a larger game when taken as a whole. This raises the possibility that a larger strategy could be employed—for example, one contingent on the choice of the opponent in the last round.

Let's return to the valedictorian game from <u>section 17.2</u>. Recall that this game was a prisoner's dilemma; because of individual incentives, they find themselves in a collectively suboptimal outcome. In other words, there is an outcome that they both prefer, but they fail to reach it because of the individual strategic incentive to try to do better for themselves. But if the same game was repeated more than once over the course of the school year, it is quite reasonable to ask if such repetition would lead the players to a different outcome. If the players know they will face the same situation again, will they be more inclined to cooperate and reach a mutually beneficial outcome?

Finitely Repeated Games

If we played the valedictorian game twice, then the strategies for each player would entail their strategy choices for each round of the game. In other words, a "strategy" for a repeated game is the complete set of strategic choices for every round of the game. So let's ask if playing the valedictorian game twice would alter the outcome in an individual round. Suppose, for example, the two talked before the game and acknowledged that they would both be better off cooperating and sharing. In the repeated game, is cooperation ever a Nash equilibrium strategy?

To answer this question, we have to think about how to solve the game. Since this game is repeated a finite number of times, in our case two, it has a final round, and similar to a sequential game, the appropriate method of solving the game is through backward induction to find the subgame perfect Nash equilibrium. In repeated games, at each round, the subsequent games are a subgame of the overall game. So in our case, the second and final round of the game is a subgame. So to solve the game, we have to first think about the outcome of the final round. Well, this final play of the game is the simple normal form game we have already solved, a single-shot, simultaneous play game with one Nash equilibrium: (don't share, don't share).

Now that we know what will happen in the final round of the game, we have to ask ourselves, What is the Nash equilibrium strategy in the first round of play? Since they both know that in the final round of play, the only outcome is for both to not share, they also know that there is no reason to share in the first round either. Why? Well, even if they agree to share, when push comes to shove, not sharing is better individually, and since not sharing is going to happen in the final round anyway, there is no way to create an incentive to share in the first round through a final round punishment mechanism. In essence, after the last period is revealed to be a single-shot prisoner's dilemma game, the second-to-last period becomes a single-shot prisoner's dilemma game as well because there is nothing in the last round that can alter the incentives in the second-to-last round, so the game is identical.

In fact, as long as there is a final round, it doesn't matter how many times we repeat this game; because of backward induction, it simply becomes a series of single-shot games with the Nash equilibrium strategies being played every time.

Infinitely Repeated Games

Things change when normal form games are repeated infinitely because there is no final round, and thus backward induction does not work; there is nowhere to work backward from. This aspect of the games allows space for reward and punishment strategies that might create incentives under which cooperation becomes a Nash equilibrium.

To see this, let's alter the scenario of our valedictorian game. Suppose that Lena and Sven are now adults in the workplace, and they work together in a company where their pay is based partly on their performance on a monthly aptitude test. For simplicity, we'll assume that their payoffs are the same as in the valedictorian game, but this time, they represent cash bonuses. The key here is that they foresee working together for as long as they can imagine. In other words, they each perceive the possibility that they will keep playing this game for an indeterminate amount of time—there is no determined last round of the game and therefore no way to use backward induction to solve it. Players have to look ahead to determine the optimal strategies.

So what would a strategy to induce cooperation look like? Suppose Lena says to Sven, "I will share with you as long as you share with me, but as soon as you don't share, I will stop sharing with you for-

ever"—let's call this the "cooperate" strategy. Sven, in response, says, "OK, I will do the same. I will share with you until such time as you don't share, and then I'll stop sharing altogether." We must then ask, Is the act of both players playing these strategies a Nash equilibrium?

To answer this question, we have to figure out the best response to the strategy: Is it to play the same strategy, or is there a better strategy to play in response? To determine the answer to this question, let's think about playing the same strategy and alternate strategies and their payoffs.

If Lena claims she will play the cooperate strategy, what is Sven's outcome if he plays the cooperate strategy in response? Well, in the first period, Sven will get 100 because they both share, and since they both shared in period one, they will both share in period two, and so Sven will get 100, and it will continue like this forever. To put a present-day value on future earnings, we discount, so Sven's earnings stream (the payoff from a cooperate strategy) looks as follows:

$$100 + 100 \times d + 100 \times d^2 + 100 \times d^3 + 100 \times d^4 + \dots$$

What is the payoff from not cooperating? Well, in the period in which Sven decides not to share, Lena will still be sharing, and so Sven will get 110, but then after that, Lena will not share, and Sven knows this, so he will not share as well, and he will therefore get 95 for every round after. Let's call this strategy "deviate." Thus his earning stream (the **payoff from a deviate strategy**) looks like the following:

$$110 + 95 \times d + 95 \times d^2 + 95 \times d^3 + 95 \times d^4 + \dots$$

Note that we are only comparing the two strategies from the moment Sven decides to deviate, as the two payoff streams are identical up to that point and therefore cancel themselves out.

Is to cooperate the best response to the cooperate strategy? Yes, if

$$100 + 100 \times d + 100 \times d^2 + 100 \times d^3 + 100 \times d^4 + \dots > 110 + 95 \times d + 95 \times d^2 + 95 \times d^3 + 95 \times d^4 + \dots$$

Rearranging, we get:

$$5(d+d^2+d^3+d^4+\dots) > 10$$

This says that cooperation is better as long as the extra five points a cooperating player gets for every subsequent period after the first is better than the extra ten the deviating player gets in the first period. To determine if this is true, we have to use the result that

$$d+d^2+d^3+d^4+\ldots=\frac{d}{1-4}.$$
 So $5(\frac{d}{1-d})>10$, or
$$5d>10(1-d)$$

$$15d>10$$

$$d>\frac{2}{3}.$$

You can think of d as a measure of how much the players care about future payoffs, and so this says that as long as they care enough about the future payoffs, they will cooperate. In other words, if $d>\frac{2}{3}$,

then playing cooperate is a best response to the other player playing cooperate and vice versa: the strategy pair (cooperate, cooperate) is a Nash equilibrium for the infinitely repeated game.

This type of strategy has a name in economics: a **trigger strategy**. A trigger strategy is one where cooperative play continues until an opponent deviates and then ceases permanently or for a specified number of periods. An alternate strategy is the **tit-for-tat strategy**, where a player simply plays the same

strategy their opponent played in the previous round. Tit-for-tat strategies can also be a Nash equilibrium, and in fact, in infinitely repeated games where there are often many Nash equilibriums, the trigger strategy identified above is just one of many.

17.5 POLICY EXAMPLE

DO WE NEED TO REGULATE BANKS TO SAVE THEM FROM THEMSELVES?

Learning Objective 17.5: Explain how game theory can be used to understand the banking collapse of 2008.

In the mid-2000s, banks in the United States found themselves struggling to satisfy a tremendous demand for mortgages from the market for mortgage-backed securities: securities that were created from bundles of residential or commercial mortgages. This, along with the low-interest rate policy of the Federal Reserve, led to a tremendous housing boom in the United States that evolved into a speculative investment bubble. The bursting of this bubble led to the housing market crash and, in 2008, to a banking crisis: the failure of major banking institutions and the unprecedented government bailout of banks. These twin crises led to the worst recession since the Great Depression.

Interestingly, this banking crisis came relatively soon after a series of reforms of banking regulations in the United States that gave banks much more freedom in their operations. Most notably was the 1999 repeal of the provisions of the Glass-Steagall Act, enacted after the beginning of the Great Depression in 1933, which prohibited commercial banks from engaging in investment activities.

Part of the argument at the time of the repeal was that banks should be allowed to innovate and be more flexible, which would benefit consumers. The rationale was that increased competition and the discipline of the market would inhibit excessive risk-taking, so stringent government regulation was no longer necessary. But the discipline of the market assumes that rewards are absolute, meaning that returns are not based on relative performance or that the environment is not strategic. Is this an accurate description of modern banking? Probably not.

In everything from stock prices to CEO pay, relative performance matters, and if one bank were to rely on a low-risk strategy while others were engaging in higher risk-higher reward strategies, both the company's stock price and the compensation of the CEO might suffer. We can describe this in a very simplified model where there are two banks, and they can engage in either low-risk or high-risk strategies. This scenario is described in **table 17.9**, where we have two players, Big Bank and Huge Bank; the two strategies for each; and the payoffs (in millions):

| | Table 17.9 The risky ba | anking game | | |
|----------|-------------------------|---------------|---------------|--|
| | | Huge Bank | | |
| | | Low-Risk | High-Risk | |
| Big Bank | Low-Risk | B: 30; H: 30; | B: 22; H: 45; | |
| | High-Risk | B: 45; H: 22; | B: 25; H: 25; | |

We can see from the normal form game that both banks have dominant strategies: high risk. This is because the rewards are relative. Being a high-risk bank when your competitor is a low-risk bank brings a big reward; the relatively high returns are compounded by the reward from the stock market. In the end, both banks end up choosing high risk and are in a worse outcome than if they had chosen a low-risk strategy because of the increased likelihood of negative events from the strategy. Astute observers will recognize this game as a prisoner's dilemma, where behavior based on the individual self-interest of

the banks leads them to a second-best outcome. If you include the cost to society of bailing out high-risk banks when they fail, the second-best outcome is that much worse.

Can policy correct the situation and lead to a mutually beneficial outcome? The answer in this case is a **resounding yes**. If policy makers take away the ability of the banks to engage in high-risk strategies, the bad equilibrium will disappear, and only the low-risk, low-risk outcome will remain. The banks are better off, and because the adverse effects of high-risk strategies going bad are taken away, society benefits as well.

EXPLORING THE POLICY QUESTION

- 1. Why do you think that banks were so willing to engage in risky bets in the early 2000s?
- 2. Do you think that government regulation restricting their strategy choices is appropriate in cases where society has to pay for risky bets gone bad?

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

17.1 What Is Game Theory?

<u>Learning Objective 17.1</u>: Describe game theory and the types of situations it describes.

17.2 Single Play Games

Learning Objective 17.2: Describe normal form games, and identify optimal strategies and equilibrium outcomes in such games.

17.3 Sequential Games

<u>Learning Objective 17.3</u>: Describe sequential move games, and explain how they are solved.

17.4 Repeated Games

<u>Learning Objective 17.4</u>: Describe repeated games and the difference between finitely repeated games and infinitely repeated games and their equilibrium.

17.5 Policy Example

Do We Need to Regulate Banks to Save Them from Themselves?

Learning Objective 17.5: Explain how game theory can be used to understand the banking collapse of 2008.

LEARN: KEY TOPICS

Terms

Strategic interactions

Interactions in which agents must anticipate the actions of others when making decisions. Game theory is uesd to model them.

Game theory

The study of strategic interactions among economic agents. Any complete description of a game must include the following three elements:

Players

The agents actively participating in a game and who will experience outcomes based on the play of all players.

Strategies

All the possible strategic choices available to each player; can be the same for all players, the same for some players, or different for each player.

Payoffs

The outcomes associated with every possible strategic combination between players.

Non-cooperative games

Games in which the players are not able to negotiate and make binding agreements within the game, i.e., most competitive sports.

Simultaneous games

Games in which players take strategic actions at the same time without knowing what move the other has chosen, i.e., tag, rock paper scissors, real-time strategy games.

Sequential games

Games where players take turns and move consecutively, i.e., checkers, chess, a turn-based RPG.

Single-shot games

Games that are played once and then are over, i.e., rock paper scissors to determine who gets to sit in the front seat of the car.

Repeated games

Simlutaneous move games played repeatedly by the same players, i.e., rock paper scissors, best out of five.

Common knowledge

All participants are aware of all components in a game, and are also aware that all participants are aware.

Payoff matrix

A table that lists the players of the game, their strategies, and the payoffs associated with every possible strategy combination.

Normal form games

Games that can be represented with a payoff matrix.

Dominant strategy

A strategy for which the payoffs are always greater than any other strategy no matter what the opponent does.

Dominated strategy

A strategy for which the payoffs are always lower than any other strategy no matter what the opponent does.

Dominant strategy equilibrium (DSE)

An equilibrium in which each player plays their dominant strategy.

Best response function

A player's optimal strategy choice for every possible strategy choice of the other player.

Nash equilibrium

An outcome where, given the strategy choices of the other players, no individual player can obtain a higher payoff by altering their strategy choice

Pure strategies

A strategy a player selects with complete certainty.

Mixed strategies

A player randomizes strategies according to a set of probabilities that they choose.

Sequential move games

Games where players take turns making their strategic choices. Generally modeled by a game tree.

Game tree

A diagram that describes the players, their turns, their potential strategies for each turn, and the payoffs for every possible set of strateies.

Extensive form games

Another name for sequential move games.

Subgame perfect Nash equilibrium (SPNE)

The solution in which every player, at every turn of teh game, is playing an individually optimal strategy.

Trigger strategy

A strategy where cooperative play continues until an opponent deviates and then ceases permanently or for a specified number of period. In infinitely repeated games, where there are often many Nash equilibriums, the trigger strategy is just one of many.

Tit-for-tat strategy

A player simply plays the same strategy their opponent played in the previous round-can be considered a Nash equilibrium.

Tables and Figures

The valedictorian game

The valedictorian game

| Note Strategy | Sven's Payoff | Lena's Payoff |
|---------------|---------------|---------------|
| Sven shares | 90 | 110 |
| Lena shares | 110 | 90 |
| Neither share | 95 | 95 |
| Both share | 100 | 100 |

The party game, version 1

Figure 17.2.2 The party game, version 1

| | | Malia | |
|---------|-------------------------|-------------------------|------------------|
| | | International Club (IC) | Debate Club (DC) |
| Caitlin | International Club (IC) | C: 10; M: 10; | C: 2; M: 2 |
| | Debate Club (DC) | C: 2; M: 2 | C: 10; M: 10; |

The party game, version 2

| Figure 17.2.3 Th | e party game, version 2 |
|------------------|-------------------------|
|------------------|-------------------------|

| Figure 17.2.5 The part | | Malia | |
|------------------------|-------------------------|-------------------------|------------------|
| | | International Club (IC) | Debate Club (DC) |
| Caitlin | International Club (IC) | C: 1; M: 10; | C: 1; M: 2 |
| | Debate Club (DC) | C: 5; M: 2 | C: 15; M: 10; |

The matching pennies game

Table 17.4 The matching coin game

| Round | Ahmed's Play | Naveen's Play | Results |
|---------|--------------|---------------|-------------------------|
| Round 1 | Heads | Tails | Ahmed: -1 Naveen: +1 |
| Round 2 | Heads | Heads | Ahmed: +1 Naveen: -1 |
| Round 3 | Tails | Tails | Ahmed: +1 Naveen: -1 |
| Round 4 | Tails | Heads | Ahmed: -1 Naveen: +1 |

The curry pricing game

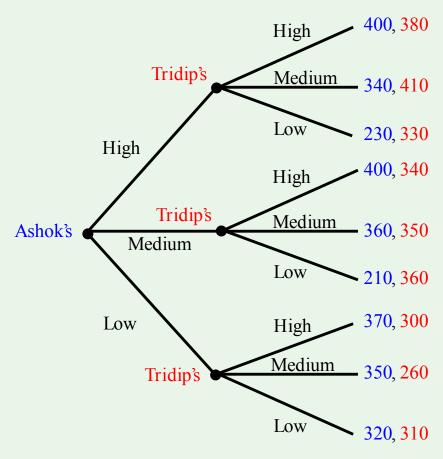


Figure 17.1 The curry pricing game

The market entry game

| | Table 17.8 Nash equilibrium in the ma | Market entry game Vito's (Potential Entrant) | |
|-----------------------|--|---|-----------------------|
| | | Enter | Don't Enter |
| Gino's (Incumbent) | Accommodate | G: 200; V: <u>300;</u> | G: <u>400</u> ; V: 0 |
| | Fight | G: 100; M: 200 | G: <u>400</u> ; M: 0; |

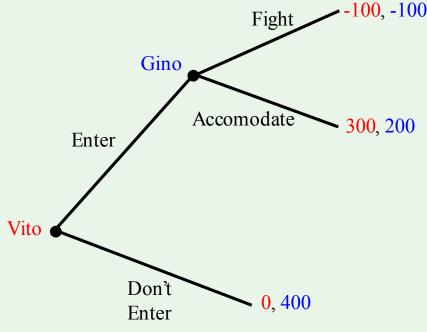


Figure 17.2 The market entry game

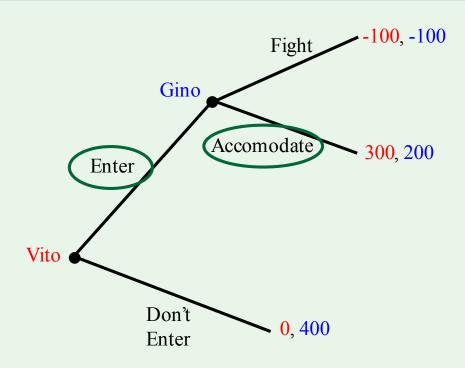


Figure 17.3 The squential market entry game SPNE

The risky banking game

Table 17.9 The risky banking game

| | | Huge Bank | |
|----------|-----------|---------------|---------------|
| | | Low-Risk | High-Risk |
| Big Bank | Low-Risk | B: 30; H: 30; | B: 22; H: 45; |
| | High-Risk | B: 45; H: 22; | B: 25; H: 25; |

Equations

Payoff from a cooperate strategy

$$100 + 100 imes d + 100 imes d^2 + 100 imes d^3 + 100 imes d^4 + \dots$$

Payoff from a deviate strategy

$$110 + 95 \times d + 95 \times d^2 + 95 \times d^3 + 95 \times d^4 + \dots$$

Comparing the Two

Is to cooperate the best response to the cooperate strategy? Yes, if

$$100 + 100 imes d + 100 imes d^2 + 100 imes d^3 + 100 imes d^4 + \dots \ > 110 + 95 imes d + 95 imes d^2 + 95 imes d^3 + 95 imes d^4 + \dots$$

Which can be rearranged into:

$$5(d+d^2+d^3+d^4+\dots)>10$$

When applied to the valedictorian game, the equation says cooperation is better that as long as the extra five points a cooperating player gets for every subsequent period after the first is better than the extra ten the deviating player gets in the first period. We can test that with the following equation:

$$d+d^2+d^3+d^4+\ldots=\frac{d}{1-4}$$

Thus

$$5(rac{d}{1-d})>10$$
, or $5d>10(1-d)$ $15d>10$ $d>rac{2}{3}$

The variable d can be thought of as a measure of how much the players care about future payoffs. With $d>rac{2}{3}$, we can assume that the players will cooperate due to their concern over future outcomes.

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CHAPTER 18

Models of Oligopoly: Cournot, Bertrand, and Stackelberg

Cournot, Bertrand, and Stackelberg

THE POLICY QUESTION

HOW SHOULD THE GOVERNMENT HAVE RESPONDED TO BIG OIL COMPANY MERGERS?

Exploring the Policy Question

- 1. How do oil companies compete—on quantities or prices?
- 2. What policy solutions present themselves from this analysis?

LEARNING OBJECTIVES

18.1 Cournot Model of Oligopoly: Quantity Setters

Learning Objective 18.1: Describe how oligopolist firms that choose quantities can be modeled using game theory.

18.2 Bertrand Model of Oligopoly: Price Setters

Learning Objective 18.2: Describe how oligopolist firms that choose prices can be modeled using game theory.

18.3 Stackelberg Model of Oligopoly: First-Mover Advantage

Learning Objective 18.3: Describe the different outcomes when oligopolist firms choose quantities sequentially.

18.4 Policy Example

How Should the Government Have Responded to Big Oil Company Mergers?

<u>Learning Objective 18.4</u>: Explain how models of oligopoly can help us understand how to respond to proposed mergers of oil companies that sell retail gas.

18.1 COURNOT MODEL OF OLIGOPOLY: QUANTITY SETTERS

Learning Objective 18.1: Describe how oligopolist firms that choose quantities can be modeled using game theory.

Oligopoly markets are markets in which only a few firms compete, where firms produce homogeneous or differentiated products, and where barriers to entry exist that may be natural or constructed. There are three main models of oligopoly markets, and each is considered a slightly different competitive environment. The Cournot model considers firms that make an identical product and make output decisions simultaneously. The Bertrand model considers firms that make an identical product but compete on price and make their pricing decisions simultaneously. The Stackelberg model considers quantity-setting firms with an identical product that make output decisions simultaneously. This chapter considers all three in order, beginning with the Cournot model.

Table 18.1 Metrics of the four basic market structures

| | Number of firms | Similarity of goods | Barriers to entry or exit | Chapter |
|--------------------------|-----------------|-----------------------|---------------------------|-----------|
| Perfect competition | Many | Identical | No | <u>13</u> |
| Monopolistic competition | Many | Distinct | No | 19 |
| Oligopoly | Few | Identical or distinct | Yes | 18 |
| Monopoly | One | Unique | Yes | <u>15</u> |

Oligopolists face downward-sloping demand curves, which means that price is a function of the total quantity produced, which, in turn, implies that one firm's output affects not only the price it receives for its output but the price its competitors receive as well. This creates a strategic environment where one firm's profit maximizing output level is a function of its competitors' output levels. The model we use to analyze this is one first introduced by French economist and mathematician Antoine Augustin Cournot in 1838. Interestingly, the solution to the Cournot model is the same as the more general Nash equilibrium concept introduced by John Nash in 1949 and the one used to solve for equilibrium in non-cooperative games in chapter 17.

We will start by considering the simplest situation: two companies that make an identical product and that have the same cost function. Later we will explore what happens when we relax those assumptions and allow more firms, differentiated products, and different cost functions.

Let's begin by considering a situation where there are two oil refineries located in the Denver, Colorado, area that are the only two providers of gasoline for the Rocky Mountain regional wholesale market. We'll call them Federal Gas and National Gas. The gas they produce is identical, and they each decide independently—and without knowing the other's choice—the quantity of gas to produce for the week at the beginning of each week. We will call Federal's output choice q_F and National's output choice q_N , where q represents liters of gasoline. The weekly demand for wholesale gas in the Rocky Mountain region is P=A-BQ, where Q is the total quantity of gas supplied by the two firms, or $Q=q_F+q_N$. Immediately, you can see the strategic component: the price they both receive for their gas is a function of each company's output. We will assume that each liter of gas produced costs the company c, or that c is the marginal cost of producing a liter of gas for both companies and that there are no fixed costs.

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With these assumptions in place, we can express Federal's profit function:

Calculus

If the profit function is $\pi_F{=}q_F(A-B(q_F+q_N)-c)$,

then we can find the optimal output level by solving for the stationary point, or solving

$$\frac{\partial \pi_F}{\partial q_F} = 0$$

If $\pi_F = q_F (A - B(q_F + q_N) - c)$, then we can expand

to find

$$\pi_F {=} Aq_F - Bqrac{F}{2} {-} Bq_Fq_N - cq_F$$

Taking the partial derivative of this expression with respect to q_F ,

$$rac{\partial \pi_F}{\partial q_F} \!\!=\!\! A - 2Bq_F - Bq_N - c \!\!=\!\! 0$$

If we rearrange this, we can see that this is simply an expression of

$$MR = MC \cdot \ A - 2Bq_F - Bq_N {=} c$$

The marginal revenue looks the same as a monopolist's MR function but with one additional term, $-Bq_N$.

Solving for q_F yields

$$q_F = rac{A - Bq_N - c}{2B}$$

or

$$q_F^*=rac{A-c}{2B}-rac{1}{2}qN$$

This is Federal Gas's best response function, their profit maximizing output level given the output choice of their rivals. It is the same best response function as the ones in <u>chapter 17</u>. By symmetry, National Gas has an identical best response function:

$$q_N^*=rac{A-c}{2B}-rac{1}{2}qF$$

$$\pi_F = P imes q_F -\!\!\!-\!\!\!- c imes q_F = q_F(P-c)$$

Substituting the inverse demand curve, we arrive at the expression

$$\pi_F = q_F(A - BQ - c).$$

Substituting $Q=q_A+q_B$ yields

$$\pi_F = q_F(A-B(q_F+q_N)-c).$$

The expression for National is symmetric:

$$\pi_N = q_N(A - B(q_N + q_F) - c)$$

Note that we have now described a game complete with players, Federal and National; strategies, q_F and q_N ; and payoffs, π_F and π_N . Now the task is to search for the equilibrium of the game. To do so,

we have to begin with a best response function. In this case, the best response is the firm's profit maximizing output. This will depend on both the firm's own output and the competing firm's output.

We know from chapter 15 that the monopolists' marginal revenue curve when facing an inverse demand curve P=A-BQ is MR(q)=A-2Bq. This duopolistic example shows that the firms' marginal revenue curves include one extra term:

$$MR_F(q_F) = A - 2Bq_F - Bq_N$$
 and $MR_N(q_N) = A - 2Bq_N - Bq_F$

The profit maximizing rule tells us that to find the profit maximizing output, we must set the marginal revenue to the marginal cost and solve. Doing so yields

$$q_F^* = rac{A-c}{2B} - rac{1}{2}qN$$

for Federal Gas and

$$q_N^*=rac{A-c}{2B}-rac{1}{2}qF$$

for National Gas. These are the firms' best response functions, their profit maximizing output levels given the output choice of their rivals.

Now that we know the best response functions, solving for equilibrium in the model is relatively straightforward. We can begin by graphing the best response functions. These graphical illustrations of the best response functions are called **reaction curves**. A Nash equilibrium is a correspondence of best response functions, which is the same as a crossing of the reaction curves.

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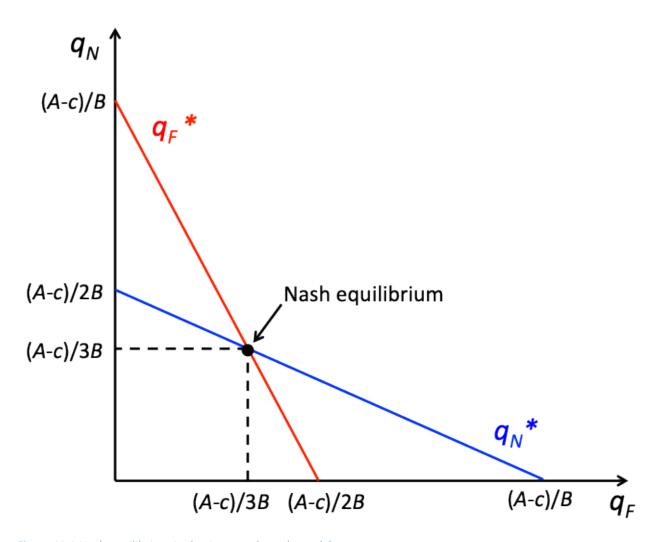


Figure 18.1 Nash equilibrium in the Cournot duopoly model

In **figure 18.1**, we can see the Nash equilibrium of the Cournot duopoly model as the intersection of the reaction curves. Mathematically, this intersection is found by simultaneously solving

$$q_F^*=rac{A-c}{2B}-rac{1}{2}q_N$$
 and $q_F^*=rac{A-c}{2B}-rac{1}{2}q_F$

This is a system of two equations and two unknowns and therefore has a unique solution as long as the slopes are not equal. We can solve these by substituting one equation into the other, which yields a single equation with a single unknown:

$$q_F^* = rac{A-c}{2B} - rac{1}{2} [rac{A-c}{2B} - rac{1}{2} q_F]$$

Solving this by steps results in the following:

$$q_F^* = rac{A-c}{2B} - rac{A-c}{4B} + rac{1}{4}q_Frac{3}{4}q_F^* = rac{A-c}{4B} \ q_F^* = rac{A-c}{3B}$$

And by symmetry, we know that the two optimal quantities are the same:

$$q_N^* = rac{A-c}{3B}$$

The Nash equilibrium is

$$(q_F^st,q_N^st)$$

or

$$(\frac{A-c}{3B}, \frac{A-c}{3B}).$$

Let's consider a specific example. Suppose in the above example, the weekly demand curve for wholesale gas in the Rocky Mountain region is

$$p=1,000-2Q$$
, in thousands of gallons

Both firms have constant marginal costs of 400. In this case,

$$A=1,000$$
, $B=2$ and $C=400$.

So,

$$q_F^* = rac{A-c}{3B} = rac{1,000-400}{(3)(2)} = rac{600}{6} = 100$$

By symmetry, we know

$$q_N^st=100$$

as well. So both Federal Gas and National Gas produce 100,000 gallons of gasoline a week. Total output is the sum of the two and is 200,000 gallons. The price is p=1,000-2(200)=\$600 for 1,000 gallons of gas, or \$0.60 a gallon.

To analyze this from the beginning, we can set up the total revenue function for Federal Gas:

$$TR(q_F) = p imes q_F \ = (1,000-2Q)q_F \ = (1,000-2q_F-2q_N)q_F \ = 1,000-2q_F^2-2q_Fq_N$$

The marginal revenue function that is associated with this is

$$MR(q_F) = 1,000 - 4q_F - 2q_N$$
.

We know marginal cost is 400, so setting marginal revenue equal to marginal cost results in the following expression:

$$1,000 - 4q_F - 2q_N = 400$$

Solving for q_F results in the following:

$$q_F = rac{600 - 2q_N}{4} \ q_F^* = 150 - rac{q_F}{2}$$

This is the best response function for Federal Gas. By symmetry, we know that National Gas has the same best response function:

$$q_N^*=150-rac{q_F}{2}$$

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Solving for the Nash equilibrium, we get the following:

$$egin{aligned} q_N^* &= 150 - rac{q_F}{2} \ q_F^* &= 150 - 75 + rac{q_F}{4} \ /frac34q_F^* &= 25 \ q_F^* &= 100 \end{aligned}$$

We can insert the solution for q_F into q_N^st :

$$q_N^* = 150 - rac{(100)}{2} = 100$$

18.2 BERTRAND MODEL OF OLIGOPOLY: PRICE SETTERS

Learning Objective 18.2: Describe how oligopolist firms that choose prices can be modeled using game theory.

In the previous section, we studied oligopolists that make an identical good and who compete by setting quantities. The example we used in that section was wholesale gasoline, where the market sets a price that equates supply and demand and the strategic decision of the refiners was how much oil to refine into gasoline. In this section, we turn our attention to a different situation in which the oligopolists compete on price. The example here is the retail gas stations that bought the wholesale gas from the refiners and are now ready to sell it to consumers. We still have identical goods; for consumers, the gas that goes into their cars is all the same, and we will assume away any other differences like cleaner stations or the presence of a mini-mart.

Let's imagine a simple situation where there are two gas stations, Fast Gas and Speedy Gas, on either side of a busy main street. Both stations have large signs that display the gas prices that each station is offering for the day. Consumers are assumed to be indifferent about the gas or the stations, so they will go to the station that is offering the lower price. So an individual gas station's demand is conditional on its relative price with the other station.

Formally, we can express this with the following demand function for Fast Gas:

$$Q_F \left\{egin{array}{l} a-bP_F ext{ if } P_F < P_S \ rac{a-bP}{2} ext{ if } P_F = P_S \ 0 ext{ if } P_S > P_F \end{array}
ight.$$

Speedy Gas has an equivalent demand curve:

$$Q_S \left\{ egin{aligned} a - bP_S ext{ if } P_S < P_F \ rac{a - bP}{2} ext{ if } P_S = P_F \ 0 ext{ if } P_S > P_F \end{aligned}
ight.$$

In other words, these demand curves say that if a station has a lower price than the other, they will get all the demand at that price, and the other station will get no demand. If they have the same price, then each will get one-half of the demand at that price.

Let's assume that Fast Gas and Speedy Gas both have the same constant marginal cost of c and no fixed costs to keep the analysis simple. The question we now have to answer is, What are the best response functions for the two stations? Remember that best response functions are one player's optimal strategy choice given the strategy choice of the other player. So what is Fast Gas's best response to Speedy Gas's price?

If Speedy Gas charges

$$P_S > c$$

Fast Gas can set $P_F>P_S$ and they will get no customers at all and make a profit of zero. Fast Gas could instead set

$$P_F = P_S$$

and get $\dfrac{1}{2}$ the demand at that price and make a positive profit. Or they could set

$$P_F=P_S-\$0.01$$

or set their price one cent below Speedy Gas's price and get all the customers at a price that is one cent below the price, at which they would get $\frac{1}{2}$ the demand.

Clearly, this third option is the one that yields the most profit. Now we just have to consider the case where $P_S=c$. In this case, undercutting the price by one cent is not optimal because Fast Gas would get all the demand but would lose money on every gallon of gas sold, yielding negative profits. Setting

$$P_F = P_S = c$$

would give them half the demand at a break-even price and would yield exactly zero profits.

The best response function we just described for Fast Gas is the same best response function for Speedy Gas. So where are the correspondences of best response functions? As long as the prices are above c, there is always an incentive for both stations to undercut each other's price, so there is no equilibrium. But at $P_F = P_S = c$, both stations are playing their best response to each other simultaneously. So the unique Nash equilibrium to this game is

$$P_F = P_S = c$$
.

What is particularly interesting about this is the fact that this is the same outcome that would have occurred if they were in a perfectly competitive market because competition would have driven prices down to marginal cost. So in a situation where competition is based on price and the good is relatively homogeneous, as few as two firms can drive the market to an efficient outcome.

18.3 STACKELBERG MODEL OF OLIGOPOLY: FIRST-MOVER ADVANTAGE

Learning Objective 18.3: Describe the different outcomes when oligopolist firms choose quantities sequentially.

Both the Cournot model and the Bertrand model assume simultaneous move games. This makes sense when one firm has to make a strategic decision before knowing about the strategy choice of the other firm. But not all situations are like this. What happens when one firm makes its strategic decision first and the other firm chooses second? This is the situation described by the Stackelberg model, where the firms are quantity setters selling homogenous goods.

Let's return to the example of two oil companies: Federal Gas and National Gas. The gas they produce is identical, but now they decide their output levels sequentially. We will assume that Federal Gas sets its output first, and then after observing Federal's choice, National Gas decides on the quantity of gas they are going to produce for the week. We will again call Federal's output choice q_F and National's

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output choice q_N , where q represents liters of gasoline. The weekly demand for wholesale gas is still P=A-BQ, where Q is the total quantity of gas supplied by the two firms, or

$$Q = q_F + q_N$$
.

We have now turned the previous Cournot game into a sequential game, and the SPNE solution to a sequential game is found through backward induction. So we have to start at the second move of the game: National's output choice. When National makes this decision, Federal's output choices are already made and known to National, so it is taken as given. Therefore, we can express Federal's profit function as

$$\Pi_N = q_N(A - B(q_N + q_F) - c).$$

This is the same as in the Cournot example, and for National, the best response function is also the same. This is because in the Cournot case, both firms took the other's output as given.

$$q_N^*=rac{A-c}{2B}-rac{1}{2}q_F$$

When it comes to Federal's decision, we diverge from the Cournot model because instead of taking q_N as a given, Federal knows exactly how National will respond because they know the best response function. Federal's profit function,

$$\Pi_F = q_F(A - Bq_F - Bq_N - c)$$
,

can be re-written, replacing q_N with the best response function:

$$\Pi_F=q_F(A-Bq_F-B(rac{A-C}{2B}-rac{1}{2})-c)$$

We can see that Federal's profits are determined only by their own output once we explicitly consider National's response. Simplifying yields

$$\Pi_F = q_F (rac{A-c}{2} - Brac{1}{2}q_F) \cdot$$

We know that the second mover's best response is the same as in <u>section 18.1</u>, and the solution to the profit optimization problem above yields the following best response function for Federal Gas:

$$q_F^* = rac{A-c}{2B}$$
 ,

substituting this into National's best response function and solving the following:

$$q_N^* = rac{A-c}{2B} - rac{1}{2} iggl[rac{A-c}{2B}iggr] \ q_N^* = rac{A-c}{2B} - iggl[rac{A-c}{4B}iggr] \ q_N^* = rac{A-c}{4B}$$

The subgame perfect Nash equilibrium is

Calculus

If the profit function is $\Pi_F {=} q_F ig(rac{A-C}{2} {-} Brac{1}{2} q_Fig)$, then we

can find the optimal output level by solving for the stationary point, or solving

$$rac{\partial \Pi_F}{\partial q_F}$$
 $=$ 0 If Π_F $=$ q_F $(rac{A-c}{2}-Brac{1}{2}q_F)$, then we can expand to find Π_F $=$ q_F $(rac{A-c}{2})q_F-Brac{1}{2}q_F^2$

Taking the partial derivative of this expression with respect to q_F , we get

$$rac{\partial \Pi_F}{\partial q_F} = (rac{A-c}{2}) - Bq_F = 0$$

Solving for q_F yields

$$q_F = rac{A-c}{2B}$$

This is Federal Gas's profit maximizing output level, given that they choose first and can anticipate National's response.

$$(q_F^*, q_F^*)$$

A few things are worth noting when comparing this outcome to the Nash equilibrium outcome of the Cournot game in section 18.1. First, the individual output level for Federal, the first mover in the Stackelberg game, the **Stackelberg leader**, is higher than it is in the Cournot game. Second, the individual output level for National, the second mover in the Stackelberg game, the **Stackelberg follower**, is lower than it is in the Cournot game. Third, the total output is larger in the Stackelberg outcome than in the Cournot outcome. This means the price is lower because the demand curve is downward sloping. Since the Cournot outcome is one of the options for the Stackelberg leader—if it chooses the same output as in the Cournot case, the follower will as well—it must be true that profits are higher for the Stackelberg leader. And since both the quantity produced and the price received are lower for the Stackelberg follower compared to the Cournot outcome, the profits must be lower as well.

So from this we see the major differences in the Stackelberg model compared to the Cournot model. There is a considerable **first-mover advantage**. By being able to set its quantity first, Federal Gas is able to gain a larger share of the market for itself, and even though it leads to a lower price, it makes up for that lower price with the increase in quantity to achieve higher profits. The opposite is true for the second mover: by being forced to choose after the leader has set its output, the follower is forced to accept a lower price and lower output. From the consumer's perspective, the Stackelberg outcome is preferable because overall, there is more quantity at a lower price.

18.4 POLICY EXAMPLE

HOW SHOULD THE GOVERNMENT HAVE RESPONDED TO BIG OIL COMPANY MERGERS?

Learning Objective 18.4: Explain how models of oligopoly can help us understand how to respond to proposed mergers of oil companies that sell retail gas.

The end of the twentieth century saw a number of mergers of massive oil companies. In 1999, BP Amoco acquired ARCO, followed soon thereafter by Exxon's acquisition of Mobil. Then, in 2001, Chevron acquired Texaco for \$38.7 billion. The newly combined company became the world's fourth-largest producer of oil and natural gas. Whenever any such mergers and acquisitions are proposed, the US government has to approve the deal, and sometimes this approval comes with conditions designed to protect US consumers from undue harm that the consolidation might cause due to market concentration. In this case, the Federal Trade Commission (FTC) was the agency that provided oversight, and in the end, they approved the merger with the following condition: they had to sell their stake in two massive oil refineries. However, they were largely allowed to retain their retail gas operations, even though both companies had significant market presence and their merger would cause a drop in the competitiveness of the retail gas market, particularly in some areas where both companies had a significant market share.

On their face, these decisions seem to make little sense. How is it that the US government is worried about the impact of the merger on refining and the wholesale gas market but not on the retail gas market? The answer lies in the way these two markets fit into the economic models of oligopoly. Refining and wholesale gas operations are more akin to the Cournot model, where a few firms produce a homogenous product and compete on quantity and the sum total of all gas refined sets the wholesale market price. The insight of the Cournot model is that every merger produces fewer firms, and this constrains supply and increases price. Remember that this is a function not of capacity—that has not changed—but of the strategic environment, which makes it easier for all firms to constrict supply, which, in turn, raises prices and profits. The lower supply and higher prices do material harm to consumers, however, and it

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is for this reason that the FTC stepped in and demanded that the merged company sell off its interest in two big refining operations.

On the other hand, retail gas is more akin to the Bertrand model, where a bunch of retailers are selling a homogenous good but are competing mostly on price. A cursory examination of the retail gas industry confirms this: prices are posted prominently, and consumers show very strong responses to lower prices. The Bertrand model shows us that it takes very little competition to result in highly competitive pricing, so a merger that might reduce the number of competing gas station brands by one is unlikely to have much of a material effect on prices and therefore will be unlikely to harm consumers.

Viewed through the lens of the models of oligopoly studied in this chapter, the FTC's decision to demand a divestment in oil refining and wholesale gas operations but mostly allow the retail side to consolidate makes sense. It is no surprise that these are the very same models the government uses to analyze such situations and devise a response.

EXPLORING THE POLICY QUESTION

- 1. Do you think it is correct that wholesale gas looks more like the Cournot model and retail gas looks more like the Bertrand model?
- 2. Do you think the government did the right thing in the case of the Chevron-Texaco merger?

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

18.1 Cournot Model of Oligopoly: Quantity Setters

Learning Objective 18.1: Describe how oligopolist firms that choose quantities can be modeled using game theory.

18.2 Bertrand Model of Oligopoly: Price Setters

Learning Objective 18.2: Describe how oligopolist firms that choose prices can be modeled using game theory.

18.3 Stackelberg Model of Oligopoly: First-Mover Advantage

Learning Objective 18.3: Describe the different outcomes when oligopolist firms choose quantities sequentially.

18.4 Policy Example

How Should the Government Have Responded to Big Oil Company Mergers?

<u>Learning Objective 18.4</u>: Explain how models of oligopoly can help us understand how to respond to proposed mergers of oil companies that sell retail gas.

LEARN: KEY TOPICS

Terms

Oligopolist market

Oligopoly markets are markets in which only a few firms compete, where firms produce homogeneous or differentiated products, and where barriers to entry exist that may be natural or constructed.

The Cournot Model

The Cournot model considers firms that make an identical product and make output decisions simultaneously.

The Bertrand Model

The Bertrand model considers firms that make an identical product but compete on price and make their pricing decisions simultaneously.

The Stackelberg Model

The Stackelberg model considers quantity-setting firms with an identical product that make output decisions simultaneously.

Tables and Graphs

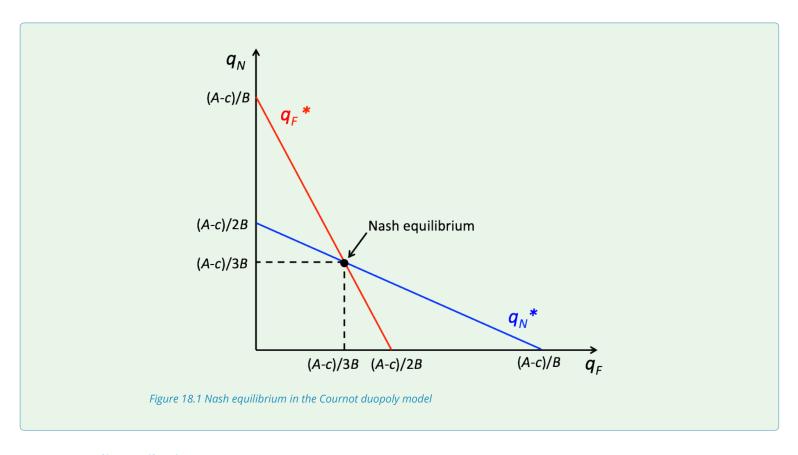
Metrics of the four basic market structures

Table 18.1 Metrics of the four basic market structures

| | Number of firms | Similarity of goods | Barriers to entry or exit | Chapter |
|--------------------------|-----------------|-----------------------|---------------------------|-----------|
| Perfect competition | Many | Identical | No | <u>13</u> |
| Monopolistic competition | Many | Distinct | No | <u>19</u> |
| Oligopoly | Few | Identical or distinct | Yes | 18 |
| Monopoly | One | Unique | Yes | 15 |

Nash equilibrium in the Cournot duopoly model

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CHAPTER 19

Monopolistic Competition

THE POLICY QUESTION

SHOULD PUBLIC SCHOOLS REQUIRE STUDENTS TO WEAR UNIFORMS?

Exploring the Policy Question

- 1. How are fashion and sportswear companies able to charge so much for clothes?
- 2. Would requiring the use of generic uniform clothes improve welfare?

LEARNING OBJECTIVES

19.1 What Is Monopolistic Competition?

Learning Objective 19.1: Describe the structure of the monopolistically competitive market.

19.2 Equilibrium in Monopolistic Competition

Learning Objective 19.2: Explain how equilibrium is achieved in monopolistically competitive markets.

19.3 Policy Example

Should Public Schools Require Students to Wear Uniforms?

<u>Learning Objective 19.3</u>: Use knowledge of monopolistically competitive markets to explain how switching to generic uniforms can improve welfare.

19.1 WHAT IS MONOPOLISTIC COMPETITION?

Learning Objective 19.1: Describe the structure of the monopolistically competitive market.

Monopolistically, competitive markets are markets in which low fixed costs and free entry and exit of firms make them competitive but in which firms are able to differentiate their products, which causes them to face downward-sloping demand curves like imperfectly competitive firms, such as monopolists.

As an example, consider the market for athletic shoes. In the United States in 2017, Nike had a 35 percent share of the athletic shoe market; its Jordan brand had a 12 percent share; Adidas had an 11 percent share; and Sketchers, New Balance, Converse, and Under Armour had 6.3 percent, 3.7 percent, 3.6 percent, and 2.4 percent, respectively. The process of designing and making athletic shoes is not very

capital intensive, so there are low fixed costs and no barriers to entry—any company that would like to sell shoes in the United States may do so. Athletic shoes are largely similar, and despite high-end shoes that may include special materials or technologies that enjoy patent protection, a regular pair of running shoes are relatively the same: cloth upper, foam padding, and a rubber sole. Despite this, Nike is able to charge considerably more for its shoes than a generic equivalent. Why? Part of the reason is that through branding and marketing, Nike has differentiated its shoes from those of competing companies.

Though athletic shoe companies expend a lot of time and effort on product differentiation, even firms that produce very similar products might be monopolistically competitive with a small amount of differentiation if the market is small enough. In perfectly competitive markets, the assumption is that firms are price takers because each individual firm is such a small part of the overall market. But if the market is so small that it only supports a few firms, each firm could have a downward-sloping demand curve. For example, in a very small town with only two coffee shops, if the shops are able to attract a particular type of customer, they might be able to charge more because the customers prefer their shop to the rival shop. Perhaps one shop has a decor and music that appeal to younger customers, while the other has a decor and music that appeal to older customers.

19.2 EQUILIBRIUM IN MONOPOLISTIC COMPETITION

Learning Objective 19.2: Explain how equilibrium is achieved in monopolistically competitive markets.

To think about equilibrium in monopolistically competitive markets, we begin by assuming firms with identical costs and homogeneous products. Unlike perfectly competitive firms that take the market equilibrium prices as given, monopolistically competitive firms achieve some pricing power through product differentiation. In essence, these firms "capture" part of the market for themselves. This doesn't mean they can charge any price they like but that they create for themselves a downward-sloping demand curve. In the absence of competition, such a scenario would potentially lead to monopoly rents and economic profits. However, the free entry and exit of firms will guarantee that there will be no economic profits in the long run because any positive economic profits will induce new firms to enter. The resulting equilibrium looks like the graph in **figure 19.1**, which shows how one firm can both face a downward-sloping demand curve and have zero economic profits.

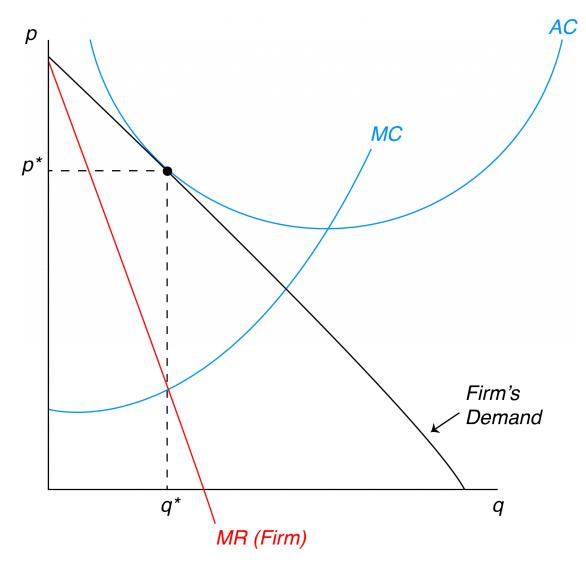
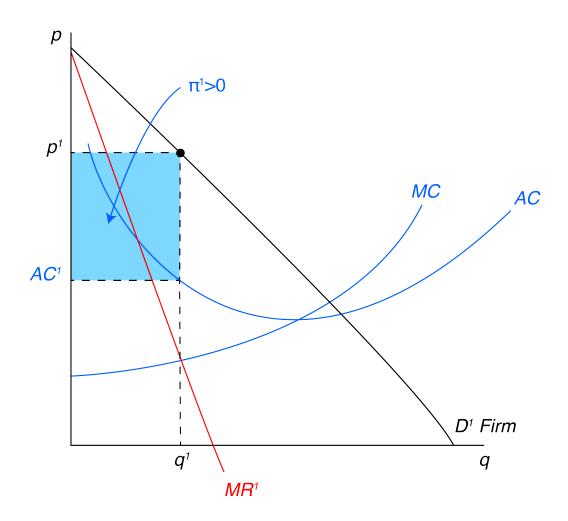


Figure 19.1 Equilibrium in monopolistically competitive markets

In **figure 19.1**, the red line is the firm's marginal revenue curve. Since the firm faces a downward-sloping demand curve, they have a downward-sloping marginal revenue curve similar to a monopolist. The difference is this marginal revenue curve is from their individual demand curve, which is only a part of total demand. Monopolistically competitive firms are profit maximizing firms and therefore set their output where marginal revenue equals marginal cost. To find this point, we look at the firm's cost curves, in blue, and find the intersection of marginal revenue and marginal cost. In the figure, this occurs at the quantity q^* . The maximum price the firm can charge and sell q^* is p^* . The firm's average cost at q^* is equal to p^* , so its total cost is equal to its total revenue, and therefore its economic profits are zero.



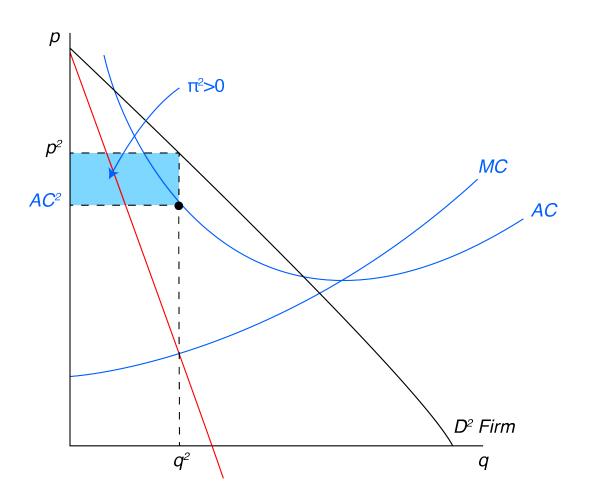


Figure 19.2 Achieving equilibrium in monopolistically competitive markets

How is this equilibrium reached? Start by considering a firm that is making positive economic profits while facing a downward-sloping demand curve, as in **figure 19.2**, panel a. As other entrepreneurs observe the profits being made by incumbent firms, they will decide to enter the market. This will whittle away some of the demand for the incumbent firm, as seen in panel b. This will continue as long as any positive economic profits remain but will stop once economic profits arrive at zero, as seen in panel c. Note that on the firm level, this outcome is not the same as the competitive market outcome, where a firm's price is equal to marginal cost. This means that there is some welfare loss from a firm's ability to differentiate products. It can also be true that the process of product differentiation can be costly—for example, when Nike pays athletes to wear its shoes and advertises its brand. This leads to higher costs and further diminishes welfare produced by the athletic shoe market.

19.3 POLICY EXAMPLE

SHOULD PUBLIC SCHOOLS REQUIRE STUDENTS TO WEAR UNIFORMS?

Learning Objective 19.3: Use knowledge of monopolistically competitive markets to explain how switching to generic uniforms can improve welfare.

There are a number of rationales for school uniforms in public schools: to assure that kids from poorer households don't feel disadvantaged, to reduce problems with inappropriate attire, to eliminate the possibility of gang-related attire, and so on. All of these are potentially good reasons, but good policy analysis requires that we think about the social welfare of the market itself. By removing the incentive to differentiate through fashion and brands, school districts are forcing pupils to move from a monopolistically competitive market to one that is closer to a perfectly competitive market. The cost to individuals could be a loss of utility from being unable to express individual style, but the potential gain to the community is a lower cost of attending school.

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

19.1 What Is Monopolistic Competition?

Learning Objective 19.1: Describe the structure of the monopolistically competitive market.

19.2 Equilibrium in Monopolistic Competition

Learning Objective 19.2: Explain how equilibrium is achieved in monopolistically competitive markets.

19.3 Policy Example

Should Public Schools Require Students to Wear Uniforms?

<u>Learning Objective 19.3</u>: Use knowledge of monopolistically competitive markets to explain how switching to generic uniforms can improve welfare.

LEARN: KEY TOPICS

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Monopolistically, competitive markets are markets in which low fixed costs and free entry and exit of firms make them competitive but in which firms are able to differentiate their products, which causes them to face downward-sloping demand curves like imperfectly competitive firms, such as monopolists.

Graphs

Equilibrium in monopolistically competitive markets

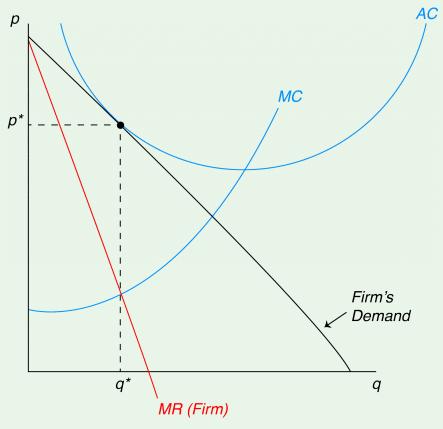
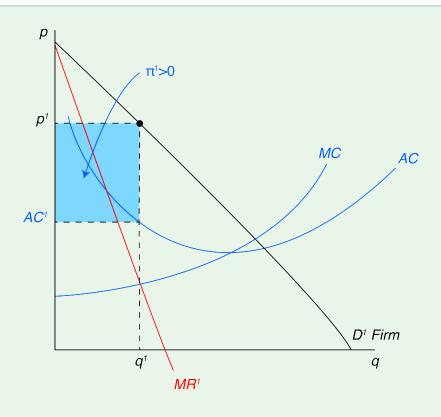
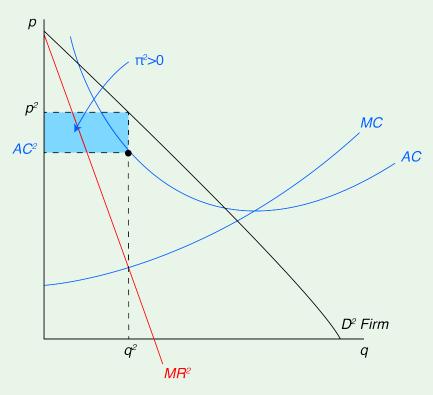


Figure 19.1 Equilibrium in monopolistically competitive markets

Achieving equilibrium in monopolistically competitive markets





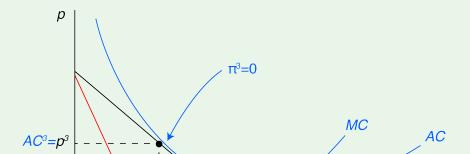


Figure 19.2 Achieving equilibrium in monopolistically competitive markets

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CHAPTER 20

Externalities

THE POLICY QUESTION

SHOULD THE CITY OF NEW YORK BAN SODA TO ADDRESS THE OBESITY EPIDEMIC?

In 2012, Michael Bloomberg, the then mayor of New York, announced the sugary drinks portion cap rule, which would have banned the sale of sweetened drinks in containers larger than 16 oz. in places that fell under New York City regulation, including delis, restaurants, and fast-food outlets. The argument for the ban focused on the negative health outcomes associated with the consumption of high amounts of sugar. These negative outcomes, the promotors claimed, were a societal concern, as the disproportionately affected pooper populations rely more heavily on government-supported health care.

Here's an excerpt from the Washington Post article on March 11, 2013:

Under Bloomberg's ban, "sugary beverages" larger than 16 ounces could not be sold at food-service establishments in New York City. At restaurants with self-service soda fountains, cups larger than 16 ounces could not be provided. Only outlets that get health-department grades were included, so supermarkets, vending machine operators and convenience stores . . . didn't have to worry about the ban. There was no ban on refills. Failure to comply could have led to a \$200 fine. It was set to take effect on Tuesday.

[A "sugary beverage" is] a drink with more than 25 calories per eight ounces, which has either been sweetened by the manufacturer or mixed with another caloric sweetener. The ban did not apply to pure fruit juice or fruit smoothies, drinks that are more than half milk, calorie-free diet sodas or alcoholic beverages. Milkshakes, if they were more than half milk or ice cream, were exempt. But sweetened coffee drinks, if less than half milk, were not.

To some people, the attempted ban represents a ridiculous intrusion of the government into the market and individual choice. To others, the ban represents a reasonable government response to an obesity epidemic that puts a strain on and imposes real costs on the public health care system. In order to analyze these conflicting viewpoints, we need to understand the nature and economics of externalities: private actions that have social costs and benefits.

In this chapter, we will study externalities and develop a model to study them. We can use the model to discuss ways to address externalities through private action or government policy.

With a general understanding of externalities in place, we can proceed to study the New York City soda ban and analyze its effectiveness in dealing with the particular externality problem of the obesity epidemic.

Exploring the Policy Question

- 1. Is there a true social cost associated with the private consumption of sugary drinks?
- 2. Are a ban on the sale of large-sized drinks or a tax on sugar content reasonable policy solutions?

LEARNING OBJECTIVES

20.1 Social Costs and Benefits

<u>Learning Objective 20.1</u>: Define social costs and benefits.

20.2 Defining Externalities

Learning Objective 20.2: Describe the economic effects of the four categories of externalities.

20.3 How Externalities Lead to Socially Inefficient Outcomes

<u>Learning Objective 20.3</u>: Explain how externalities lead to market failures.

20.4 Methods of Addressing Market Failures

Learning Objective 20.4: Describe methods of addressing positive and negative externalities, and explain how they work.

20.5 The Coase Theorem

Learning Objective 20.5: Describe the Coase theorem and explain how it works with externalities.

20.6 Policy Example

Should New York Ban Soda to Address the Obesity Epidemic?

Learning Objective 20.6: Apply externality concepts to the policy question of banning sugary drinks.

20.1 SOCIAL COSTS AND BENEFITS

Learning Objective 20.1: Define social costs and benefits.

To understand externalities, it is important to first define the concept of social costs and benefits. **Social costs** and **social benefits** are costs and benefits of production or consumption that accrue to everyone in society, including those who are not directly involved in the economic activity. Social costs and benefits are the sum of the private costs and benefits of an economic activity and the *external costs* and *external benefits*: the costs and benefits that accrue to those not directly involved in the economic activity.

A key aspect of external costs and benefits is that they are not reflected in prices. Prices are the private costs of a purchase or the private benefits of a sale.

The archetypical example of an external cost is a factory that, in its production of some good, generates pollution. Examples include smokestack emissions from a coal-fired power plant or a liquid contaminant from a refinery operation that gets into the nearby water or soil.

The owners of the factory pay the private cost of production: the total of all of the costs (including opportunity costs) they have to pay to produce their good. Private cost of production can include the cost of raw materials, energy, labor, rent, pollution controls, and so on. But there is another cost of production for a factory that soils the air or water: the cost to all those who live near the plant and are affected by

the pollution. The *social cost* of production includes both the private cost of production and this *external cost,* the cost that accrues to society and not to the plant owners. Only the plant owners pay the private cost of production, but society as a whole pays the entire social cost.

This is just one example of external costs and benefits. Consumers might also impose external costs through their consumption; for example, a cigarette smoker in a bar pays the private price for smoking in the form of the cost of the cigarette and the cost of their own negative health consequences. But there is also an external cost: the cost to the others in the bar who have to put up with the irritating and smelly smoke as well as potential negative health consequences of secondhand smoke. The smoker pays the private costs but not the external cost, so the social cost of smoking in a bar exceeds the private cost. Another example is the societal cost of treating obesity-related illnesses if a person with such an illness requires public assistance to pay their medical bills.

An example of social benefits in production is the classic story of the beekeeper that lives next to the apple orchard. The beekeeper produces honey and gets a private benefit from the honey: the total revenue of the sale of the honey. But in keeping bees next to the orchard, the beekeeper is also helping increase the apple orchard's harvest of apples through the pollination that the bees facilitate. The extra revenue the owner of the orchard sees from the impact of the neighboring bees does not accrue to the beekeeper and is thus external. The social benefit of an economic activity includes the private benefit and the *external benefit*.

There can be external benefits in consumption as well. Consider a homeowner who buys a lot of flowers and makes a lovely flower garden in their front yard. The homeowner gets a private benefit from the consumption of the flowers, but the neighbors also benefit—the lovely garden not only is pleasing to look at but can cause home values to increase as well. The nicer the street of houses looks, the higher the price a house on the street will command. Here again, then, we have both private and external benefits with the consumption of these flowers for the flower garden.

20.2 DEFINING EXTERNALITIES

Learning Objective 20.2: Describe the economic effects of the four categories of externalities.

Externalities are the costs or benefits associated with an economic activity that affects people not directly involved in that activity. In other words, externalities exist when there are external costs or benefits associated with an economic activity. Externalities can be present in both consumption activities and production activities.

All of the economic actions we take, like driving our cars and maintaining our homes, have private benefits and costs. Driving a car takes gasoline, and you have to pay to maintain and insure your vehicle. Painting your house makes it more attractive, helps prolong its life, and increases its resale value. But many economic activities have associated costs and benefits that accrue to non-users as well. We call these costs and benefits externalities.

Markets are efficient only when all the costs and benefits of an action are private. When external costs and benefits exist, private markets fail to achieve efficiency. The market equilibrium results in too many activities for which there are **negative externalities**, costs imposed on individuals not directly involved in the economic activity. The market equilibrium results in too few activities for which there are **positive externalities**, benefits that accrue to individuals not directly involved in an economic activity.

Externalities can be categorized and doing so makes it easier to identify and analyze them. There are four categories, depending on whether they are positive or negative and consumption or production:

1. Positive production externalities

- Negative production externalities
- 3. Positive consumption externalities
- 4. Negative consumption externalities

The clearest way to understand the effect of externalities relative to the market outcome is to start with the familiar supply-and-demand equilibrium. In a graph of this equilibrium, the supply curve is a private marginal cost (PMC) curve, and the demand curve is a private marginal benefit (PMB) curve.

To go from the private to the true social cost and benefits, which include externalities, we need to account for external marginal costs and marginal benefits by drawing a social marginal benefit (SMB) curve and a social marginal cost (SMC) curve. How do the private marginal benefit (demand) curve and private marginal cost (supply) curve change with externalities?

When negative production externalities are present, to get the social marginal cost curve, we have to add the external marginal cost (EMC) to the private marginal cost (supply) curve. When negative consumption externalities are present, to get the social marginal benefit curve, we have to subtract the EMC from the private marginal benefit (demand) curve. When positive production externalities are present, to get the social marginal cost curve, we have to subtract the external marginal benefit (EMB) from the private marginal cost (supply) curve. When positive consumption externalities are present, to get the social marginal benefit curve, we have to add the EMB to the private marginal benefit (demand) curve.

Note that each externality generates deadweight loss—the difference in the total surplus generated by the private free market and what *should* be generated when we take into account the social costs and benefits. **Table 20.1** summarizes the effects of each type of externality.

| Type of externality | External marginal cost or benefit | Effect on social marginal benefit or cost curve |
|----------------------|-----------------------------------|---|
| Negative production | External marginal cost | Raises the social marginal cost above the supply curve |
| Positive production | External marginal benefit | Lowers the social marginal cost below the supply curve |
| Negative consumption | External marginal cost | Lowers the social marginal benefit below the demand curve |
| Positive consumption | External marginal benefit | Raises the social marginal benefit above the demand curve |

Table 20.1 Effects of externalities

20.3 HOW EXTERNALITIES LEAD TO SOCIALLY INEFFICIENT OUTCOMES

Learning Objective 20.3: Explain how externalities lead to market failures.

Externalities contribute to inefficient economic outcomes. We can begin to see this with a simple example: You are a smart economics student on the eve of an exam. You study until you feel the marginal benefit of extra study is no longer greater than the marginal cost. Part of the marginal cost is the opportunity cost of not listening to music at a high volume, which is your favorite late evening activity. So you close the e-text, put away your economics notes, and crank up the stereo. You have successfully optimized your own utility and, for that alone, deserve an A in economics for the night.

However, you also have a roommate who studies chemistry and has an exam tomorrow. Your roommate still needs to study for a few more hours, and your loud music will make it hard to concentrate. Your loud music listening imparts an external cost to your roommate, or an externality. If you took into account the effect of the music on your roommate, your calculation of the optimal amount of time listening to music would change, as can be seen in **figure 20.1**.

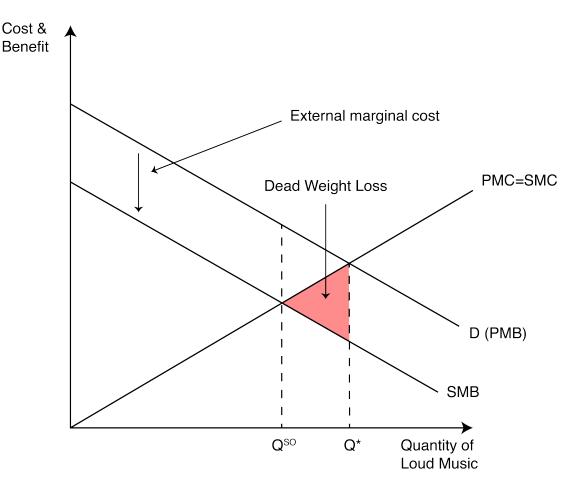


Figure 20.1 Negative consumption externality

In **figure 20.1**, the effect of the loud music can be seen clearly: it imparts an external marginal cost, which we have to subtract from the private marginal benefit to get the social marginal benefit. When the social marginal benefit curve is shifted below the demand curve (PMB), the new intersection between the SMB curve and the supply curve (PMC = SMC) determines the socially optimal amount of loud music, Q^{SO} . This is below the amount of loud music that is delivered by the free market, Q^* . Because too much of the good is consumed, there is deadweight loss, as shown in the pink triangle.

The socially inefficient outcome occurs because the individual economic actor makes decisions based on their private costs and benefits. Rational economic actors, as we have learned, will continue to consume or produce until the private marginal benefit of the activity equals the private marginal cost. These actors do not take into account the costs or benefits their actions have on society. As we will see in the next section, there is a potential role for government to intervene in markets to try to improve efficiency.

As noted earlier, in all cases of externalities, we get deadweight loss. We are now in a position to quantify the deadweight loss associated with externalities and socially inefficient outcomes.

20.4 METHODS OF ADDRESSING MARKET FAILURES

Learning Objective 20.4: Describe methods of addressing positive and negative externalities and explain how they work.

Now that we have mastered the essential idea of externalities, both positive and negative, and seen how their presence can lead to inefficient outcomes—deadweight loss—it is appropriate to think about ways that policy could be used to correct this inefficiency.

Let's start by dividing the externalities into negative and positive, as the policy prescriptions are quite different.

Negative Externalities

We can focus on two characteristics of negative externalities in designing policies to address them:

- 1. In equilibrium, the amount produced or consumed is too high relative to the social optimum.
- 2. In equilibrium, the private marginal cost curve (production externality) or the private marginal benefit curve (consumption externality) does not align with the social marginal cost and benefit curves.

Quantity Controls: Limiting the Economic Activity

One way to address the externality is to focus on the outcome and limit the amount of activity that an economic actor can do. For example, if the production of a good produces harmful pollution, a government could, theoretically, limit the amount of the production of the good to the socially optimal amount. In **figure 20.2**, we can see the socially optimal amount is $Q^{\rm QUOTA}$, so setting a production quota at that point will achieve the socially optimal level.

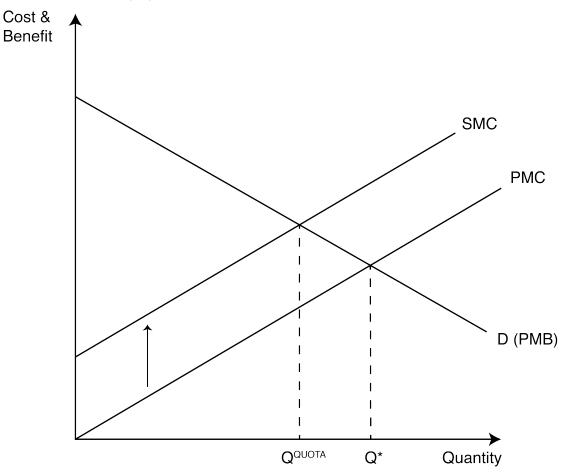


Figure 20.2 Quantity controls to achieve the socially optimal production

Limiting the Externality

Another way to address the externality is to regulate the externality itself. For example, a government could mandate pollution controls for the factory. This has the effect of closing the gap between the private and the social cost because the external cost is lowered. Eventually, if the pollution is eliminated, the negative externality is eliminated as well, and the private marginal cost and the social marginal cost coincide.

Taxes: Adjusting the Cost of the Economic Activity

Both limiting the economic activity and limiting the externality pose challenges. For our pollution example, you have to know a lot about the markets and the available technologies to determine the right quantity of restrictions and pollution controls.

A potentially simpler alternative is to tax the activity so that the private marginal cost equals the social marginal cost or the private marginal benefit equals the social marginal benefit. This type of tax has a special name: a **Pigovian tax**. It is named after the English economist, Arthur Pigou, who first proposed such taxes as a way to restore socially efficient market solutions. **Figure 20.3** shows how a tax equal to the external marginal cost will align the PMC with the SMC and achieve the socially optimal amount of output.

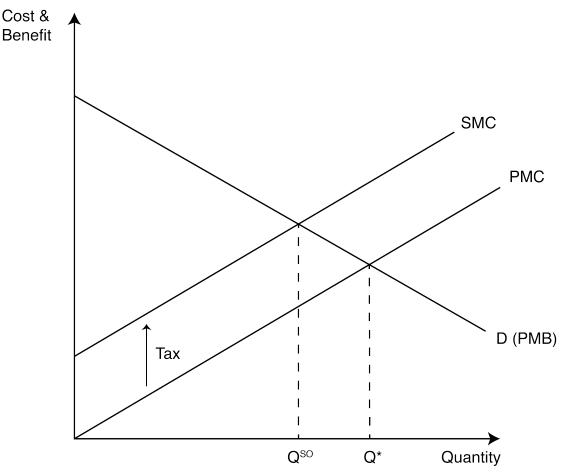


Figure 20.3 Pigovian tax equal to the external marginal cost

Positive Externalities

Again, we can focus on both the failure to produce or consume enough of the economic activity that has a positive externality and the fact that the private marginal benefit is below the social marginal benefit and the private marginal cost is higher than the social marginal cost.

Quantity Controls: Expanding the Economic Activity

It is not generally thought to be the role of the federal government to compel the consumption or the production of a good. For this reason, government-imposed quantity controls are somewhat uncommon. Examples of this type of regulation are laws that compel auto manufacturers to install smog-control equipment or design cars with pedestrian safety features.

At other levels of government, communities often have codes that set minimum standards for property upkeep. Newer planned communities often have covenants that regulate the upkeep of property. Homeowners in these communities are required to follow the covenants. **Figure 20.4** shows how such a quantity control over home maintenance can work to achieve the socially optimal level.

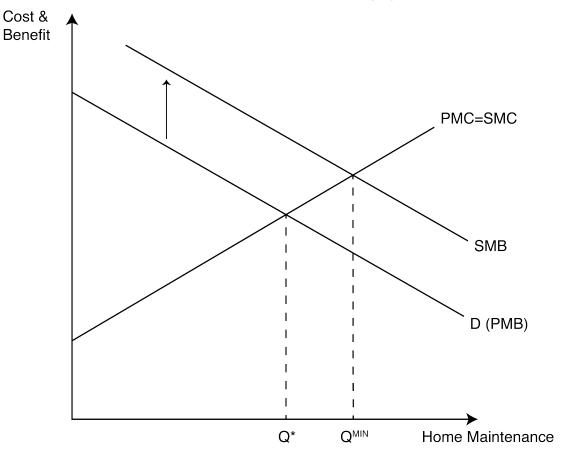


Figure 20.4 Achieving optimal home maintenance with a neighborhood covenant

Tax Credits, Tax Breaks, and Subsidies: Increasing the Benefit of the Economic Activity

Like the case of negative externalities, a potentially simpler alternative to quantity controls is to simply give credits (or tax breaks) for the activity so that the private marginal cost equals the social marginal cost

or the private marginal benefit equals the social marginal benefit. An example is a city credit that store owners can claim if they spend money improving their storefront, as in **figure 20.5**.

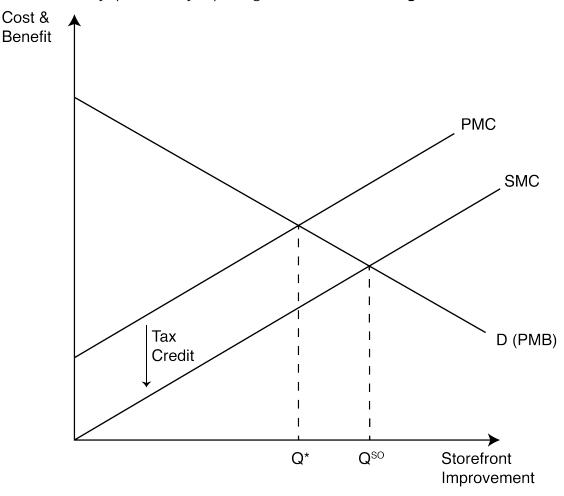


Figure 20.5 Achieving socially optimal storefront maintenance with a tax credit

20.5 THE COASE THEOREM

Learning Objective 20.5: Describe the Coase theorem and explain how it works with externalities.

The common feature of all externalities is that there are costs and/or benefits to economic activity that are not accounted for in the price of the activity. Another way of saying the same thing is that markets for these external costs and benefits do not exist. For example, there is no market for the factory that pollutes to pay for the medical bills of neighbors. In 1960, economist and lawyer Ronald Coase considered what would happen if a market did exist for these costs and benefits.

The way he saw the problem was that **property rights**—the rights to control the use of a good or resource—are not well defined in the case of an air-polluting factory. That is, if neighbors do not have the well-defined right to clean air, there is no incentive for the factory to pay for or take into account the neighbors' medical bills, shorter life-span, and diminished quality of life due to the odor from the factory. The **Coase theorem** states that if property rights are well defined and negotiations among the actors are costless, the result will be a socially efficient level of the economic activity in question. It is one of the most important and influential theorems in economics.

Suppose that the neighbors' combined medical and other costs, per unit of output, are \$10. Suppose also that the marginal private cost of output is constant at \$100 per unit. The marginal social cost is then the \$100 private cost plus the \$10 external cost, or \$110 per unit of output.

Defining clean air as a property right and allowing for free negotiation enables the neighbors to quantify at \$10 their willingness to pay for clean air or, conversely, their willingness to accept the dirty air. So for each unit of output, neighbors will demand to be compensated exactly the amount of their true loss: \$10. Since they have the right to clean air, the factory owners are obliged to pay them, and thus the private cost to the factory owners is exactly equal to the social cost, or PMC = SMC. We know now that this will result in a socially efficient outcome.

Students often are surprised to learn that it does not matter who has the property rights, only that they are well defined. Suppose that the factory owners instead had the right to pollute the air as much as they like. Neighbors would be willing to pay the factory owners \$10 a unit to reduce emissions from the current level. In this scenario, the opportunity cost of producing each extra unit has suddenly increased by \$10. So again, the PMC is now \$110, not \$100; the PMC = SMC; and the socially efficient level of output will result. The transfer of wealth is quite different here, so assigning property rights has big implications in terms of the relative welfare of the groups. But in terms of the socially efficient level of output assignment of property rights has no impact.

You may think that implementing the Coase theorem is an ideal policy solution for externalities, but a few words of caution are in order. The assumption of costless negotiation is quite improbable in practice. In order for it to be true in the example of the polluting factory, the neighbors all have to be able to identify themselves and band together, correctly assess the values of the damage done to them per unit of output and be able to demand the money from the factory owners. Costless negotiation is unlikely to be the case in any similar real-world situation.

An interesting real-world application of the Coase theorem has happened in sparsely populated areas of eastern Oregon, where residents have been paid \$5,000 by a wind-energy company to put up with the noise of wind turbines (residents must sign a waiver promising not to complain about the noise). Oregon law gives the right to peace and quiet to the residents, so for the turbines to exist, the residents must agree to live with the noise. In this case, because the area is sparsely populated and it is pretty easy to determine who is affected (just use a decibel meter), negotiation is relatively easy.

20.6 POLICY EXAMPLE

SHOULD NEW YORK BAN SODA TO ADDRESS THE OBESITY EPIDEMIC?

Learning Objective 20.6: Apply externality concepts to the policy question of banning sugary drinks. Let's return now to the proposed soda ban in New York City, applying the economic tools, concepts, and models from this chapter.

Step 1: Understand the External Cost of the Consumption of "Sugary Drinks"

We need to examine the link between sugary beverages and personal health and well-being. We can then try to relate these personal issues to social costs.

A number of studies have demonstrated a connection between consuming soft drinks and negative health consequences. The following points are from the <u>Harvard School of Public Health</u>:

Sugary drink portion sizes have risen dramatically over the past forty years, and children and adults are drinking more soft drinks than ever.

On any given day, half the people in the United States consume sugary drinks: one in four get at least 200 calories from such drinks, and 5 percent get at least 567 calories—equivalent to four cans of soda. Sugary drinks (soda, energy drinks, sports drinks) are the top calorie source in teens' diets (226 calories per day), beating out pizza (213 calories per day).

Sugary drinks increase the risk of obesity, diabetes, heart disease, and gout.

A twenty-year study on 120,000 men and women found that people who increased their sugary drink consumption by one 12 oz. serving per day gained more weight over time—on average, an extra pound every four years—than people who did not change their intake. Other studies have found a significant link between sugary drink consumption and weight gain in children. One study found that for each additional 12 oz. soda children consumed each day, the odds of becoming obese increased by 60 percent during one and a half years of follow-up.

People who consume sugary drinks regularly—one to two cans a day or more—have a 26 percent greater risk of developing type 2 diabetes than people who rarely have such drinks. Risks are even greater in young adults and Asians.

A study that followed forty thousand men for two decades found that those who averaged one can of a sugary beverage per day had a 20 percent higher risk of having a heart attack or dying from a heart attack than men who rarely consumed sugary drinks. A related study in women found a similar sugary beverage–heart disease link.

A twenty-two-year study of eighty thousand women found that those who consumed a can a day of sugary drink had a 75 percent higher risk of gout than women who rarely had such drinks. Researchers found a similarly elevated risk in men.

And from Mic:

Currently, 58 percent of New York City adults and 40 percent of New York City public school children are overweight or obese.

Other studies have attempted to quantify the social cost of negative health consequences associated with obesity. The following information is from <u>Reuters</u>:

Obese men rack up an additional \$1,152 a year in medical spending, especially for hospitalizations and prescription drugs, John Cawley and Chad Meyerhoefer of Lehigh University reported in January in the *Journal of Health Economics*. Obese women account for an extra \$3,613 a year. Using data from 9,852 men (average BMI: 28) and 13,837 women (average BMI: 27) ages twenty to sixty-four, among whom 28 percent were obese, the researchers found even higher costs among the uninsured: annual medical spending for an obese person was \$3,271 compared with \$512 for the non-obese.

Nationally, that comes to \$190 billion a year in additional medical spending as a result of obesity, calculated Cawley, or 20.6 percent of US health care expenditures.

Those extra medical costs are partly borne by the non-obese, in the form of higher taxes to support Medicaid and higher health insurance premiums. Obese women raise such "third-party" expenditures to \$3,220 a year each, and obese men, \$967 a year, Cawley and Meyerhoefer found.

In addition, there have been studies about the extra cost of heavier drivers on the roads in terms of road wear and tear and extra fuel use. There is also this: an obese man is 64 percent less likely to be arrested for a crime than a healthy man.

For the sake of our exercise, let's accept the link between sugary drinks and social costs.

Step 2: Categorize the Externality

In this case, we have a classic negative consumption externality—there is an external cost to an individual's consumption of the good, and therefore the social marginal benefit is lower than the private marginal benefit.

Step 3: Show the Social Inefficiency in Terms of Deadweight Loss

Because this consumption activity, drinking sugary drinks, is associated with external costs, the socially optimal level of consumption is lower than the market outcome. This results in deadweight loss. We can see the deadweight loss in figure 20.6.2.

Step 4: Consider Whether the Solution Will Have the Desired Effect

How do we incorporate the large soda ban into the model? What this ban does is increase the cost per ounce for producers. How? Well, it is cheaper to sell in bulk (see <u>chapter 8</u>), so if producers are forced to sell in smaller packages, the cost per ounce will increase. This effect will raise the private marginal cost (supply) curve. If you raise it enough, you can reduce soda consumption to the socially optimal level.

But in the real world, we don't always have a good idea of where to stop the private marginal cost. Is this added cost proportional to the external cost? Is it greater or less than the external cost?

From this exercise, we can conclude that the policy has the potential to achieve its aims, but there is a question about the magnitude of the effect of the policy relative to the magnitude of the cost of the problem.

Step 5: Consider Possible Policy Alternatives

What about an outright ban on sugary drinks? This clearly would go too far in the sense that it is well below the socially efficient level of drink consumption.

A Pigovian tax on sugary drinks seems like a much simpler policy. In fact, this is a common and popular policy solution to other goods that produce negative externalities, like cigarettes and alcohol. But again, the challenge is to get the amount of the tax right so that the socially efficient level is reached.

EXPLORING THE POLICY QUESTION

- 1. Do you think the ban on the sale of sugary drinks in large quantities is a good idea from a policy perspective? Why or why not?
- 2. Do you think such a ban would have the desired effect?
- 3. Reading the articles above, how much discretion do you think local authorities should have to address externalities?
- 4. Do you think the true nature of this problem is an external cost that consumers don't take into account when making consumption choices, or is it more a question of ignorance about the potential negative health consequences? If the latter, can you think of alternate policy solutions?

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

20.1 Social Costs and Benefits

<u>Learning Objective 20.1</u>: Define social costs and benefits.

20.2 Defining Externalities

Learning Objective 20.2: Describe the economic effects of the four categories of externalities.

20.3 How Externalities Lead to Socially Inefficient Outcomes

Learning Objective 20.3: Explain how externalities lead to market failures.

20.4 Methods of Addressing Market Failures

Learning Objective 20.4: Describe methods of addressing positive and negative externalities and explain how they work.

20.5 The Coase Theorem

Learning Objective 20.5: Describe the Coase theorem and explain how it works with externalities.

20.6 Policy Example

Should New York Ban Soda to Address the Obesity Epidemic?

Learning Objective 20.6: Apply externality concepts to the policy question of banning sugary drinks.

LEARN: KEY TOPICS

Terms

Social cost

Social costs are costs of production or consumption that accrue to everyone in society, including those who are not directly involved in the economic activity. The social cost of production includes both the private cost of production and this *external cost*, the cost that accrues to society and not to the plant owners. Only the plant owners pay the private cost of production, but society as a whole pays the entire social cost.

Social benefit

Social benefits are benefits of production or consumption that accrue to everyone in society, including those who are not directly involved in the economic activity. An example of social benefits in production is the classic story of the beekeeper that lives next to the apple orchard. The beekeeper produces honey and gets a private benefit from the honey: the total revenue of the sale of the honey. But in keeping bees next to the orchard, the beekeeper is also helping increase the apple orchard's harvest of apples through the pollination that the bees facilitate. The extra revenue the owner of the orchard sees from the impact of the neighboring bees does not accrue to the beekeeper and is thus external. The social benefit of an economic activity includes the private benefit and the *external benefit*.

Externalities

Externalities are the costs or benefits associated with an economic activity that affects people not directly involved in that activity. In other words, externalities exist when there are external costs or benefits associated with an economic activity. Externalities can be present in both consumption activities and production activities.

Property rights

Property rights are the rights to control the use of a good or resource.

Coase theorem

The Coase theorem states that if property rights are well defined and negotiations among the actors are costless, the result will be a socially efficient level of the economic activity in question.

Graphs



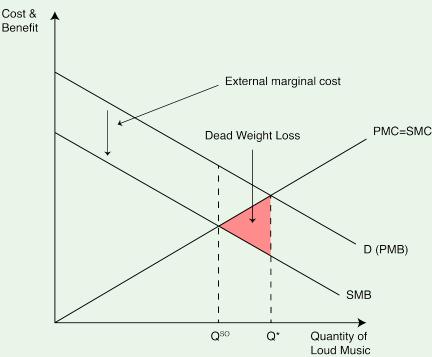


Figure 20.1 Negative consumption externality

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CHAPTER 21

Public Goods

THE POLICY QUESTION

SHOULD THE GOVERNMENT REGULATE THE EXTRACTION OF FISH FROM THE OCEAN IN WATERS WITHIN TEN NAUTICAL MILES OF THE US SHORELINE?

EXPLORING THE POLICY QUESTION

- 1. Does the societal benefit from the advent of new drugs outweigh the cost to society from the creation of monopolies?
- 2. What other way could society promote the development of new medicines?

LEARNING OBJECTIVES

21.1 What Is a Public Good?

Learning Objective 21.1: Describe the two key features of a public good.

21.2 The Free-Rider Problem

Learning Objective 21.2: Explain how public goods lead to overuse.

21.3 Problems with the Public Provision of Public Goods

Learning Objective 21.3: Describe the problem of under-provision of public goods.

21.4 Policy Example

Policing Fish Extraction within 10 Nautical Miles of the US Shoreline

Learning Objective 21.4: Explain how the application of property rights can help solve the free-rider problem in fisheries.

21.1 WHAT IS A PUBLIC GOOD?

Learning Objective 21.1: Describe the two key features of a public good.

Public goods are goods that have some degree of non-rivalry and non-excludability. **Rival goods** are goods that are diminished with use. An example of a rival good is a sandwich. When someone consumes

a sandwich, that sandwich is gone, and no one else can consume it. Non-rival goods are goods that do not diminish with individual consumption; for example, no amount of consumption of the music from a radio station leaves any less music for anyone else with a radio to listen to. Clean air, national defense, and lighthouses are other classic examples of non-rival goods. **Exclusive goods** are goods for which consumption can be controlled or prevented. The sandwich behind the deli counter in a market is an exclusive good; consumption can only happen if the deli workers allow it. Non-exclusive goods are things like the roads and parks in a city; anyone can drive on the roads or enjoy the park. Fisheries are another example of non-excludability.

Private goods are, like the sandwich, goods that are both rival and exclusive. What this textbook has been discussing all along are private goods. But what happens when the goods have some non-rivalry and/or some non-excludability? Public goods like these are subject to market failures. For example, suppose someone tried to charge a price for a radio transmission. The result would be that no one would pay that price because they can get the radio signal for free, and there is no way to stop those that didn't pay from receiving the signal. This is known as the **free-rider problem**—when non-payers consume a good that has a positive marginal cost.

We can classify goods based on the presence of rivalry and excludability, as is shown in **table 21.1** below. We divide goods into four categories:

1. Private Goods

Goods that have both rivalry and exclusion (and are the type of goods we have studied up to this point)

2. Public Goods

Goods that are both non-excludable and non-rival

3. Club Goods

Goods that are excludable but non-rival; and

4. Common Property/Common-Pool Resources

Goods that are rival but non-excludable.

Table 21.1 Goods based on the presence of rivalry and excludability

| | Excludable | Non-excludable | |
|-----------|---|--|--|
| Rival | Private goods: sandwich, gasoline, computer | Common property resources: fishery, roads, parks | |
| Non-rival | Club goods: satellite radio, cable TV, sporting event | sporting event Public goods: clean air, national defense, lighthouse | |

We also distinguish between pure public goods, goods that are completely non-rival and non-excludable like radio transmissions, and impure public goods, which have at least some of both non-rivalry and non-excludability. City roads are an example of an impure public good; they are non-excludable but not perfectly non-rival—each car takes up a little of the road space, leaving just a tiny bit less for others.

21.2 THE FREE-RIDER PROBLEM

Learning Objective 21.2: Explain how public goods lead to overuse.

Public goods are both non-rival and non-exclusive. For example, national defense is a public good. All residents of a country enjoy the protection of military defense of the territory; no one is excluded or

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excludable. And no matter how much one individual consumes of national defense, there is just as much national defense of the other residents of the country, so it is non-rival.

Market failures in the provision of public goods arise for a very simple reason: since non-payers cannot be prevented from consuming the good, the incentives to pay for the good are diminished. We call this problem the **free-rider problem**. It is easy to understand this when we think about individual incentives. Utility for the consumption of a public good is increased the less the consumer pays for it.

We can illustrate this with a simple example of two neighbors with adjacent properties considering erecting a fence between their properties to provide privacy. Neighbor 1 is a private person and someone who values privacy very highly. Neighbor 2 is someone who values privacy but much less than neighbor 1. **Figure 21.1** shows the demand curves for the two neighbors of the length of the privacy fence in meters. D^1 is Neighbor 1's demand curve, and D^2 is Neighbor 2's demand curve. These demand curves represent the value to each neighbor of a meter of fence. By adding these two values together, we get the true social benefit of the fence, and we can show this in the figure as the vertical sum of the two demand curves, which is labeled D^{SB} , where SB stands for social benefit. For example, to erect a ten-meter fence, Neighbor 1 is willing to pay \$30 a meter, and Neighbor 2 is willing to pay \$20 a meter. The social willingness to pay for the shared fence is the sum of the two individual's willingness to pay, or \$50. Notice immediately that the social marginal benefit of the good is not the same as the private marginal benefits for either neighbor.

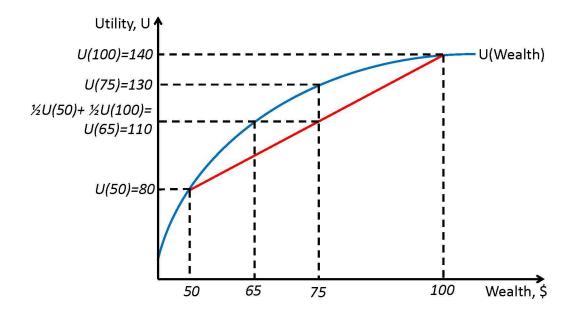


Figure 21.1 The free-rider problem and the underprovision of public goods

Contrast this with a private good, where consumption benefits only the buyer, and therefore, the social marginal benefit is the same as the private marginal benefit. Recall that when determining the total demand or the social marginal benefit curve for the market for a private good, we sum the individual demand curves *horizontally* because the benefit to a consumer only comes from when they consume their own private units of the good. The difference here is the lack of rivalry: the same unit of a public good benefits all consumers in the market. So we have to add up all the individual benefits for each unit of the public good or sum the demand curves *vertically*.

Fences are costly, however, and we will assume that the cost per meter of erecting a fence is \$50. This is the marginal cost of fencing and is the social marginal cost, since that is the total cost to the two neighbors of erecting a meter of fence.

The socially optimal amount of fencing for the two neighbors is the point at which the social marginal benefit of the fence, given by the demand curve D^{SB} , intersects with the marginal cost of the fence. In figure 21.1, this intersection occurs at ten meters.

To understand what will actually occur, notice that the individually optimal amount of fencing for Neighbor 1 is six meters. In other words, if the neighbor was going to build a fence individually, six meters is the amount that neighbor would build. Neighbor 2 would not build any fence individually, as the marginal cost of building is higher than the marginal benefit, even for the first meter of fence. Since Neighbor 2 does not want to collaborate on the fence, Neighbor 1 will build it alone and will build six meters of fence, and Neighbor 2 will enjoy the benefit of the fence without contributing to it. We see in this example how the private provision of public goods is subject to under-provision: Neighbor 2 free rides off Neighbor 1's fence, and thus only six meters of fencing is constructed, while ten meters is socially optimal.

To ensure public goods are provided, governments usually step in and provide the good themselves or subsidize or mandate its provision. An example is local fire departments. Fire protection is a classic public good; all those in the fire district benefit from the service, and the protection of one household leaves no less for the other households in the district. Left to the market, we can be confident that a sub-optimal amount of fire protection would be provided, thus it becomes part of the accepted role of the government to levy a tax on homeowners and provide fire protection themselves.

21.3 PROBLEMS WITH THE PUBLIC PROVISION OF PUBLIC GOODS

Learning Objective 21.3: Describe the problem of under-provision of public goods.

In order to value public goods, you must look beyond the market valuation. Because of the presence of free ridership, the market will undervalue public goods. Alternatively, governments can rely on surveys, but these types of surveys are often poor because it is very hard to judge the value of a public good to an individual. An individual might be able to answer how much they would be willing to pay for a proposed new park in their neighborhood, but how much is the police protection they enjoy worth? Without knowing what life would be like in the absence of a police force, that is a very difficult question to answer. Other things for which individuals lack enough information to value correctly could include clean air and drinking water, national defense, and public education.

Another way to both value and potentially provide public goods is through a popular vote. This seems to be a reasonable solution on the surface, but upon examination, it is clear that the ability of such a system to provide public good rests pivotally on the median voter.

Consider the following example: suppose a town on a river is considering building a bridge over the river. To keep the analysis simple, let's assume a simplified world where there are five residents of the town, and the bridge costs exactly \$1,000 to construct. The bridge is worth different amounts to each resident depending on factors such as income, how close they live to the bridge, how often they anticipate using the bridge, and so on. **Table 21.2** lists each resident and their maximum willingness to pay for a bridge, which is a measure of the monetary value to them of the bridge.

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Table 21.2 Resident's willingness to pay for a new bridge

| Resident ID | Willingness-to-pay price (\$) |
|------------------------|-------------------------------|
| Resident A | \$500 |
| Resident B | \$350 |
| Resident C | \$175 |
| Resident D | \$150 |
| Resident E | \$125 |
| Total Value to Society | \$1,300 |

Note that the total value to the society of the new bridge is \$1,300, which is more than the cost of \$1,000, and so from a social welfare perspective, the bridge should be built—the community will see a net benefit from doing so. Suppose the town proposes a tax of \$200 on each resident, which would net exactly the \$1,000 needed to build the bridge. When put to a vote, this proposal will fail because Residents C, D, and E will all vote no: the \$200 they are being asked to pay is greater than their individual benefit. Note that the pivotal voter in this is Resident C. If Resident C's willingness to pay were \$200 or more, they would vote yes. Resident C is the median voter, halfway from the top and bottom, and the construction of the bridge will rest crucially on their valuation relative to the individual cost.

It is also worth noting that other means of provision in this case are also problematic. Voluntary contributions would fall prey to the free-rider problem, as C, D, and E all know that their contributions are not needed provided the others contribute fully and will therefore withhold. A toll would have to raise the \$1,000 cost and thus would be the equivalent of the \$200 tax. In this case, the "voting" would happen by use: only A and B would pay \$200 to use it, and the toll revenues would fall far short of the cost of the bridge.

If these willingnesses-to-pay were closely related to income, then charging a tax as a percentage of income might work, but if they have more to do with proximity, work-travel patterns, and so on, this approach would fail as well. So how do public goods get provided in most cases? Out of general funds from the government. By packaging together a whole host of public goods, including roads, parks, schools, libraries, public safety, and the like, governments can average out individual differences related to preferences and create broad support for the funding of these activities.

21.4 POLICY EXAMPLE

SHOULD THE GOVERNMENT REGULATE THE EXTRACTION OF FISH FROM THE OCEAN IN WATERS WITHIN TEN NAUTICAL MILES OF THE US SHORELINE?

Learning Objective 21.4: Explain how the application of property rights can help solve the free-rider problem in fisheries.

When fishing boats set out on the ocean and decide how many fish to catch, like any economic actor, they make a marginal benefit, marginal cost calculation. They will continue to fish as long as their private marginal benefit, the value of the next fish caught, equals the private marginal cost, the expense of catching the last fish. As a common-pool resource, however, there is a social cost to the boat's catch that is not part of their calculation: the fact that the more fish they catch, the fewer fish there are for others to catch. In addition, fisheries need a healthy population of mature fish to remain uncaught so that those fish can reproduce and provide fish to catch next season.

In this situation, the private marginal cost and the social marginal cost differ due to the cost of depleting the fishery from one fishing boat's catch. Without regulation, each individual boat will catch more than the socially optimal amount, leading to deadweight loss.

With the application of property rights—typically a quota system that assigns the right of an individual fishing boat to catch only a limited amount of fish—the socially optimal amount of fish extraction is established.

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

21.1 What Is a Public Good?

Learning Objective 21.1: Describe the two key features of a public good.

21.2 The Free-Rider Problem

Learning Objective 21.2: Explain how public goods lead to overuse.

21.3 Problems with the Public Provision of Public Goods

Learning Objective 21.3: Describe the problem of under-provision of public goods.

21.4 Policy Example

Policing Fish Extraction within 10 Nautical Miles of the US Shoreline

Learning Objective 21.4: Explain how the application of property rights can help solve the free-rider problem in fisheries.

LEARN: KEY TOPICS

Terms

Public goods

Public goods are goods that have some degree of non-rivalry and non-excludability. We also distinguish between pure public goods, goods that are completely non-rival and non-excludable like radio transmissions, and impure public goods that have at least some of both non-rivalry and non-excludability. City roads are an example of an impure public good, they are non-excludable but they are not perfectly non-rival, each car takes up a little of the road space leaving just a tiny bit less for others.

Rival goods

Rival goods are goods that are diminished with use. An example of a rival good is a sandwich, when someone consumes a sandwich that sandwich is gone and no one else can consume it. Non-rival goods are goods that do not diminish with individual consumption, for example no amount of consumption of the music from a radio station leaves any less music for anyone else with a radio to listen to. Clean air, national defense and lighthouses are other classic examples of non-rival goods.

Exclusive goods

Exclusive goods are good for which consumption can be controlled or prevented. The sandwich behind the deli counter in a market is an exclusive good, consumption can only happen if the deli workers allow it. Non-exclusive goods are things like the roads and parks in a city where anyone can drive on the roads or enjoy the park. Fisheries are another example of non-excludability.

Private goods

Private goods are goods that are both rival and exclusive.

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CHAPTER 22

Asymmetric Information

THE POLICY QUESTION

SHOULD THE GOVERNMENT MANDATE THE PURCHASE OF HEALTH INSURANCE?

A key component of the Affordable Care Act, passed by Congress and signed into law by President Obama in 2010, was the individual mandate. This compelled individuals to purchase health insurance or face a large financial penalty. This provision proved to be the most controversial of the new law, yet many economists believed it to be the crucial piece that guaranteed the success of the new law.

EXPLORING THE POLICY QUESTION

- 1. Why do many economists think it essential that the individual mandate be a part of the Affordable Care Act?
- 2. Is the individual mandate the only way to achieve universal health insurance? What other ways do societies accomplish this?

LEARNING OBJECTIVES

22.1 The Market-for-Lemons Problem

Learning Objective 22.1: Describe the lemons problem in markets with asymmetric information.

22.2 Adverse Selection

Learning Objective 22.2: Explain the term adverse selection and how it affects insurance markets.

22.3 Principal-Agent Models

<u>Learning Objective 22.3</u>: Describe how asymmetric information can affect principal-agent relationships.

22.4 Moral Hazard

Learning Objective 22.4: Explain moral hazard and how it can affect the efficiency of markets.

22.5 Policy Example
The Affordable Care Act

<u>Learning Objective 22.5</u>: Explain how adverse selection models explain the importance economists place on the individual mandate in the Affordable Care Act.

22.1 THE MARKET-FOR-LEMONS PROBLEM

Learning Objective 22.1: Describe the lemons problem in markets with asymmetric information.

One of the assumptions of the efficient-markets hypothesis is that buyers and sellers are completely informed; they know everything there is to know about the goods for sale in a market, like their quality. This is critical for achieving efficiency, since a buyer's willingness to pay for a good depends on them knowing the value of the good to themselves. If a buyer, for example, overestimates the value of a good to themselves, perhaps by over-estimating its quality, then they might end up buying it at a price that exceeds their willingness to pay for the good once its quality is revealed. This would be an exchange that lowers total surplus, and the market cannot therefore be efficient.

Asymmetric information describes a situation where one side of an exchange, the buyer or the seller, knows more about the product than the other. Generally, we might expect the sellers of goods to know more about them than buyers, but not always—a collector of antiques might know more about the value of an item they see for sale by someone who found an old item in their attic. Items whose value is not immediately known to a buyer or seller are said to have **hidden characteristics**. Asymmetric information can also arise when agents' actions are not visible to all parties. For example, a customer may hire a mechanic to fix their car, but they do not observe the actions the mechanic actually takes. The mechanic might say they replaced a part when, in fact, they did not. We call these **hidden actions**.

In situations where both parties to a transaction have the same information, either full or partial information, neither party has an advantage over the other. However, when one party has access to more information, this can lead to opportunistic behavior, where the more informed party takes advantage of the less informed party for economic gain. This advantage taking leads to market failures where transactions fail to yield efficient outcomes. Two main problems associated with asymmetric information are **adverse selection** and **moral hazard**. Adverse selection refers to the situation where asymmetric information on the part of one party in an economic transaction leads to the desirable good remaining unsold, even though it would be sold in a market with full information.

The classic example of this is called the market for lemons, after <u>George Akerlof's 1970 paper</u> of the same name. In this scenario, sellers of used cars possess more information about the true quality of the cars than sellers do, since the owners of used cars have been using them and know their faults. In a simplified version of this model, consider a world in which there are only two types of cars: good quality cars and bad quality cars (or "lemons," which in the United States is slang for a bad car). There are equal numbers of both in the marketplace, and both buyers and sellers know this. Buyers value good used cars at \$10,000 and lemons at \$5,000. Sellers are willing to sell good used cars for \$8,000 and lemons for \$3,000. For clarity, let's suppose that there are exactly one hundred cars of each type and over two hundred buyers, each willing to buy either car, given the right price.

Immediately, we can see that in a world of full information, an efficient outcome will arise: owners of good cars will sell them at a price between \$8,000 and \$10,000, and owners of lemons will sell them at a price between \$3,000 and \$5,000. Each car sold will generate a total of \$2,000 in total surplus regardless

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of the price agreed to, as this is the difference between the sellers' minimum willingness to accept and the buyers' maximum willingness to pay. In the end, the sale of two hundred cars will yield a total surplus of \$400,000 (or two hundred cars times \$2,000 surplus for each).

Now consider a world of asymmetric information, where the sellers know the quality of the cars they are selling but the buyers do not. Sellers of both types of cars have an incentive to claim that their cars are of good quality. Buyers understand the incentive to misrepresent the true quality of the car and therefore do not believe the sellers' claims. So what happens in the market? Let's keep things simple by assuming that buyers are risk neutral. In this case, the buyers know that with equal amounts of both types of cars in the market, choosing one at random will yield an expected value of \$7,500.

```
Probability of a good car = .5, value of a good car = $10,000
Probability of a bad car = .5, value of a lemon = $5,000
Expected value = (.5)(\$10,000) + (.5)(\$5,000) = \$7,500
```

This means that no buyer is willing to pay more than \$7,500 for a used car. Since this is true, no seller of a good car is willing to sell, as \$7,500 is lower than their minimum willingness to accept. Because of this, no owner of a good-quality used car will sell it, and the only cars for sale on the market will be the lemons. Both buyers and sellers can figure this out, and in the end, buyers know that only lemons are for sale and will not offer more than \$5,000. This leaves a market for only lemons in which all one hundred lemons will be sold for a price between \$5,000 and \$3,000. Each transaction generates \$2,000 in total surplus for a total of \$200,000. This is the market failure: the asymmetric information problem leads to a deadweight loss of \$200,000, or the difference between the total surplus in the full information market-place and the total surplus in the market with asymmetric information.

The fact that the good-quality cars disappear from the market is called **adverse selection**, a topic we will focus on in the next section.

22.2 ADVERSE SELECTION

Learning Objective 22.2: Explain the term adverse selection and how it affects insurance markets.

Adverse selection occurs when the more desirable attributes of a market withdraw due to asymmetric information. This could be better-quality products, better-quality consumers, or better-quality sellers. The result is that consumers and producers may not make transactions that are socially beneficial, transactions that would yield positive producer and/or consumer surplus. This is the market failure associated with asymmetric information: the ability of the more informed agents to exploit their advantage.

Insurance markets are a classic example of market failures from information asymmetries. Information asymmetries exist in insurance markets due to the fact that there is both **hidden action** and **hidden characteristics**: insurers cannot monitor the actions and private information of the insured. For example, in car insurance, the insurer does not know how carefully a driver actually drives. In health insurance, the insurer might not know about pre-existing conditions and the lifestyle of their insured. Because of this information asymmetry, insurers have to charge a price that is an average of the costs of their insured. This price is often too high for the most desirable consumers, causing them to not purchase insurance. This decision to stay out of the market makes the situation worse, as the average cost of the insured increases as the lowest cost consumers exit, further raising the price of insurance and forcing even more of the healthier consumers from the market.

This outcome is inefficient because if insurance companies had full information about their clients, they could charge each a price that is above the cost of insurance but is less than the risk premium—the

amount above the cost that consumers are willing to pay to avoid risk—that would allow these healthier clients to purchase insurance and create more surplus in society.

22.3 PRINCIPAL-AGENT MODELS

Learning Objective 22.3: Describe how asymmetric information can affect principal-agent relationships. **Principal-agent relationships** are situations in which one person, the principal, pays another person to perform a task for them. In its most basic form, this describes the employee-employer relationship. But it can also describe a situation in which a car owner pays a mechanic to fix their car, a homeowner hires a housecleaner, or many other everyday situations. These relationships are often subject to asymmetric information because agents can act in ways that are unobserved by the principal. If the individual incentives are not aligned, the agents might take actions contrary to the interests of the principal. For example, the owner of a car in need of repair would like the car to be repaired properly and as inexpensively as possible. The mechanic's incentives might be to repair the car properly but to maximize their revenue from the situation. So, for example, the mechanic might like to perform extra, unnecessary work in order to earn more money. Since the car owner does not know that the extra work is unnecessary, the mechanic can claim it is and earn the extra revenue. Similarly, an employer's incentive is to have each employee work hard and efficiently. But a worker's incentive might be to expend as minimal an effort as possible but still perform their assigned duties. If the employer cannot detect that the employee is not giving their maximum effort, the employee is free to give a diminished effort. In these situations, it would be unsurprising for employees to give less than their full effort.

The key to these situations of misaligned incentives is the presence of **hidden actions**: efforts (or lack thereof) on the part of one or both parties that are unobserved by the other. For example, if a job simply requires an agent to put two component pieces of a computer together on an assembly line, the principal can presumably observe the agent's actions by monitoring the number of parts they assemble in an hour. They can also test to make sure the connection of each set of two parts is good. In this case, it is easy to write a contract to align incentives: specify the number of parts the agent is required to join properly in an hour. But consider the situation where the principal cannot observe the effort of the agent. For example, in retail sales, it might be difficult to observe each interaction with customers. We call these hidden actions, and they make it difficult or impossible to write a contract specifying a particular level of effort.

Principal-agent relationships where there is hidden action can be addressed through contracts that seek to align incentives through rewarding performance instead of effort. A typical one in the case of retail sales is through the use of commissions, where the agent gets a percentage of every sale they make (or a percentage of sales over a certain threshold). This helps align the incentives of the principal, to make as much revenue as possible, with the agent, who, with a commission contract, would like to maximize the value of their own sales. Other examples are CEO pay, where the CEO of a company is compensated partially based on the performance of the firm itself.

22.4 MORAL HAZARD

Learning Objective 22.4: Explain moral hazard and how it can affect the efficiency of markets.

Another consequence of hidden action is **moral hazard**, where people who have entered into contract to mitigate the cost of risk engage in riskier behavior because the costs have diminished. An insurance contract that covers the cost of damage from an automobile collision might cause the holder of the contract to drive in a less cautious manner, increasing the risk of an accident. Borrowers who have limited liability contracts might be more willing to take risks with the money they borrow. If the actions of the

contract holder could be monitored, the problem would go away, as the contract could be written to take behavior into account and either prohibit it or charge a price based on the nature of the actions the contract holder engages in. It is the hidden action aspect of these contracts that gives rise to moral hazard.

The consequence of contracts that reduce the cost of risk-taking and therefore increase the incentives to take risks is that they become more expensive. An insurer who sells auto insurance will have to charge higher premiums as a consequence of moral hazard because its costs go up with riskier driving on the part of the policyholders. This causes premiums to go up for all holders, making it too expensive for the most careful drivers and causing a market failure.

22.5 POLICY EXAMPLE

THE AFFORDABLE CARE ACT

Learning Objective 22.5: Explain how adverse selection models explain the importance economists place on the individual mandate in the Affordable Care Act.

Social insurance contracts like the Affordable Care Act rest on the principle that adverse events, like an injury, accident, or health crisis, can happen to anyone and that by pooling resources, the unlucky can be cared for from the shared resources of society. When participation isn't universal, the cost to the participants depends on the average risk of the insured. If optional, adverse selection tells us who is the most likely to stay in the pool and who is most likely to leave, the most risky and the least risky, respectively. This will increase the cost of insurance for those who remain and threaten the viability of the system as care becomes less "affordable."

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

22.1 The Market-for-Lemons Problem

Learning Objective 22.1: Describe the lemons problem in markets with asymmetric information.

22.2 Adverse Selection

Learning Objective 22.2: Explain the term adverse selection and how it affects insurance markets.

22.3 Principal-Agent Models

Learning Objective 22.3: Describe how asymmetric information can affect principal-agent relationships.

22.4 Moral Hazard

Learning Objective 22.4: Explain moral hazard and how it can affect the efficiency of markets.

22.5 Policy Example The Affordable Care Act

<u>Learning Objective 22.5</u>: Explain how adverse selection models explain the importance economists place on the individual mandate in the Affordable Care Act.

LEARN: KEY TOPICS

Terms

Hidden characteristics

Items whose value is not immediately known to a buyer or seller are said to have hidden characteristics.

Hidden action

When agents' actions are not visible to all parties (for example, a customer may hire a mechanic to fix their car, but they do not observe the actions the mechanic actually takes), we call these hidden actions.

Adverse selection

Adverse selection refers to the situation where asymmetric information on the part of one party in an economic transaction leads to the desirable good remaining unsold, even though it would be sold in a market with full information.

Moral hazard

Another consequence of hidden action is moral hazard, where people who have entered into contract to mitigate the cost of risk engage in riskier behavior because the costs have diminished.

Principal-agent relationships

Principal-agent relationships are situations in which one person, the principal, pays another person to perform a task for them.

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CHAPTER 23

Uncertainty and Risk

THE POLICY QUESTION

SHOULD THE US GOVERNMENT PROVIDE FLOOD INSURANCE?

Much insurance is provided by the private market, but one important exception is flood insurance, which is generally provided by the federal government in the United States. The country's National Flood Insurance Program is run by the Federal Emergency Management Agency and provides supplemental flood insurance for flood-prone homes, as most private homeowner policies do not cover flood damage.

EXPLORING THE POLICY QUESTION

- 1. Why don't private insurers provide flood insurance?
- 2. What is the justification for government provision of flood insurance?

LEARNING OBJECTIVES

23.1 What Are Risky Outcomes?

Learning Objective 23.1: Define risky outcomes, and describe how they are assessed.

23.2 Evaluating Risky Outcomes

Learning Objective 23.2: Explain expected utility and risk preference.

23.3 Risk Reduction

<u>Learning Objective 23.3</u>: Describe how diversification and insurance mitigate risk.

23.4 The Policy Question

Should the US Government Provide Flood Insurance?

<u>Learning Objective 23.4</u>: Apply knowledge of risk and insurance to explain how systematic risk makes risk pools difficult and destroys private markets for insurance.

23.1 WHAT ARE RISKY OUTCOMES?

Learning Objective 23.1: Define risky outcomes, and describe how they are assessed.

Risk describes any economic activity in which there are uncertain outcomes. For example, a person who places a bet on the flip of a coin faces two different outcomes with equal chance. A driver of a car knows that there is a chance of a collision. People understand that in the future, there is a possibility that they will fall ill or suffer an injury that requires medical attention. All of these scenarios are examples of uncertainty, and uncertainty implies risk. For this chapter, as in economics in general, we use the terms *risk* and *uncertainty* interchangeably.

Associated with any uncertain outcome are probabilities. Recall that **probabilities** are numbers between zero and one that indicate the likelihood that a particular outcome will occur. In a coin flip, the probability of one side landing facing up is one-half, or 50 percent. Sometimes these probabilities are known, like in the coin-flipping example, and sometimes these probabilities are unknown, like in the carcollision example. Even when we don't know the probabilities, we can often estimate based on aggregate data or some other information, such as if the roads are covered in snow. In either case, the ability to assign probabilities distinguishes these risks as quantifiable. We will only consider quantifiable risk in this chapter.

In the absence of a known probability like a coin flip, economic agents have to estimate. They generally do so in two ways: they can estimate based on frequency or based on subjective probability. **Frequency** is how often a particular outcome has occurred over a known number of events. For example, a person who lives in an area that only rarely gets snow in the winter might wonder what the chances are that there will be snow this winter. They might remember that in the last ten years, it has snowed in three of them. Therefore, they might estimate the probability of snow this year based on its annual frequency, 3/10, or 3/10, or 3/10 percent. Formally, if 3/10 equals the number of times an event has occurred and 3/10 equals the number of times possible, then the frequency, 3/10, equals

$$F = \frac{k}{N}$$
.

Subjective probability is when individuals estimate probabilities based on their own experiences and whatever data are available to them. For example, a homeowner might not have ever experienced a house fire but might make an inference about how likely they are based on their own knowledge of fires in their community and reports of fires they see in the news. A weather forecaster is also making a subjective probability estimate when forecasting a chance of rain. They look at the data and models available to them but use their own experience as a guide on how to interpret the data and model predictions and make their own assessments.

If there are multiple possible outcomes, probabilities can be assigned to each one. The **expected value** of an uncertain outcome is the sum of the value of each possible outcome multiplied by the probability it will occur. For example, consider a jar of one hundred marbles of four different colors: red, blue, green, and yellow. If there are forty red marbles, twenty blue marbles, thirty green marbles, and ten yellow marbles, then the probability of randomly drawing a red one is .4 (40/100), a blue one is .2, a green one is .3, and a yellow one is .1. Suppose also that red ones are worth \$10, blues ones are worth \$50, green are worth \$20, and yellow are worth \$100. The expected value (EV) of one random draw is

$$EV = Pr(Red) \times Value(Red) + Pr(Blue) \times Value(Blue) + Pr(Green) \times Value(Green) + Pr(Yellow) \times Value(Yellow)$$

or

$$EV = .4 \times \$10 + .2 \times \$50 + .3 \times \$20 + .1 \times \$100 = \$30$$

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The expected value from the marble game is the amount one could expect to earn on average if the game is repeated many times. The average outcome of the marble game is to earn \$30.

23.2 EVALUATING RISKY OUTCOMES

Learning Objective 23.2: Explain expected utility and risk preference.

Consider the following gamble. With an 80 percent chance, you will win \$400, and with a 20 percent chance, you will win \$2,500. The expected value of this gamble is $EV=.6\times\$1,000+.4\times\$2,500=\$1,600$. A **fair gamble** is one where the cost of the gamble is equal to the expected value. But how much would you be willing to pay to play this game? In order to answer that, we need to know about expected utility.

Expected utility (EU) is the probability-weighted average utility a person gets from each possible outcome of an uncertain situation. To understand this concept, we can apply it to the gamble. The expected utility from the above gamble is

$$EU = .6 \times U(\$1,000) + .4 \times U(\$2,500).$$

To look at a specific example, suppose a person's utility can be expressed as a function of money in the following way:

$$U(Money) = \sqrt{Money}$$

Then the expected utility from the above gamble is

$$EU = .6 imes \sqrt{1,000} + .4x\sqrt{2,500} = .6x31.62 + .2x50 pprox 29.$$

As with utility in general, this number does not mean anything in absolute terms, only as a relative measure. If instead this person were given the expected value of the gamble, \$1,600, for certain, they would get

$$Y(\$1,600) = \sqrt{1,600} = 40.$$

In other words, the guaranteed amount of \$1,600 yields higher utility than the gamble that has an expected value of \$1,600. This shows that the individual is risk averse.

A person who is unwilling to make a fair gamble, like the person above, is **risk averse**. A person who prefers the gamble to the guaranteed fair payout is **risk loving**. A person who is indifferent between the gamble and the fair payout is risk neutral.

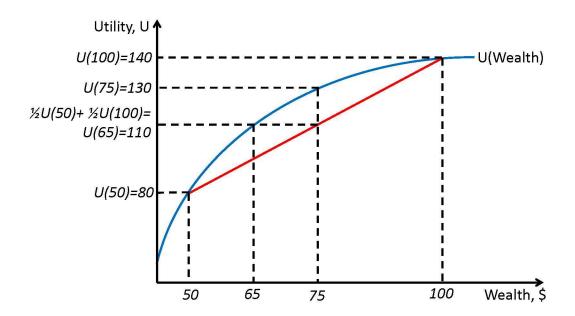


Figure 23.1 Graph of risk aversion

Figure 23.1 illustrates a person with a utility function with regard to wealth that is risk averse. The graph of the utility function has a declining slope as wealth increases. Consider two possible outcomes, \$50 and \$100. The graph tells us that the utility of \$50 for this agent is 80 and the utility for \$100 is 140. Remember that the value of the utility has no meaning in absolute terms, only in relative terms. So this agent prefers more wealth to less, but the marginal utility of wealth is decreasing. It is precisely this diminishing marginal utility of wealth that leads to risk aversion.

Now consider a game where a coin is flipped and the actual payment, \$50 or \$100, depends on which side of the coin is showing after the flip. This means that the agent has a 50 percent chance of getting \$50 and a 50 percent chance of getting \$100. In expected value, the game is worth \$75. The utility of \$75 for this agent is 130, as shown in the figure. The expected utility is the average of the utility levels at the two outcomes and can be seen as the midway point on the chord that connects the two points on the utility function. Expected utility is (.5)(80) + (.5)(140) = 110. This means that playing this risky game yields a utility of 110 for this agent.

What certain payment would yield the agent the same utility? If we look at the figure, we see that point d on the graph of the utility function is at \$65. The difference between the expected value of the gamble, \$75, and the amount of the certain payment that yields the same utility as the gamble, \$65, is called the risk premium. In this case, the risk premium is \$10. The risk premium is the amount an agent is willing to pay to avoid the risk of a fair gamble.

Graph of Risk-Neutral and Risk-Loving Utility Curve

Not all individuals are risk averse. An individual with a constant marginal utility of wealth is risk neutral, and an individual with an increasing marginal utility of wealth is risk loving. **Figure 23.2** illustrates both situations, using the same scenario as in **figure 23.1**. Note that there is no risk premium for the risk-neutral individual, and the risk-loving individual would actually suffer a cost if the gamble were removed.

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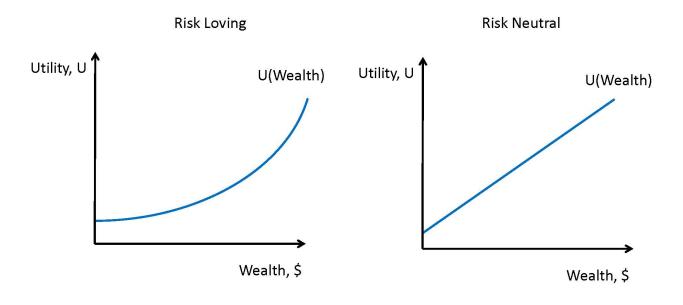


Figure 23.2.2 Risk-loving and risk-neutral utility curves

23.3 RISK REDUCTION

Learning Objective 23.3: Describe how diversification and insurance mitigate risk.

Risk-averse individuals wish to diminish or eliminate entirely the risks they face. Even risk-neutral individuals avoid unfair risks, and risk-loving individuals may wish to avoid very unfair risks. The easiest way to avoid risk is to abstain from risky activities, but it is not always possible to do so. A farmer, for example, cannot avoid the inherent variability of the weather. But there are some actions individuals can take to mitigate risk: drivers can drive more carefully, farmers can plant drought-resistant crops, and travelers can avoid airlines with poor safety records. Often, the ability to mitigate risk through conscious choices requires information about the risks. For example, in order to lower risk from air travel, a traveler would need access to the safety records of airlines.

Another way to reduce risk is through diversification. In a simple example, a farmer might plant some crops that grow well in dry conditions and others that grow well in wet conditions so that no matter if it is a wet or a dry year, the farmer will have at least one good harvest. This diversification requires that the risks are perfectly negatively correlated. Risks that are negatively correlated in general can be combined to reduce overall risk. For example, consider investing in the stock market. Investing in a few firms in the same industry is risky because their risks are probably positively correlated. If one firm in the automotive industry is doing poorly, it might be because demand for cars is soft and thus all automobile manufacturers might be doing poorly as a result. However, if you invest in many firms across a wide range of

industries, it is likely that some will do well, while others will do poorly, and therefore the overall risk will be reduced.

A common way that individuals reduce risk is through the purchase of insurance. Private insurance markets exist thanks to the risk premium described earlier in the chapter. Risk-averse individuals are willing to pay a price to avoid or lower risk. Risk-averse individuals will always choose to purchase fair insurance. Fair insurance is a contract that has an expected value to the insurer as zero—in other words, a fair bet. As a simple example, consider an auto insurance policy. Suppose there is a 1 percent chance a driver will have an accident in a year. If an accident occurs, the cost of the damage will be \$5,000. Thus the expected loss is (.1)(\$5,000), or \$50. A fair insurance contract is one that would fully insure against this loss and charge the driver exactly the expected cost, or \$50. This contract offers no profit for the insurance company, however. In fact, a risk-averse individual would be willing to buy insurance that is less than completely fair due to the risk premium, which gives rise to the private insurance industry.

The private insurance industry relies on diversified risk in order to stay in business. If an insurer has one thousand clients, each with a 1 percent risk of needing to make a claim, it is necessary that the 1 percent risk is not too positively correlated to avoid situations in which too many insured make claims in the same year. The insurance company relies on the fact that it can expect, on average, ten claims a year to keep its business going and not suffer a catastrophic loss from too many insured filing claims in the same year, which could bankrupt them. Take mortgage insurance, for example. Insurers will cover the loss to banks if a homeowner with a mortgage defaults. Normally, these risks are quite diverse, particularly if the insurer insures mortgages across a diverse geographical area so that an economic downturn in one city, like the closure of a large employer, will not cause too many claims at one time. This is normally a safe strategy, but the 2006 housing crisis in the United States spread across the entire country and led to a number of mortgage insurers falling into deep crises, most notably American International Group (AIG), which was bailed out by the US government to the tune of \$180 billion dollars and led to the government taking control of the firm.

23.4 THE POLICY QUESTION

SHOULD THE US GOVERNMENT PROVIDE FLOOD INSURANCE?

Learning Objective 23.4: Apply knowledge of risk and insurance to explain how systematic risk makes risk pools difficult and destroys private markets for insurance.

Risk-averse homeowners whose houses are situated in areas that have a possibility of flooding will have a demand for insurance as long as the insurance contract is within the risk premium the homeowners are willing to pay. But flood insurance is not easy to acquire on the private market. The reason for this is the fact that most people who wish to purchase flood insurance own homes in flood-prone areas. Floods are relatively uncommon but very costly. When a flood happens, most homes in the flood area are severely damaged, so the risks are highly and positively correlated. This makes insuring against floods very difficult for private insurers who struggle to diversify their risk portfolio and puts them in danger of a catastrophic payout should a flood occur. For this reason, much of private insurance is priced beyond the risk premium of private homeowners. This is exacerbated by the fact that it is common that homeowners in flood-prone areas are disproportionately low-income households because flood-prone land is generally cheaper than land in higher areas. Lower-income households have more limited resources with which to deal with the costs of a flood should they not have insurance.

For these reasons, the federal government has stepped into the flood insurance market and provides subsidized insurance for flood-prone households. The federal government has the resources to deal with correlated risks and expensive payouts that most private insurers do not.

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REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

23.1 What Are Risky Outcomes?

Learning Objective 23.1: Define risky outcomes, and describe how they are assessed.

23.2 Evaluating Risky Outcomes

<u>Learning Objective 23.2</u>: Explain expected utility and risk preference.

23.3 Risk Reduction

<u>Learning Objective 23.3</u>: Describe how diversification and insurance mitigate risk.

23.4 The Policy Question

Should the US Government Provide Flood Insurance?

<u>Learning Objective 23.4</u>: Apply knowledge of risk and insurance to explain how systematic risk makes risk pools difficult and destroys private markets for insurance.

LEARN: KEY TOPICS

Terms

Probabilities

Probabilities are numbers between zero and one that indicate the likelihood that a particular outcome will occur. Subjective probability is when individuals estimate probabilities based on their own experiences and whatever data are available to them.

Frequency

Frequency is how often a particular outcome has occurred over a known number of events.

Expected value

The expected value of an uncertain outcome is the sum of the value of each possible outcome multiplied by the probability it will occur.

Fair gamble

A fair gamble is one where the cost of the gamble is equal to the expected value.

Expected utility

Expected utility is the probability-weighted average utility a person gets from each possible outcome of an uncertain situation.

Risk averse

A person who is unwilling to make a fair gamble, like the person above, is risk averse.

Risk loving

A person who prefers the gamble to the guaranteed fair payout is risk loving.

Risk neutral

A person who is indifferent between the gamble and the fair payout is risk neutral.

Risk premium

The difference between the expected value of the gamble and the amount of the certain payment that yields the same utility as the gamble is called the risk premium.

Graphs

Graph of risk aversion

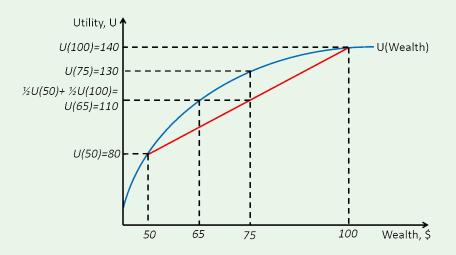


Figure 23.1 Graph of risk aversion

Risk-loving and risk-neutral utility curves

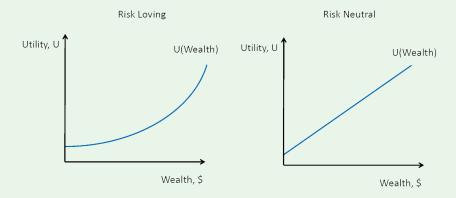


Figure 23.2 Risk-loving and risk-neutral utility curves

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CHAPTER 24

Time: Money Now or Money Later?

Money Now or Money Later?

THE POLICY QUESTION

SHOULD THE GOVERNMENT REGULATE THE PAYDAY LOAN INDUSTRY?

The term **payday lenders** describes businesses that provide short-term credit to generally more risky borrowers. They often charge high interest rates, and that has led them to become the target of government regulators who are concerned that they are unfairly taking advantage of a vulnerable population that is forced to accept terms that are unfavorable and damaging. Defenders of the businesses suggest that they are simply filling a need and that high interest rates are determined by the market and are a consequence of low repayment rates.

EXPLORING THE POLICY QUESTION

- 1. What is payday lending?
- 2. What is the justification for government regulations that place restrictions on the industry?

LEARNING OBJECTIVES

24.1 Present Discounted Value

Learning Objective 24.1: Explain how money in the future and in the past is given a value in the present.

24.2 Inflation

Learning Objective 24.2: Describe how inflation is accounted for in present value calculations.

24.3 Choices over Time

Learning Objective 24.3: Describe how individuals can use present value to make decisions over time.

24.4 Interest Rates

Learning Objective 24.4: Explain how interest rates are determined and how they change.

24.5 Policy Example

Should the Government Regulate the Payday Loan Industry?

<u>Learning Objective 24.5</u>: Apply knowledge of time in economics to evaluate the role of payday lenders and to determine if there is a role for the regulation of such lenders.

24.1 PRESENT DISCOUNTED VALUE

Learning Objective 24.1: Explain how money in the future and in the past is given a value in the present. Your grandmother gives you a savings bond that will pay you exactly \$100 in one year. You cannot cash it in until its maturity date, so it is not convertible into money until exactly one year. This chapter is about how we value money and other costs and benefits across time. The main force that determines the value of money across time is interest rates. Interest rates determine the return an individual gets for allowing others to use their money for a period of time. Formally, an **interest rate** is a percentage extra of an amount of money that must be paid to borrow that money for a fixed period of time. For example, if you put \$1,000 into a savings account that pays a simple 3 percent annual interest rate, *i*, then after one year, you would have

$$\$1,000(1+i) = \$1,000(1+.03) = \$1,000^*(1.03) = \$1,030$$

The interest rate allows us to do such calculations: determine the amount of money a person will gain after a determined amount of time from an investment or savings.

The **discount rate** is the method of placing a value on future consumption relative to present consumption. In general, individuals do not like to wait to consume, and waiting is a cost. The discount rate is a measure of the cost of waiting for consumption. Discount rates are personal; each individual has their own depending on how much they dislike waiting for consumption in the future. A person's willingness to lend money depends crucially on the discount rate. If a person has a very low discount rate, meaning that consumption in the future is almost as desirable as consumption today, they would be willing to loan money for a low interest rate. On the other hand, if they had a high discount rate, it would take a high interest rate to get them to lend money because lending that money means it is not available to fund current consumption.

Compounding is the process by which a sum of money, the principle, placed in an account that earns interest periodically, will grow based on the interest earned by the principle and by the subsequent interest payments.

For example, if \$1,000 is in a savings account that pays 3 percent interest annually, it will earn \$30 after a year. If that interest is withdrawn, leaving \$1,000 for the second year, it would earn another \$30, for a total interest income of \$60. So after five years, the total interest earned would be \$150, leaving a total of \$1,150. If instead the interest income is left in the account after the first year, in the second year, the account would earn interest on the \$1,030, or it would earn

$$\$1,030(1.03) = \$1,060.90$$

Thus, the process of compounding interest leads to an additional \$0.90 in interest. After five years, the total is

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$$1,000(1.03)(1.03)(1.03)(1.03)(1.03)$$
 or $1,000(1.03)^5 = 1,159.27$

The additional interest earned with compounding is \$9.27 over five years.

The general formula for the growth of money where the interest is left to accumulate is

$$P(1+i/n)^{nt}$$

where P is the original amount of money; the principle, i, is the interest rate in decimal terms; n is the number of times per year the interest is paid; and t is the number of years the principle and interest sit in the account. The more frequently the interest is paid, the faster the money in the account will grow. In the example above, suppose interest is paid quarterly rather than annually; instead of being paid once a year, it is paid four times a year. Applying the formula, we get

$$1,000(1+03/4)^{20} = 1,161.18$$

The more frequent interest payment leads to \$11.18 in interest income versus the \$9.27 earned with annual payments.

When growth is continuous, the exponential function describes the rate of growth. This is used to calculate things like population growth but also for accounts that pay and charge interest continuously, like many bank accounts, savings vehicles, and loans. The formula for the growth of money where the interest is left to accumulate for accounts that pay interest continuously is Pe^{it} , where[latex]e is the exponential function (expressed as "exp" on some calculators). This leads to the most rapid growth in money in an account. Using our example from before, the calculation is

$$\$1,000e^{(0.3)5} = \$1,161.83$$

Now that we know how interest rates work and are calculated, we can use them to calculate both future values, like we have been doing above, and present values. Future value (FV) is the value a sum of money is worth after a period of time if placed into an interest-earning account and left to accrue compound interest. Present value (PV) is what an amount of money that will be paid in the future is worth today given the interest rate. The best way to understand present value is to ask the question, How much money would I need to put into an account that earns the market interest rate today to have X amount of money at a specific time in the future? For example, if the market interest rate is 3 percent and the basic savings account pays interest annually, then the amount of money you would need to place into a savings account today in order to have \$103 in exactly one year is \$100. So the present value of \$103 in a year is \$100. Expressed as a formula, we would say that

$$PV(1.03) = \$103$$

Solving for PV yields

$$PV = (\$103/1.03) = \$100$$

In general the formula for PV is

$$PV = FV/(1+i)^t$$

for annual interest payments. For more frequent payments, the formula is

$$PV = FV/(1+i/n)^{nt}$$

For continuous interest payments, the formula becomes

$$PV = FV/e^{it}$$
.

As a final example, suppose you have a bond that will pay \$5,000 in exactly six years. If the market interest rate is 4.2 percent and accounts are paid continuously, the present value of the sum is

$$PV = \$5,000/e^{(.042)6} = \$3,886.22$$

Remember that \$3,886.22 is the exact amount of money you could put into an account that pays 4.2 percent interest continuously, and if you left the accrued interest in the account, in exactly six years, you would have \$5,000. In this way, we can compare the value of money through time, both in the future and in the present.

24.2 INFLATION

Learning Objective 24.2: Describe how inflation is accounted for in present value calculations.

In the future and present value calculations we made above, we ignored inflation. But in general, prices tend to rise over time. So though we calculate the amount of money we could put in a bank account today to have a precise sum after a fixed period of time, that sum might not buy as much if prices have risen over that time. In other words, the amount of *consumption* that \$100 allows falls over time if *nominal* prices rise. What we have done in the previous section is calculate present value in nominal terms, but what we generally want is to calculate present value in real terms using real, not nominal, prices. For example, if someone asks you to lend them \$10 to buy a cheeseburger, you might want to make sure that when they repay it in a year, they repay you enough money to buy the same cheeseburger. If the price of the burger has risen to \$12, then you would need to be repaid \$2 more to compensate for the price inflation. In real terms, the \$12 in a year is the same as \$10 today.

To adjust for inflation, g, we have to take it into account for our present value calculations. Let's start with an example of a \$100 debt that is due to be repaid in exactly one year. Suppose that inflation is 2 percent, or g=.02. The real amount you need to repay is \$100, but the nominal amount is \$100(1+g), or \$102. This is how much you would need to repay for the lender to be able to buy the same amount of consumption as they could with \$100 a year ago. Alternatively, the real value today of \$102 paid in a year is \$100.

To calculate the real present value of this future payment, we have to use the interest rate as before. To keep it in real terms, we need to convert the nominal interest rate to a real interest rate by adjusting it for inflation using the inflation rate. If r is the real interest rate, say 3 percent, then the value of \$100 next year is \$103 in real terms. To convert this to the nominal value, we have to multiply by (1+g), as seen above. If g is 2 percent, then we multiply \$103 by (1+.02) to get \$105.06. This is the amount that the borrower would have to repay in order for the real value of the repayment to be a 3 percent gain.

Note that the formula for this calculation is

$$P(1+r)(1+g)$$

where P is the principle amount (in this case \$100). From this, it is possible to describe the general formula for the nominal interest rate, i, as

$$1 + i = (1 + r)(1 + g)$$

Solving for *i* yields

$$i = r + rg + g$$

Solving this equation for r yields

$$r=rac{i-g}{1+g}$$

Note that if the interest rates and inflation rates are low, then 1+g is very close to 1, and the relationship between the real and nominal interest rates can be approximated as

$$rpprox i-q$$

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or the nominal interest rate minus inflation. In our example, the approximation is that the real interest rate is the nominal interest rate, 3 percent, minus the inflation rate, 2 percent, which is 1 percent. Since (.03-.02)/(1+.02) equals .098, or .98 percent, you can see the approximation is very close but not exactly the real interest rate.

To calculate the real present value of a sum of money, we use the real interest rate rather than the nominal interest rate. For example, using our values for nominal interest rates and inflation, we can calculate the value of \$100 in a year as worth \$100/(1+.0098), or \$99.03 in real terms. Note that in nominal terms, this would be \$100/(1+.03), or \$97.09. The difference is the erosion in the real value of the money due to inflation over the year. If you put \$97.09 in an account earning 3 percent interest, you would get exactly \$100 in a year, but that \$100 in a year would not buy the same amount of consumption as \$100 today would. So in order to get the same consumption as \$100 today in a year, you need to put \$99.03 in the account today (and you would get \$102 in nominal dollars in a year, which is exactly \$100 times the inflation rate).

24.3 CHOICES OVER TIME

Learning Objective 24.3: Describe how individuals can use present value to make decisions over time.

Now that we now know how to evaluate money and consumption across time, we can begin to study decisions across time. Let's start with an example: The owner of a business can invest in a new production technology that will increase profits by \$150,000 a year for five years. The cost of this technology is \$450,000. Should the owner make this investment?

Without thinking about time, you might think the answer is immediately obviously yes, as the stream of extra profits is \$750,000 and the cost is \$700,000. However, by using this logic, we are ignoring the fact that the owner has to wait for the extra profits. In order to compare the \$700,000 expenditure today to the future profits, we need to bring the future profits into the present. To do so, we need the interest rate, so for this example, suppose the real interest rate is 2 percent. Our calculation, then, is

$$PV = igg[rac{\$150,000}{(1+r)^1} + rac{\$150,000}{(1+r)^2} + rac{\$150,000}{(1+r)^3} + rac{\$150,000}{(1+r)^4} + rac{\$150,000}{(1+r)^5}igg].$$

Note that each of the payments is appropriately brought into real present value terms based on the formula and summed together. Since the real present value of the return on the investment is \$694,655.13 and the real present cost of the investment is \$700,000, the answer to our question is actually no, the owner should not make the investment.

A different way to think about the same kind of investment decisions is to think about the **net present value**, which considers the difference between the present value of the benefits of an action and the present value of the costs of the action. A rational economic actor such as a firm should undertake an investment only if the present value of the returns on the investment, R, is greater than the present value of the costs of the investment, C, or if R>C. Since net present value (NPV) is simply the difference between the two, the statement is equivalent to saying that the investment should only happen if net present value is positive, which gives us this rule:

$$NPV = R - C > 0$$

To calculate this, assume that the initial year is t=0, the firm's revenue in year t is R_t , and the firms cost in year t is C_t . The stream of revenues and costs ends in year T. The net present value rule is the following:

$$NPV = R - C \ = \left[R_0 + rac{R_1}{(1+r)^1} + rac{R_2}{(1+r)^2} + \ldots + rac{R_T}{(1+r)^T}
ight] - \left[C_0 + rac{C_1}{(1+r)^1} + rac{C_2}{(1+r)^2} + \ldots + rac{C_r}{(1+r)^T}
ight] > 0$$

Note that revenue minus costs is similar to profit and is profit if fixed and opportunity costs are included in

$$C: \Pi_t = R_t - C_t$$

We can rewrite the NPV rule as a cash-flow rule (or profit rule) that states that a firm should only undertake an investment if the net present value of the cash flow is positive. We can do this by rearranging terms in the expression above:

$$egin{aligned} NPV &= \left[R_0 - C_0 + rac{R_1 - C_1}{(1+r)^1} + rac{R_2 -_2}{(1+r)^2} + \ldots + rac{R_T - C_T}{(1+r)^T}
ight] \ &= \left[\Pi_0 + rac{\Pi_1}{(1+r)^1} + rac{\Pi_2}{(1+r)^2} + \ldots + rac{\Pi_T}{(1+r)^T}
ight] > 0 \end{aligned}$$

The expression makes clear that the decision to make an investment that has revenues and costs into the future depends not on the annual cash flow but on the present value of the net cash flow so that even an investment that has years in which there is a negative return in cash-flow terms can be a good investment over the life of the investment. For example, consider an investment that costs \$50 million in the first year and \$20 million a year for two more years. In the first year, there is no revenue; in the second, revenue is \$10 million; and in the third, revenue is \$100 million. Using the NPV formula with a real interest rate of r = 3 percent, we get the following:

$$NPV = -\$50 + rac{\$10 - \$20}{1.03} + rac{\$100 - \$20}{(1.03)^2} = -\$50 + rac{-\$10}{1.03} + rac{\$80}{1.0609} \ = -\$50 - \$9.7 + \$75.4 \ = \$15.7 > 0$$

So the firm should make this investment even though cash flow is negative for the first two years.

24.4 INTEREST RATES

Learning Objective 24.4: Explain how interest rates are determined and how they change.

Interest rates determine investment decisions. At the most basic level, interest rates represent the opportunity cost of investing money if the alternative is to put the money into an interest-earning savings account. But where does the market interest rate get determined? The market for borrowing and lending money is called the **capital market**, where the supply is the number of funds loaned, the demand is the number of funds borrowed, and the price is the interest rate itself. The capital market is a competitive market, and as such, the interest rate is determined in equilibrium. The market interest rate is the rate at which the number of funds supplied equals the number of funds demanded.

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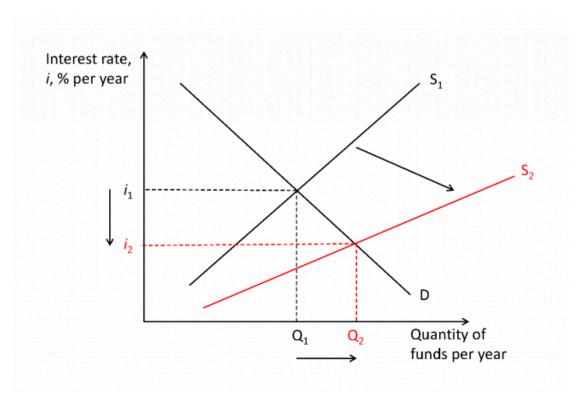


Figure 24.4.1 Capital market equilibrium

In **figure 24.1**, the capital market is initially in equilibrium at i_1 , Q_1 . The supply curve represents the number of funds offered to loans and is upward sloping because as interest rates rise, more funds are made available because of the higher return on loans. The demand curve represents the number of funds desired to borrow and is downward sloping because as interest rates fall, more funds are desired due to the lower expense of borrowing. At interest rate i_1 , the number of funds demanded equals the number of funds supplied, Q_1 .

The demand curve will shift based on opportunities to invest, a person needing funds to pay expenses like buying a house or paying for college, governments needing money to build roads and buildings, firms needing money to make new investments in plants and equipment, and so on. The supply curve will shift based on things like changes in tax policy that incentivize retirement investment, increased investment among foreigners, or the government's policy to buy back government bonds to increase the money supply. In **figure 24.1**, the supply curve shifts to the right, perhaps due to a new tax policy that incentivizes savings. The effect of the increased supply of funds leads to a lower interest rate, i_2 , and a greater amount of funds lent and borrowed, Q_2 .

24.5 POLICY EXAMPLE

SHOULD THE GOVERNMENT REGULATE THE PAYDAY LOAN INDUSTRY?

Learning Objective 24.5: Apply knowledge of time in economics to evaluate the role of payday lenders and to determine if there is a role for the regulation of such lenders.

Payday loans refer to loans that have a number of common features. The loans are generally small; \$500 is a common loan limit. The loans are usually repaid in a single payment on the borrower's next payday (hence the name). Loans are typically from two to four weeks in duration. Most lenders do not

evaluate individual borrowers' ability to repay the loan. As the <u>US Consumer Financial Protection Bureau</u> states,

Many state laws set a maximum amount for payday loan fees ranging from \$10 to \$30 for every \$100 borrowed. A typical two-week payday loan with a \$15 per \$100 fee equates to an annual percentage rate (APR) of almost 400 percent. By comparison, APRs on credit cards can range from about 12 percent to about 30 percent. In many states that permit payday lending, the cost of the loan, fees, and the maximum loan amount are capped.

Critics of payday lenders argue that the effective interest rates they charge (in the form of fees) are exorbitantly high and that these lenders are taking advantage of people with no other source of credit. The lenders themselves argue that credit markets are competitive and therefore the interest rates they charge are based on the market for small loans to people with very high default rates. The fact that borrowers are willing to pay such high rates suggests that the need for short-term credit is very high. On the other hand, critics suggest that the willingness to pay such high rates is evidence that consumers do not fully understand the costs or are driven out of desperation to borrow.

As seen in the quote above, many states have responded to the growth in payday lending with regulations that cap the loan amounts and limit the fees that the lenders can charge. Governments worry about low-income people being trapped in a cycle of debt, which effectively lowers their incomes even further due to the payment of fees. This does not address the source of the problem, however, which is the cause of the need for short-term credit itself.

REVIEW: TOPICS AND RELATED LEARNING OUTCOMES

24.1 Present Discounted Value

Learning Objective 24.1: Explain how money in the future and in the past is given a value in the present.

24.2 Inflation

Learning Objective 24.2: Describe how inflation is accounted for in present value calculations.

24.3 Choices over Time

Learning Objective 24.3: Describe how individuals can use present value to make decisions over time.

24.4 Interest Rates

Learning Objective 24.4: Explain how interest rates are determined and how they change.

24.5 Policy Example

Should the Government Regulate the Payday Loan Industry?

<u>Learning Objective 24.5</u>: Apply knowledge of time in economics to evaluate the role of payday lenders and to determine if there is a role for the regulation of such lenders.

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LEARN: KEY TOPICS

Terms

Interest rate

An interest rate is a percentage extra of an amount of money that must be paid to borrow that money for a fixed period of time.

Discount rate

The discount rate is the method of placing a value on future consumption relative to present consumption.

Compounding

Compounding is the process by which a sum of money, the principle, placed in an account that earns interest periodically, will grow based on the interest earned by the principle and by the subsequent interest payments.

Future value

Future value is the value a sum of money is worth after a period of time if placed into an interest-earning account and left to accrue compound interest.

Present value

Present value is what an amount of money that will be paid in the future is worth today given the interest rate.

Net present value

The net present value considers the difference between the present value of the benefits of an action and the present value of the costs of the action.

Capital market

The market for borrowing and lending money is called the capital market, where the supply is the number of funds loaned, the demand is the number of funds borrowed, and the price is the interest rate itself. The capital market is a competitive market, and as such, the interest rate is determined in equilibrium.

Graph

Capital market equilibrium

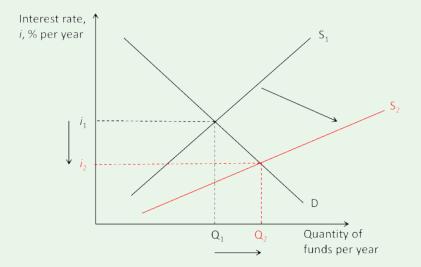


Figure 24.1 Capital market equilibrium

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• Said, Edward W. Culture and Imperialism. Knopf, 1994.

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- Davidson, Donald, *Essays on Actions and Events*. Oxford: Clarendon, 2001. https://biblioteca-mathom.files.wordpress.com/2012/10/essays-on-actions-and-events.pdf.
- Kerouac, Jack. *The Dharma Bums.* New York: Viking Press, 1958.

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| 1.02 | 12/18/2020 | Images and labels updated | All |
| 1.03 | 05/11/2021 | Equations updated | Module 1 |
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